

# Terbium(III) hydrogendiphosphate(V) tetrahydrate

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Key indicators: single-crystal X-ray study;  $T = 295\text{ K}$ ; mean  $\sigma(\text{P}-\text{O}) = 0.002\text{ \AA}$ ;  $R$  factor = 0.012;  $wR$  factor = 0.034; data-to-parameter ratio = 11.9.

The Tb atom of the title compound,  $\text{TbHP}_2\text{O}_7\cdot 4\text{H}_2\text{O}$ , is coordinated by the O atoms of three symmetrically independent water molecules and by five O atoms belonging to  $\text{HP}_2\text{O}_7^-$  groups. The  $\text{TbO}_8$  polyhedra are interconnected by the diphosphate anions, forming a three-dimensional network which is additionally stabilized by  $\text{O}-\text{H}\cdots\text{O}$  hydrogen bonding between water molecules and O atoms of the  $\text{HP}_2\text{O}_7^-$  anions. Uncoordinated water molecules are situated in channels and are connected *via* hydrogen bonds with the framework.

## Related literature

Isostructural compounds of the type  $\text{REHP}_2\text{O}_7\cdot 4\text{H}_2\text{O}$  were reported for  $\text{RE} = \text{Sm}$  by Chehimi-Moumen *et al.* (2002), for  $\text{RE} = \text{Gd}$  by Hraiech *et al.* (2005) and for  $\text{RE} = \text{Eu}$  by Anna-Rabah *et al.* (2006).

## Experimental

### Crystal data

$\text{TbHP}_2\text{O}_7\cdot 4\text{H}_2\text{O}$

$M_r = 405.9$

Monoclinic,  $P_{2_1}/n$

$a = 6.6006 (6)\text{ \AA}$

$b = 11.4744 (9)\text{ \AA}$

$c = 11.7252 (13)\text{ \AA}$

$\beta = 92.150 (8)^\circ$

$V = 887.42 (15)\text{ \AA}^3$

$Z = 4$

Mo  $K\alpha$  radiation

$\mu = 8.38\text{ mm}^{-1}$

$T = 295\text{ K}$

$0.14 \times 0.06 \times 0.03\text{ mm}$

### Data collection

Oxford Diffraction Xcalibur 2 diffractometer with Sapphire 2 CCD area-detector

Absorption correction: analytical [*CrysAlis RED* (Oxford Diffraction, 2005), using a multi-faceted crystal model based on

expressions derived by Clark & Reid (1995)]

$T_{\min} = 0.329$ ,  $T_{\max} = 0.635$

8671 measured reflections

1850 independent reflections

1628 reflections with  $I > 3\sigma(I)$

$R_{\text{int}} = 0.019$

### Refinement

$R[F^2 > 2\sigma(F^2)] = 0.011$

$wR(F^2) = 0.034$

$S = 1.21$

1850 reflections

155 parameters

10 restraints

H atoms treated by a mixture of independent and constrained refinement

$\Delta\rho_{\max} = 0.29\text{ e \AA}^{-3}$

$\Delta\rho_{\min} = -0.21\text{ e \AA}^{-3}$

**Table 1**  
Selected bond lengths ( $\text{\AA}$ ).

Tb1–O1	2.3145 (17)	P1–O1	1.5129 (18)
Tb1–O2 <sup>i</sup>	2.2877 (17)	P1–O2	1.5063 (18)
Tb1–O3 <sup>ii</sup>	2.3514 (18)	P1–O3	1.5169 (19)
Tb1–O5	2.3718 (18)	P1–O7	1.6201 (18)
Tb1–O6 <sup>iii</sup>	2.3842 (17)	P2–O4	1.562 (2)
Tb1–O8	2.605 (2)	P2–O5	1.4957 (19)
Tb1–O9	2.433 (2)	P2–O6	1.4891 (18)
Tb1–O10	2.421 (2)	P2–O7	1.6116 (18)

Symmetry codes: (i)  $x + 1, y, z$ ; (ii)  $-x + 1, -y + 1, -z + 2$ ; (iii)  $-x + \frac{3}{2}, y - \frac{1}{2}, -z + \frac{3}{2}$ .

**Table 2**

Hydrogen-bond geometry ( $\text{\AA}$ ,  $^\circ$ ).

$D-\text{H}\cdots A$	$D-\text{H}$	$\text{H}\cdots A$	$D\cdots A$	$D-\text{H}\cdots A$
O4–H41 $\cdots$ O11	0.813 (13)	1.736 (14)	2.546 (3)	174 (3)
O8–H81 $\cdots$ O1 <sup>ii</sup>	0.82 (2)	1.98 (3)	2.762 (3)	159 (3)
O8–H82 $\cdots$ O3 <sup>i</sup>	0.822 (18)	2.231 (14)	2.972 (3)	150 (3)
O9–H91 $\cdots$ O4 <sup>iv</sup>	0.83 (3)	2.06 (3)	2.851 (3)	161 (3)
O9–H92 $\cdots$ O8 <sup>iii</sup>	0.828 (18)	1.95 (2)	2.750 (3)	164 (3)
O10–H101 $\cdots$ O5 <sup>iii</sup>	0.82 (2)	2.16 (3)	2.880 (3)	147 (3)
O10–H102 $\cdots$ O7 <sup>v</sup>	0.812 (16)	2.28 (2)	2.991 (3)	147 (3)
O11–H111 $\cdots$ O3 <sup>v</sup>	0.80 (2)	2.18 (2)	2.941 (3)	157 (3)

Symmetry codes: (i)  $x + 1, y, z$ ; (ii)  $-x + 1, -y + 1, -z + 2$ ; (iii)  $-x + \frac{3}{2}, y - \frac{1}{2}, -z + \frac{3}{2}$ ; (iv)  $-x + 1, -y + 1, -z + 1$ ; (v)  $-x + \frac{1}{2}, y - \frac{1}{2}, -z + \frac{3}{2}$ .

Data collection: *CrysAlis CCD* (Oxford Diffraction, 2005); cell refinement: *CrysAlis RED* (Oxford Diffraction, 2005); data reduction: *CrysAlis RED*; program(s) used to solve structure: *SIR2002* (Burla *et al.*, 2003); program(s) used to refine structure: *JANA2000* (Petříček *et al.*, 2007); molecular graphics: *DIAMOND* (Brandenburg & Putz, 2005); software used to prepare material for publication: *JANA2000*.

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: WM2172).

## References

- Anna-Rabah, Z., Chehimi-Moumen, F., Ben Hassen-Chehimi, D. & Trabelsi-Ayadi, M. (2006). *Solid State Sci.* **8**, 932–939.
- Brandenburg, K. & Putz, H. (2005). *DIAMOND*. Version 3. Crystal Impact GbR, Postfach 1251, D-53002 Bonn, Germany.
- Burla, M. C., Camalli, M., Carrozzini, B., Casciaro, G. L., Giacovazzo, C., Polidori, G. & Spagna, R. (2003). *J. Appl. Cryst.* **36**, 1103.
- Chehimi-Moumen, F., Ferid, M., Ben-Hassen-Chehimi, D. & Trabelsi-Ayadi, M. (2002). *Solid State Sci.* **4**, 979–983.
- Clark, R. C. & Reid, J. S. (1995). *Acta Cryst.* **A51**, 887–897.
- Hraiech, S., Chehimi-Moumen, F., Ferid, M., Ben Hassen-Chehimi, D. & Trabelsi-Ayadi, M. (2005). *Mater. Res. Bull.* **40**, 2170–2179.
- Oxford Diffraction (2005). *CrysAlis CCD* and *CrysAlis RED*. Oxford Diffraction Ltd, Abingdon, Oxfordshire, England.
- Petříček, V., Dušek, M. & Palatinus, L. (2007). *JANA2000*. Institute of Physics, Prague, Czech Republic.

# supporting information

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## **Terbium(III) hydrogendiphosphate(V) tetrahydrate**

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### **S1. Comment**

Acidic rare earth diphosphates of general formula  $\text{REHP}_2\text{O}_7\text{nH}_2\text{O}$  exhibit interesting luminescent and optical properties (Hraiech *et al.*, 2005 and references herein). The title compound is isostructural with other compounds of formula type  $\text{REHP}_2\text{O}_7\text{4H}_2\text{O}$ ,  $\text{RE} = \text{Sm}$  (Chehimi-Moumen *et al.*, 2002),  $\text{Gd}$  (Hraiech *et al.*, 2005), and  $\text{Eu}$  (Anna-Rabah *et al.*, 2006).

The structure of  $\text{TbHP}_2\text{O}_7\text{4H}_2\text{O}$  is made up of  $\text{TbO}_8$  polyhedra and  $\text{HP}_2\text{O}_7$  groups that form a three-dimensional framework. In channels running along  $a$  (Fig. 2) free water molecules are located which are connected *via* hydrogen bonds with the framework (see hydrogen-bonding Table).

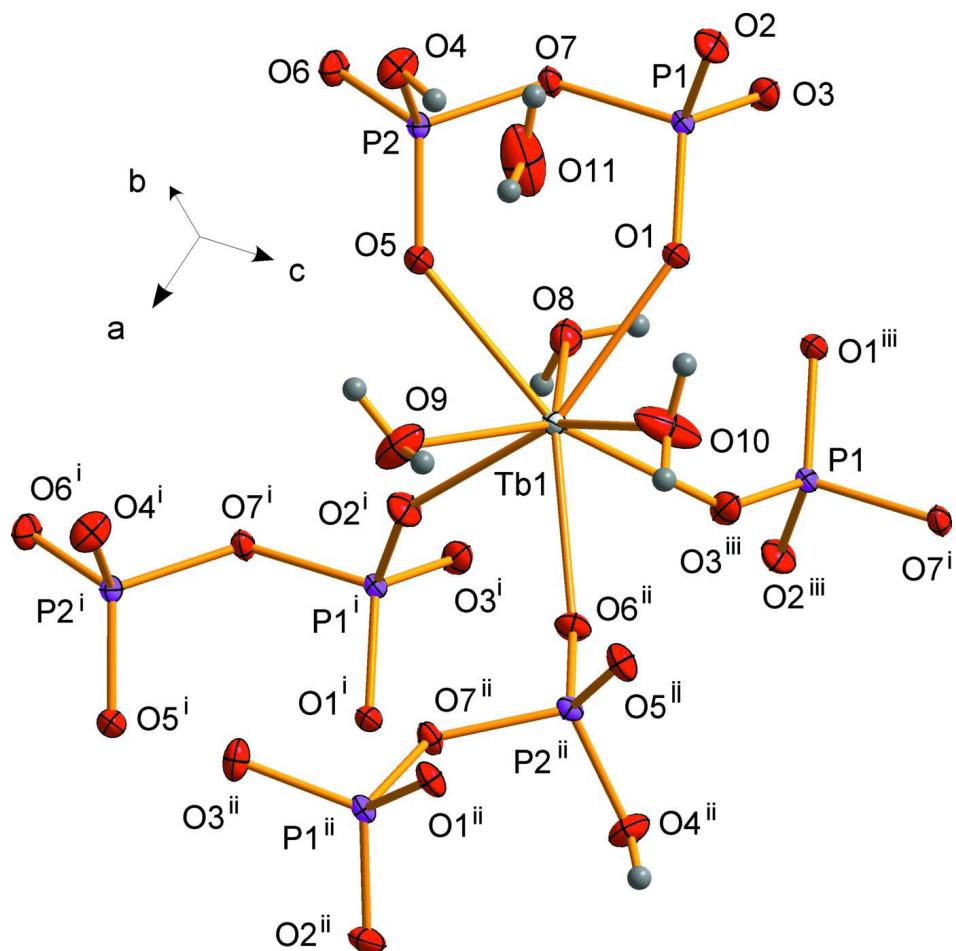
The  $\text{P}_2\text{O}_7$  group is protonated, with the H atom located at O4 (Fig. 1), as also indicated by elongation of the corresponding P—O distance. The bridging angle P1—O7—P2 between the two  $\text{PO}_4$  tetrahedra is 130.73 (11)°.

### **S2. Experimental**

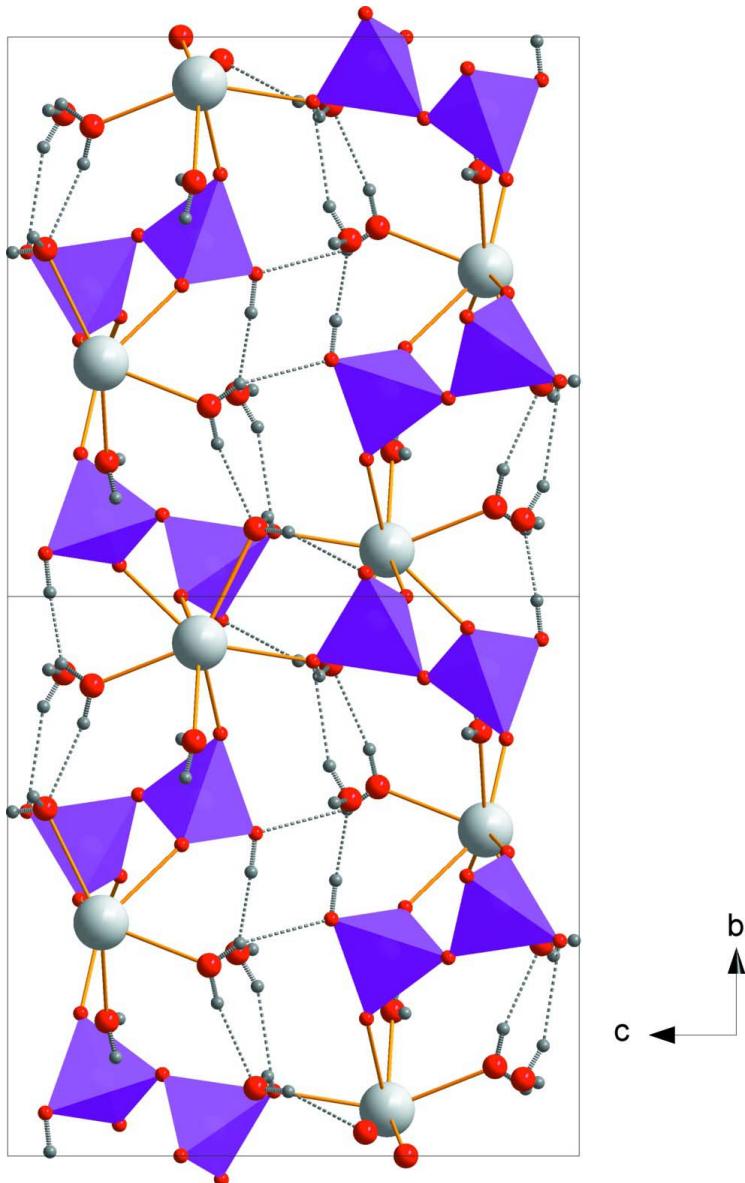
An aqueous solution of  $\text{TbCl}_3\text{6H}_2\text{O}$  (0.1*M*) was added dropwise to anhydrous  $\text{Na}_4\text{P}_2\text{O}_7$  dissolved in distilled water (0.1*M*). The pH of the mixture was controlled with diluted hydrochloric acid to be slightly acidic, and the solution was stirred for two h at room temperature. Prismatic-shaped colourless crystals with a maximal size of 0.3 mm formed after a few days on slow evaporation.

### **S3. Refinement**

The H atoms were localized from a difference Fourier map. Their coordinates were refined independently with O—H distances restrained to 0.82 (1) Å. The isotropic temperature parameters of the H atoms were refined with 1.2*U*<sub>eq</sub> of the parent atom. The H111—O11—H112 angle of the free water molecule was restrained to 109.47 (10)°.

**Figure 1**

Part of the structure of  $\text{HTbP}_2\text{O}_7 \cdot 4\text{H}_2\text{O}$  drawn with displacement ellipsoids at the 50% probability level. [Symmetry codes: (i)  $1 + x, y, z$ ; (ii)  $1.5 - x, -1/2 + y, 1.5 - z$ ; (iii)  $1 - x, 1 - y, 2 - z$ ]

**Figure 2**

The packing of  $\text{TbHP}_2\text{O}_7\cdot 4\text{H}_2\text{O}$  viewed along **a**. Hydrogen bonds are represented by dashed lines. Colour code: Pink ( $\text{P}_2\text{O}_7$  polyhedra), red spheres (O), grey spheres (Tb), dark grey spheres (H). All atoms are displayed with arbitrary radii. For clarity, O atoms belonging to  $\text{PO}_4$  tetrahedra have a smaller size than O atoms of water molecules. O atoms that would obscure H atoms important for understanding the hydrogen bonding scheme are plotted semitransparently.

### Terbium(III) hydrogendifphosphate(V) tetrahydrate

#### Crystal data

$\text{TbHP}_2\text{O}_7\cdot 4\text{H}_2\text{O}$

$M_r = 405.9$

Monoclinic,  $P2_1/n$

Hall symbol: -P 2yn

$a = 6.6006 (6)$  Å

$b = 11.4744 (9)$  Å

$c = 11.7252 (13)$  Å

$\beta = 92.150 (8)^\circ$

$V = 887.42 (15)$  Å<sup>3</sup>

$Z = 4$

$F(000) = 768$

$D_x = 3.037 \text{ Mg m}^{-3}$

Mo  $K\alpha$  radiation,  $\lambda = 0.71069 \text{ \AA}$   
 Cell parameters from 972 reflections  
 $\theta = 2.5\text{--}26.5^\circ$   
 $\mu = 8.38 \text{ mm}^{-1}$

$T = 295 \text{ K}$   
 Prism, colorless  
 $0.14 \times 0.06 \times 0.03 \text{ mm}$

#### Data collection

Oxford Diffraction CCD  
 diffractometer  
 Radiation source: X-ray tube  
 Graphite monochromator  
 Detector resolution: 8.3438 pixels  $\text{mm}^{-1}$   
 $\omega$  scans  
 Absorption correction: analytical  
 [CrysAlis RED (Oxford Diffraction, 2005),  
 using a multifaceted crystal model based on  
 expressions derived by Clark & Reid (1995)]

$T_{\min} = 0.329, T_{\max} = 0.635$   
 8671 measured reflections  
 1850 independent reflections  
 1628 reflections with  $I > 3\sigma(I)$   
 $R_{\text{int}} = 0.019$   
 $\theta_{\max} = 26.6^\circ, \theta_{\min} = 2.5^\circ$   
 $h = -8 \rightarrow 7$   
 $k = -14 \rightarrow 14$   
 $l = -14 \rightarrow 14$

#### Refinement

Refinement on  $F^2$   
 $R[F^2 > 2\sigma(F^2)] = 0.011$   
 $wR(F^2) = 0.034$   
 $S = 1.21$   
 1850 reflections  
 155 parameters  
 10 restraints  
 9 constraints  
 H atoms treated by a mixture of independent  
 and constrained refinement

Weighting scheme based on measured s.u.'s  $w =$   
 $1/[\sigma^2(I) + 0.0004I^2]$   
 $(\Delta/\sigma)_{\max} = 0.009$   
 $\Delta\rho_{\max} = 0.29 \text{ e \AA}^{-3}$   
 $\Delta\rho_{\min} = -0.21 \text{ e \AA}^{-3}$   
 Extinction correction: B-C type 1 Lorentzian  
 isotropic [Becker, P. J. & Coppens, P. (1974).  
 Acta Cryst. A30, 129–147]  
 Extinction coefficient: 2.9 (8)

#### Special details

**Refinement.** The refinement was carried out against all reflections. The conventional  $R$ -factor is always based on  $F$ . The goodness of fit as well as the weighted  $R$ -factor are based on  $F$  and  $F^2$  for refinement carried out on  $F$  and  $F^2$ , respectively. The threshold expression is used only for calculating  $R$ -factors etc. and it is not relevant to the choice of reflections for refinement.

The program used for refinement, Jana2000, uses the weighting scheme based on the experimental expectations, see \_refine\_ls\_weighting\_details, that does not force  $S$  to be one. Therefore the values of  $S$  may be larger than the ones from the SHELX program.

#### Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters ( $\text{\AA}^2$ )

	$x$	$y$	$z$	$U_{\text{iso}}^*/U_{\text{eq}}$
Tb1	0.755557 (17)	0.417027 (10)	0.836213 (10)	0.00831 (5)
P1	0.25551 (9)	0.54805 (6)	0.85787 (5)	0.00834 (18)
P2	0.47954 (9)	0.63300 (5)	0.66266 (5)	0.00860 (18)
O1	0.4213 (3)	0.45787 (15)	0.87403 (15)	0.0122 (5)
O2	0.0629 (3)	0.50007 (16)	0.80317 (16)	0.0157 (5)
O3	0.2158 (3)	0.61576 (15)	0.96588 (15)	0.0149 (5)
O4	0.3423 (3)	0.57670 (15)	0.56618 (17)	0.0169 (6)
O5	0.6553 (3)	0.55618 (15)	0.69557 (16)	0.0137 (5)
O6	0.5259 (2)	0.75465 (15)	0.62791 (15)	0.0135 (5)
O7	0.3378 (3)	0.64547 (14)	0.77094 (14)	0.0112 (5)
O8	0.7671 (3)	0.62083 (18)	0.93419 (17)	0.0177 (6)
O9	0.8201 (4)	0.34050 (17)	0.64753 (17)	0.0252 (7)

O10	0.5535 (3)	0.24098 (19)	0.8262 (2)	0.0333 (7)
O11	0.2577 (4)	0.36300 (19)	0.5980 (2)	0.0394 (9)
H81	0.697 (4)	0.614 (3)	0.9904 (18)	0.0212*
H111	0.294 (4)	0.3021 (18)	0.572 (3)	0.0472*
H82	0.881 (2)	0.643 (3)	0.955 (2)	0.0212*
H112	0.141 (2)	0.375 (3)	0.577 (3)	0.0472*
H101	0.593 (5)	0.1757 (15)	0.810 (3)	0.04*
H91	0.776 (5)	0.380 (3)	0.593 (2)	0.0303*
H92	0.777 (4)	0.2742 (13)	0.633 (3)	0.0303*
H41	0.323 (4)	0.5072 (10)	0.574 (3)	0.0203*
H102	0.434 (2)	0.243 (3)	0.807 (3)	0.04*

*Atomic displacement parameters ( $\text{\AA}^2$ )*

	$U^{11}$	$U^{22}$	$U^{33}$	$U^{12}$	$U^{13}$	$U^{23}$
Tb1	0.00694 (8)	0.00827 (8)	0.00975 (8)	0.00064 (4)	0.00087 (5)	0.00041 (4)
P1	0.0067 (3)	0.0093 (3)	0.0092 (3)	0.0008 (2)	0.0021 (2)	0.0011 (2)
P2	0.0082 (3)	0.0085 (3)	0.0092 (3)	-0.0007 (2)	0.0009 (2)	0.0011 (2)
O1	0.0097 (9)	0.0127 (8)	0.0146 (9)	0.0029 (7)	0.0037 (7)	0.0037 (7)
O2	0.0095 (9)	0.0182 (9)	0.0192 (10)	-0.0040 (7)	-0.0004 (8)	0.0001 (7)
O3	0.0201 (10)	0.0137 (8)	0.0110 (10)	0.0048 (8)	0.0034 (7)	-0.0010 (7)
O4	0.0225 (11)	0.0120 (9)	0.0157 (10)	-0.0038 (8)	-0.0041 (8)	-0.0012 (7)
O5	0.0113 (9)	0.0156 (9)	0.0143 (10)	0.0031 (7)	0.0031 (8)	0.0039 (7)
O6	0.0141 (9)	0.0107 (8)	0.0159 (9)	-0.0034 (7)	0.0016 (7)	0.0022 (7)
O7	0.0115 (9)	0.0091 (8)	0.0133 (9)	0.0003 (7)	0.0055 (7)	0.0018 (7)
O8	0.0163 (11)	0.0208 (10)	0.0160 (11)	-0.0033 (9)	0.0013 (8)	0.0035 (8)
O9	0.0432 (13)	0.0160 (10)	0.0159 (11)	0.0057 (10)	-0.0061 (9)	-0.0017 (8)
O10	0.0138 (10)	0.0163 (10)	0.0697 (17)	-0.0019 (9)	-0.0005 (11)	-0.0122 (11)
O11	0.0541 (17)	0.0120 (11)	0.0542 (16)	-0.0102 (10)	0.0317 (14)	-0.0094 (10)

*Geometric parameters ( $\text{\AA}$ ,  $^\circ$ )*

Tb1—O1	2.3145 (17)	P1—O1	1.5129 (18)
Tb1—O2 <sup>i</sup>	2.2877 (17)	P1—O2	1.5063 (18)
Tb1—O3 <sup>ii</sup>	2.3514 (18)	P1—O3	1.5169 (19)
Tb1—O5	2.3718 (18)	P1—O7	1.6201 (18)
Tb1—O6 <sup>iii</sup>	2.3842 (17)	P2—O4	1.562 (2)
Tb1—O8	2.605 (2)	P2—O5	1.4957 (19)
Tb1—O9	2.433 (2)	P2—O6	1.4891 (18)
Tb1—O10	2.421 (2)	P2—O7	1.6116 (18)
O1—Tb1—O2 <sup>i</sup>	143.70 (6)	O6 <sup>iii</sup> —Tb1—O8	128.03 (6)
O1—Tb1—O3 <sup>ii</sup>	83.41 (6)	O6 <sup>iii</sup> —Tb1—O9	75.70 (7)
O1—Tb1—O5	75.74 (6)	O6 <sup>iii</sup> —Tb1—O10	71.65 (6)
O1—Tb1—O6 <sup>iii</sup>	134.37 (6)	O8—Tb1—O9	136.20 (6)
O1—Tb1—O8	75.29 (6)	O8—Tb1—O10	141.01 (7)
O1—Tb1—O9	116.61 (7)	O9—Tb1—O10	76.69 (8)
O1—Tb1—O10	69.56 (7)	O1—P1—O2	113.46 (10)

O2 <sup>i</sup> —Tb1—O3 <sup>ii</sup>	101.23 (6)	O1—P1—O3	113.12 (10)
O2 <sup>i</sup> —Tb1—O5	80.10 (6)	O1—P1—O7	107.03 (10)
O2 <sup>i</sup> —Tb1—O6 <sup>iii</sup>	79.67 (6)	O2—P1—O3	111.92 (11)
O2 <sup>i</sup> —Tb1—O8	71.90 (6)	O2—P1—O7	106.35 (10)
O2 <sup>i</sup> —Tb1—O9	79.03 (7)	O3—P1—O7	104.14 (10)
O2 <sup>i</sup> —Tb1—O10	146.08 (7)	O4—P2—O5	111.48 (10)
O3 <sup>ii</sup> —Tb1—O5	143.50 (6)	O4—P2—O6	107.99 (10)
O3 <sup>ii</sup> —Tb1—O6 <sup>iii</sup>	71.04 (6)	O4—P2—O7	105.60 (10)
O3 <sup>ii</sup> —Tb1—O8	73.05 (6)	O5—P2—O6	117.25 (10)
O3 <sup>ii</sup> —Tb1—O9	146.04 (7)	O5—P2—O7	108.46 (10)
O3 <sup>ii</sup> —Tb1—O10	86.44 (8)	O6—P2—O7	105.28 (10)
O5—Tb1—O6 <sup>iii</sup>	143.13 (6)	H81—O8—H82	109 (3)
O5—Tb1—O8	72.85 (6)	H91—O9—H92	104 (3)
O5—Tb1—O9	70.39 (6)	H101—O10—H102	106 (3)
O5—Tb1—O10	112.90 (7)	H111—O11—H112	109 (3)

Symmetry codes: (i)  $x+1, y, z$ ; (ii)  $-x+1, -y+1, -z+2$ ; (iii)  $-x+3/2, y-1/2, -z+3/2$ .

#### Hydrogen-bond geometry ( $\text{\AA}$ , °)

$D\text{—H}\cdots A$	$D\text{—H}$	$\text{H}\cdots A$	$D\cdots A$	$D\text{—H}\cdots A$
O4—H41···O11	0.813 (13)	1.736 (14)	2.546 (3)	174 (3)
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O9—H91···O4 <sup>iv</sup>	0.83 (3)	2.06 (3)	2.851 (3)	161 (3)
O9—H92···O8 <sup>iii</sup>	0.828 (18)	1.95 (2)	2.750 (3)	164 (3)
O10—H101···O5 <sup>iii</sup>	0.82 (2)	2.16 (3)	2.880 (3)	147 (3)
O10—H102···O7 <sup>v</sup>	0.812 (16)	2.28 (2)	2.991 (3)	147 (3)
O11—H111···O3 <sup>v</sup>	0.80 (2)	2.18 (2)	2.941 (3)	157 (3)

Symmetry codes: (i)  $x+1, y, z$ ; (ii)  $-x+1, -y+1, -z+2$ ; (iii)  $-x+3/2, y-1/2, -z+3/2$ ; (iv)  $-x+1, -y+1, -z+1$ ; (v)  $-x+1/2, y-1/2, -z+3/2$ .