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ly for the investigation of individual powder lines and their neighbourhood. The arrangement fully employs focusing in real space and the possibility of a control of strong correlation between the scattering angle φ and the neutron wavelength in the momentum space without any use of Soller collimators (Mikula, Wagner, Lukáš & Scherm, 1992; Lukáš, Vrána, Mikula, & Kulda, 1992). In this way, with a properly adjusted monochromator bending radius, the reflected neutrons corresponding to a chosen powder diffraction line at an angle φ are quasi-parallel in the scattering plane. Then the maximum flux of neutrons registered by a detector corresponds to the minimum FWHM of their angular distribution. To avoid a rather large angular uncertainty given by the divergence of a Soller collimator placed in front of the detector, for determining the position of the peak and its profile a spatially high resolution position sensitive detector (PSD) may be advantageously used. The FWHM of about 10^{-3} rad, and the high luminosity of the diffraction geometry strengthened by the use of PSD predict such an instrument for the employment in high resolution powder diffraction experiments e.g. for the investigation of line broadening in the case of plastically deformed crystals, the analysis of peak shifts (with a precision better than 10^{-4} rad) for the studies of residual stresses (Kulda, Mikula, Lukáš & Kocsis, 1992), time and temperature phase studies and particular inelastic scattering investigations. The luminosity and resolution of the diffraction arrangement which uses the bent perfect crystal monochromator will be compared with the arrangement using a conventional mosaic monochromator.

Kulda, J., Mikula, P., Lukáš, P. & Kocsis, M. (1992). *Physica B* 180 & 181, 1041-1043.

Lukáš, P., Vrána, M., Mikula, P. & Kulda, J. In *Proceedings of SPIE's 1992 International Symposium on Optical Applied Science and Engineering*, 22-24 July, San Diego, Conference Neutron Optical Devices and Applications, edited by C.F. Majkrzak & J.L. Wood, 1738, p. 438-446.

Mikula, P., Wagner, V., Lukáš, P. & Scherm, R. (1992). *Physica B* 180 & 181, 981-983.

PS-14.03.03 COMPARISON OF THE STATISTICAL DYNAMICAL THEORIES WITH MEASUREMENT OF INTEGRATED INTENSITY. By T. Takama, Department of Applied Physics, Faculty of Engineering, Hokkaido University, Japan.

Since N. Kato (NK) developed the statistical dynamical theory of diffraction (Acta Cryst. A36, 1980, 763-778), much effort has been devoted to improving and testing it. It is expressed in terms of the static Debye-Waller factor E and two correlation lengths for the phase factor τ and the wave-field amplitude Γ . Recently, the theory was reformulated by Becker and Al Haddad (BA) (Acta Cryst. A48, 1992, 121-134). The main difference exists in treating Γ which strongly affects the incoherent scattering. NK suggested that Γ is close to the extinction distance. On the other hand, BA showed theoretically that Γ should be of the same order of magnitude as τ . The two theories were

tested (Schneider, Bouchard, Graf & Nagasawa, Acta Cryst. A48, 1992, 804-819) experimentally by comparing them with the integrating reflection power of γ -ray measured for heat-treated Si as a function of crystal thickness. They concluded that the BA theory predicts excellently their data and the E parameter alone characterizes substantially the crystal imperfection.

In the present study, an attempt was made to verify which theory describes better the diffraction from specimens with various degree of imperfection. In order to introduce the randomly distributed micro defects, the parallel-sided Cz-Si crystals were heated systematically at 1223 K for different duration from 25 to 145 hr. The integrated intensities on the Laue case were successively measured for four reflections as a function of X-ray wavelength by the energy-dispersive diffraction method. The measured profiles showed remarkably the increase in the intensity as well as the decrease in both the period and the amplitude of the Pendelösung beats with increasing duration. The NK theory described the profiles very well assuming Γ to be constant for a reflection of a crystal (Takama, Harima & Sato, Acta Cryst. A46, 1990, C412). The BA theory taking account of the parameter E alone also fitted the profiles for relatively short heating duration as concluded by Schneider et al. For the specimens heated for longer duration, however, the comparison showed a poor agreement although three parameters were taken into consideration. This means that the NK theory with constant Γ is better to interpret the diffraction in the present development stage of the theory.

PS-14.03.04 ANGULAR MEASUREMENTS WITH X-RAY INTERFEROMETRY. By P. Becker, J. Stümpel and D. Windisch, Physikalisch-Technische Bundesanstalt, W-3300 Braunschweig, Germany.

The angular dependence of the reflectivity in a skew-symmetric X-ray interferometer with the axis of rotation between two pairs of the reflecting wafers has been investigated experimentally and theoretically. Rapid oscillations with a periodicity of almost two milliseconds of angle have been observed. The period depends on the geometry and the lattice spacing of the silicon crystal. The amplitudes of the angular oscillations are strongly affected by "Pendelösung" interference phenomena. As an example of applications an optical autocollimator is calibrated by the X-ray interferometer.

A triple-Laue X-ray interferometer capable of angular measurements in the range below a second of angle was first proposed and put into operation by Becker & Bonse (1974). They used two pairs of lamellae in a skew-symmetric arrangement with an axis of rotation between them and measured the intensity oscillating in the outgoing X-ray beams taking into account the alignment parameters between the separate parts of the interferometer. They found as a result of the geometrical treatment, that the periodicity of the oscillations depends on the angle of rotation and the lamellae distance in one subunit, lamellae thickness and the lattice spacing. Their calculations, however, did not include information about the angular range and amplitude of the oscillations in the reflectivity of the interferometer.

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The aim of this paper is to calculate the integrated reflectivity of a skew-symmetric triple-Laué interferometer under variable geometry conditions and with absorption. In these calculations we follow the path of Bonse & Graeff (1977) expanded by subunit rotations. Further we discuss the design of the interferometer used for the experiment, in which a new developed optical autocollimator (ACT) capable of resolving 0.000 01 sec of arc is calibrated by angular X-ray interferometry.

PS-14.03.05 MODIFIED BRAGG LAW FOR HETEROLAYER STRUCTURES. By W.A. Keller* and D.S. de Vasconcelos, Instituto de Física, Universidade Federal da Bahia, Salvador-Ba, Brazil.

X-ray diffraction patterns for stratified structures including epilayers and superlattice structure are analyzed by an approach which was first developed for the self-consistent EM scattering by a single plane of dipoles, considered as a unit of scattering. The rigorous vectorial waves solution for the σ - and π -states of polarization has previously been found for the scattering unit and extended to a whole crystal, represented by a stack of such units. The guiding principle was the simple demand, of continuity of EM field vectors between all the units. As a result, a modified Bragg law for a perfect big crystal was obtained. We now join the known solutions for homogeneous crystal structures to resolve the scattering problem for stratified structures, for which individual components can have origin in different crystal structures as, for instance, Ge and GaAs. Again, we use the same guiding principle of continuity of EM field vectors between all the components. By this approach it is possible to obtain diffraction profiles for selected structures, that previously could only be handled by some hybrid kinematic-dynamic types of approach (S. Bensoussan, C. Malgrange and M. Sauvage-Simkin, 1987, *J. Appl. Cryst.* **20**, 222 and A. Authier, J. Gronkowski and C. Malgrange, 1987, *Acta Cryst.* **A45**, 432).

The infinite multi-superlattice structures show the diffraction profiles with features such as a sequence of tophat curves for each satellite reflection (Fig.1a). The respective total reflection regions (TRR) depend, in a critical way, on the charge densities of the component units, their structure factors and the polarization state of the incident radiation. This dependence is of the same type as that observed for the main peak and it is preserved even in cases when TRR is reduced to fractions of the arc second. The angular region of the latter depends, for a given order of reflection, on chemical composition, homogeneous layer thickness, charge density value and inter- and intra-layer distances between scattering units.

The finite multi-superlattice and multi-epilayer structures display diffraction patterns of the kinematic type. A continuous transformation of the diffraction-profiles from kinematic to dynamic type can occur as a result of a simple change of numerical value of two parameters, which depend on structure components, such as the layer thickness and the charge density of the respective component (Fig.1b).

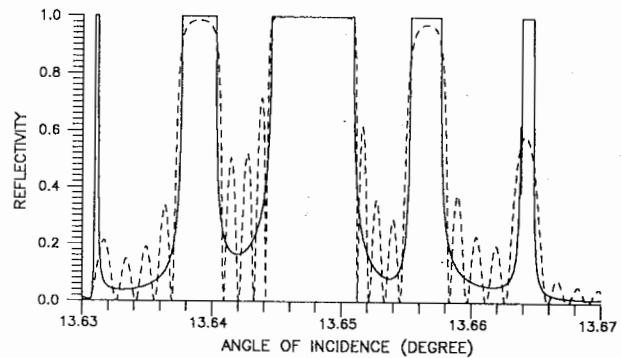


FIG.1: SUPERLATTICE STRUCTURE OF 1024*(111)Ge-700*(111)GaAs
 — 1a INFINITE NUMBER OF UNITS
 - - - 1b 4 UNITS

An attempt is made to formulate a modified Bragg law version for satellites for the multilayer superstructures with appropriate indices of refraction intrinsically included into the scattering model.

PS-14.03.06 AN EXACT AND ANALYTIC GEOMETRY OF BRAGG DIFFRACTION By Hsueh-Hsing Hung, Synchrotron Radiation Research Center, Taiwan

A novel interpretation of Bragg diffraction is reported. We have found a simple way to precisely reformulate the dynamical theory of diffraction so as to derive several important results with their clear geometric meaning on the well-constructed dispersion surface. Poynting vector is proved normal to the dispersion surface, on which a corrected hyperbola is proposed. By contrast with the conventional theories, our results not only propose a picture for the first time to cover the refraction (Fresnel's reflectivity) and diffraction (Darwin's curve) in all the angular range, but can be easily applied to the generic diffraction phenomena in periodic structure. The physics of Bragg diffraction is common in nature, the geometry should be expected simple. It is indeed and will be presented in this talk.

PS-14.03.07 DIRECT OBSERVATION OF DIFFRACTED X-RAY BEAM IN THE FORWARD DIRECTION FROM THIN AND IMPERFECT NATURAL DIAMOND CRYSTALS. By Krishan Lal*, S. Niranjana N. Goswami and Ajit Ram Verma, National Physical Laboratory, New Delhi - 110 012, India.

We have succeeded in direct observation and study of diffracted beams in the forward direction, in the case of thin