02-Methods for Structure Determination and Analysis, Computing and Graphics

The further development of the EDH based approach is to consider the set of conditional histograms calculated from the points in the unit cell satisfying some additional restrictions. Such additional constraints may imply position of a point with respect to the molecular region or the values of some other functions connected with the object under investigation.

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PS-02.01.08 ELECTRON DENSITY SQUARING METHOD AND NON-CRYSTALLOGRAPHIC SYMMETRY. By A.F.Mishnev, Latvian Institute of Organic Synthesis, Riga, Latvia

Non-crystallographic symmetry imposes restraints on phases of the structure factors. Linear relationships among structure factors due to identical molecules in different crystallographic environment have been obtained by Main & Rossmann (Acta Cryst., 1966, 21, 67-72). For a structure containing like atoms the electron density squaring method (Sayre, Acta Cryst., 1952, 5, 60-65) may be introduced in the analysis of Main & Rossmann, that results in quadratic equations for the structure factors. In the presence of non-crystallographic symmetry the structure factor of the "squared" crystal takes the form

$$G_p = \sum_{n=1}^{N} \int_{U} \rho_1^2(x_1) \cdot \exp \left\{ 2\pi i ([C_n] x_1 + d_n) \right\} dx_1. \tag{1}$$

The "squared" structure factor may be expressed by $G_p = g_p/f_p \cdot F_p$. Let $\rho_2(x)$ be the electron density in a second crystal, which contains the same molecule. Since $\rho_2(x_1) = \rho_1(x_1)$ by definition, one can obtain the equations

$$F_p = \frac{f_p}{g_p V_K V_H} \sum_{K} \sum_{H} F_K \cdot F_H \cdot S_{KHP}. \tag{2}$$

where S_{PKH} are functions of molecular envelope, rotation and translation parameters. When the two crystals are identical equation (2) reduces to the Sayre's equation. Numerical test calculations of equations (2) using simulated crystal data will be presented.

PS-02.01.09 DIRECT PHASING FOR MACROMOLECULES BY ENTROPY MAXIMISATION AND LIKELIHOOD RANKING. By G. Bricogne, Department. of Molecular Biology, Biomedical Centre, Box 590, 751 24 Uppsala, Sweden; and LURE, Bâtiment 209D, 91405 Orsay, France.

A new multisolution phasing method based on entropy maximisation and likelihood ranking, proposed for the specific purpose of extending probabilistic direct methods to the field of macromolecules [Bricogne (1984). Acta Cryst. A40, 410-445], has been implemented in two different computer programs [Bricogne & Gilmore (1990). Acta Cryst. A46, 284-297; Bricogne (1993). Acta Cryst. D49, 37-60] and applied to a wide variety of problems. The latter comprise the determination of small crystal structures from X-ray diffraction data obtained from single crystals [Gilmore, Bricogne & Bannister (1990). Acta Cryst. A46, 297-308] or from powders [Bricogne (1991). Acta Cryst. A47, 803-829; Gilmore, K. Henderson & Bricogne (1991). Acta Cryst. A47, 830-841; Shankland, Gilmore, Bricogne & Hashizume (1993). Acta Cryst. A49, in the press], and from electron diffraction data partially phased by image processing of electron micrographs [Dong et al. (1992). Nature, Lond., 355, 605-609] or even unphased [Gilmore, Shankland & Bricogne (1993). Submitted to Proc. R. Soc.

London Ser. A.]; the ab initio generation [Bricogne (1993). Acta Cryst. D49, 37-60] and ranking [Gilmore, A.N. Henderson & Bricogne (1991). Acta Cryst. A47, 842-846] of phase sets for small proteins; and the improvement of poor quality phases for a larger protein at medium resolution under constraint of solvent flatness [Xiang, Carter, Bricogne & Gilmore (1993). Acta Cryst. D49, 193-212]. These applications show that the primary goal of this new method – namely increasing the accuracy and sensitivity of probabilistic phase indications compared with conventional direct methods – has been achieved.

The main components of the method as implemented in the computer program BUSTER [Bricogne (1993). Acta Cryst. D49, 37-60] are (1) a tree-directed search through a space of trial phase sets; (2) the saddlepoint method for calculating joint probabilities of structure factors, using entropy maximisation; (3) likelihood-based scores to rank trial phase sets and prune the search tree; (4) a new method for optimising the choice of reflexions so as to maximise the sensitivity of

the likelihood to their phases; (5) efficient schemes, based on errorcorrecting codes, for sampling trial phase sets; (6) a statistical analysis of the scores for automatically selecting reliable phase indications by multidimensional Fourier techniques coupled with tests of statistical significance. This program has been successfully tested on two small structures and has been applied to data from two small proteins. The mathematical techniques now available in BUSTER bring closer

The mathematical techniques now available in BUSTER bring closer a number of major enhancements of standard macromolecular phasing methods proposed earlier [Bricogne (1988). Acta Cryst. A44, 517-545] as an extension of the initial theory. In the molecular replacement method, for instance, the detection and placement of a known fragment described in a reference position and orientation by a density p^M with transform F^M can be accomplished by calculating the log-likelihood gain:

LLG (**R**, **t**) = log
$$\frac{\mathcal{P}(\left|F_{\mathbf{h}}\right| = \left|F_{\mathbf{h}}\right|^{\text{obs}} \text{ for all } \mathbf{h} \mid (\mathcal{H}_{1}[\mathbf{R}, \mathbf{t}]))}{\mathcal{P}(\left|F_{\mathbf{h}}\right| = \left|F_{\mathbf{h}}\right|^{\text{obs}} \text{ for all } \mathbf{h} \mid (\mathcal{H}_{0}))}$$

where (\mathcal{H}_0) denotes the null hypothesis that all atoms are uniformly distributed in the asymmetric unit while $(\mathcal{H}_1|\mathbf{R},\,\mathbf{t}|)$ denotes the alternative hypothesis that the known fragment is placed in the asymmetric unit with orientation \mathbf{R} at position \mathbf{t} , and the rest of the atoms are distributed at random. A drastic simplification of LLG yields a sum of (1) a Patterson correlation (PC) - based rotation function in which a sum of point-group symmetry-related copies of the self-Patterson of the rotated fragment is correlated with the origin-removed self-Patterson of the whole structure; and (2) a PC-based translation function, expressed as a Fourier series with argument \mathbf{t} itself. This function is already an improvement on the PC functions used in XPLOR [Brünger (1990). Acta Cryst. A46, 46-57], yet it is in general a poor approximation to LLG. It will be shown how the systematic use of LLG and of its relations to Bayesian statistical methods yields a new procedure for the detection and accurate placement of a known molecular fragment and of its recycling into the phasing process which overcomes every single limitation of the current methodology [Bricogne (1993). In The Molecular Replacement Method, edited. by W. Wolf, E.J. Dodson & S. Gover. Warrington: SERC Daresbury Laboratory, in the press].

PS-02.01.10 FOURIER-TRANSFORM-BASED METHODS FOR PHASE EXTENSION AND REFINEMENT AND PERHAPS THE SOLUTION OF MACROMOLECULES. By L Refaat, C Tate and M M Woolfson*, Department of Physics, University of York, UK.

The Sayre equation is known to be effective for phase extension and refinement, either alone (Sayre, D, 1972, Acta Cryst A28, 210-212) or in conjunction with other constraints, as in the SQUASH procedure (Main, P, 1990, Acta Cryst A46, 372-377).

A method is described by which the coefficients of a set of linear equations are derived, solely from FFT operations, leading to phase