

## NASICON-type $\text{Na}_3\text{V}_2(\text{PO}_4)_3$

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Key indicators: single-crystal X-ray study;  $T = 293$  K; mean  $\sigma(\text{P}-\text{O}) = 0.001$  Å; disorder in solvent or counterion;  $R$  factor = 0.032;  $wR$  factor = 0.075; data-to-parameter ratio = 36.0.

Single crystals of the title compound, trisodium divanadium-(III) tris(orthophosphate), were grown from a self-flux in the system  $\text{Na}_4\text{P}_2\text{O}_7$ – $\text{NaVP}_2\text{O}_7$ .  $\text{Na}_3\text{V}_2(\text{PO}_4)_3$  belongs to the family of NASICON-related structures and is built up from isolated  $[\text{VO}_6]$  octahedra (3. symmetry) and  $[\text{PO}_4]$  tetrahedra (.2 symmetry) interlinked via corners to establish the framework anion  $[\text{V}_2(\text{PO}_4)_3]^{3-}$ . The two independent  $\text{Na}^+$  cations are partially occupied [site-occupancy factors = 0.805 (18) and 0.731 (7)] and are located in channels with two different oxygen environments, *viz* sixfold coordination for the first ( $\bar{3}$ . symmetry) and eightfold for the second (.2 symmetry)  $\text{Na}^+$  cation.

### Related literature

For structures and properties of complex phosphates with general formula  $\text{Na}_3M^{\text{III}}_2(\text{PO}_4)_3$  ( $M^{\text{III}} = \text{Sc}, \text{Fe}, \text{Cr}$ ), see: Collin *et al.* (1986); Genkina *et al.* (1991); Lazoryak *et al.* (1980); Lucaleau *et al.* (1986); Masquelier *et al.* (1992); Susman *et al.* (1983). For preparation of  $\text{NaVP}_2\text{O}_7$  which was used as an educt for crystal growth of the title compound, see: Zatovsky *et al.* (1999).

### Experimental

#### Crystal data

$\text{Na}_3\text{V}_2(\text{PO}_4)_3$	$Z = 6$
$M_r = 455.76$	Mo $K\alpha$ radiation
Trigonal, $R\bar{3}c$	$\mu = 2.66 \text{ mm}^{-1}$
$a = 8.7288 (2)$ Å	$T = 293$ K
$c = 21.8042 (7)$ Å	$0.20 \times 0.15 \times 0.10$ mm
$V = 1438.73 (7)$ Å <sup>3</sup>	

#### Data collection

Oxford Diffraction Xcalibur-3 CCD diffractometer	12580 measured reflections
Absorption correction: multi-scan (Blessing, 1995)	1331 independent reflections
$T_{\min} = 0.635$ , $T_{\max} = 0.780$	1153 reflections with $I > 2\sigma(I)$
	$R_{\text{int}} = 0.063$

#### Refinement

$R[F^2 > 2\sigma(F^2)] = 0.032$	37 parameters
$wR(F^2) = 0.075$	$\Delta\rho_{\text{max}} = 1.12 \text{ e } \text{\AA}^{-3}$
$S = 1.1$	$\Delta\rho_{\text{min}} = -0.74 \text{ e } \text{\AA}^{-3}$
1331 reflections	

**Table 1**  
Selected bond lengths (Å).

$\text{V1}-\text{O}2^{\text{i}}$	1.9693 (10)	$\text{Na2}-\text{O}2^{\text{iii}}$	2.6280 (16)
$\text{V1}-\text{O}1^{\text{ii}}$	2.0271 (9)	$\text{Na2}-\text{O}2^{\text{iv}}$	2.8352 (19)
$\text{Na1}-\text{O}1$	2.5045 (11)	$\text{P1}-\text{O}2^{\text{v}}$	1.5227 (12)
$\text{Na2}-\text{O}1^{\text{ii}}$	2.3883 (12)	$\text{P1}-\text{O}1$	1.5358 (10)
$\text{Na2}-\text{O}1^{\text{i}}$	2.4448 (19)		

Symmetry codes: (i)  $-y + 1, x - y + 1, z$ ; (ii)  $-x + y, -x + 1, z$ ; (iii)  $-x + \frac{4}{3}, -x + y + \frac{2}{3}, -z + \frac{1}{6}$ ; (iv)  $y + \frac{4}{3}, -x + \frac{5}{3}, z + \frac{1}{6}$ ; (v)  $x - \frac{2}{3}, x - y + \frac{2}{3}, z + \frac{1}{6}$ .

Data collection: *CrysAlis CCD* (Oxford Diffraction, 2006); cell refinement: *CrysAlis CCD*; data reduction: *CrysAlis RED* (Oxford Diffraction, 2006); program(s) used to solve structure: *SHELXS97* (Sheldrick, 2008); program(s) used to refine structure: *SHELXL97* (Sheldrick, 2008); molecular graphics: *DIAMOND* (Brandenburg, 1999); software used to prepare material for publication: *WinGX* (Farrugia, 1999) and *enCIFer* (Allen *et al.*, 2004).

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: WM2293).

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# supporting information

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## NASICON-type $\text{Na}_3\text{V}_2(\text{PO}_4)_3$

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### S1. Comment

The structures and properties of complex phosphates with general formula  $\text{Na}_3M^{\text{III}}_2(\text{PO}_4)_3$  ( $M^{\text{III}}$  - Sc, Fe, Cr) have been intensively investigated, for instance: (Collin *et al.*, 1986; Genkina *et al.*, 1991; Lazoryak *et al.*, 1980; Lucaleau *et al.*, 1986; Masquelier *et al.*, 1992; Susman *et al.*, 1983). The structure of NASICON-type  $\text{Na}_3\text{V}_2(\text{PO}_4)_3$ , (I), is reported here.

In the asymmetric unit of (I) (Fig. 1) there is one V and one P atom, while other atoms (Na and O) are represented in two distinct positions each. The main building block of (I) (Fig. 2) involves two  $\text{VO}_6$  octahedra interlinked by three phosphate groups lying along the  $c$  axis. As a result of the block aggregation, a three-dimensional framework with an overall composition of  $[\text{V}_2(\text{PO}_4)_3]^{3-}$  is organized (Fig. 3).

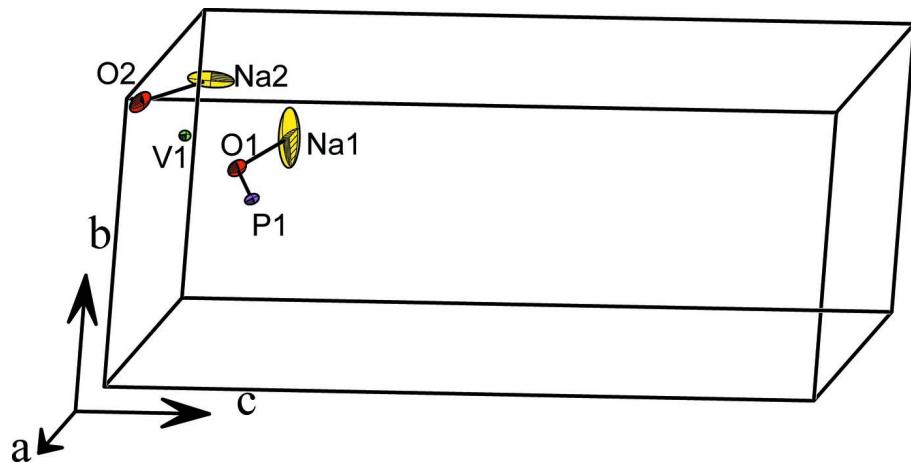
Sodium atoms are located in the voids of the framework with six- (position 6*b*) and eightfold (18*b*) coordination when a cut-off distance of 2.9 Å is considered.

### S2. Experimental

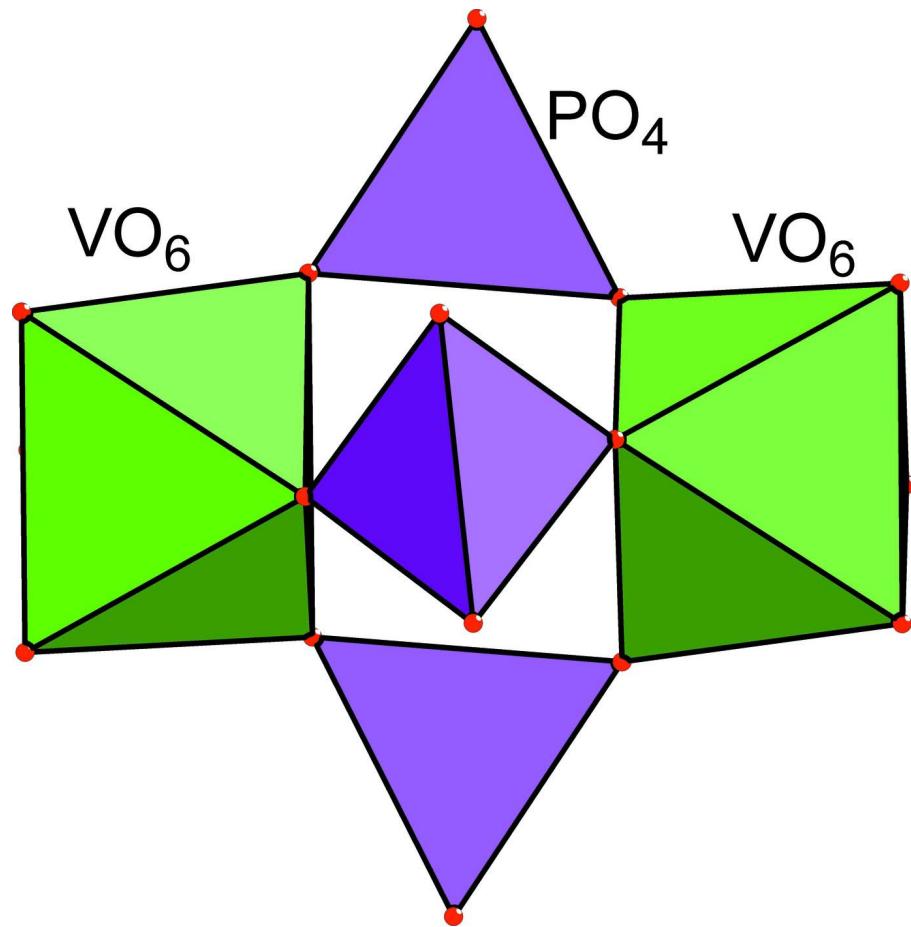
Crystals of (I) were obtained in the system  $\text{Na}_4\text{P}_2\text{O}_7$ — $\text{NaVP}_2\text{O}_7$  using a high-temperature crystallization technique. Initial  $\text{NaVP}_2\text{O}_7$  was prepared in accordance to Zatovsky *et al.* (1999). A thoroughly ground mixture of  $\text{Na}_4\text{P}_2\text{O}_7$  and  $\text{NaVP}_2\text{O}_7$  (ratio 1:3) was heated up to 1343 K and then kept for 2 h in a sealed silica tube under vacuum. Then it was cooled down to 823 K with a rate of 5 K/h and left in the furnace to reach room temperature. The final product, green prismatic crystals, was leached out from the solidified melt with boiling water.

### S3. Refinement

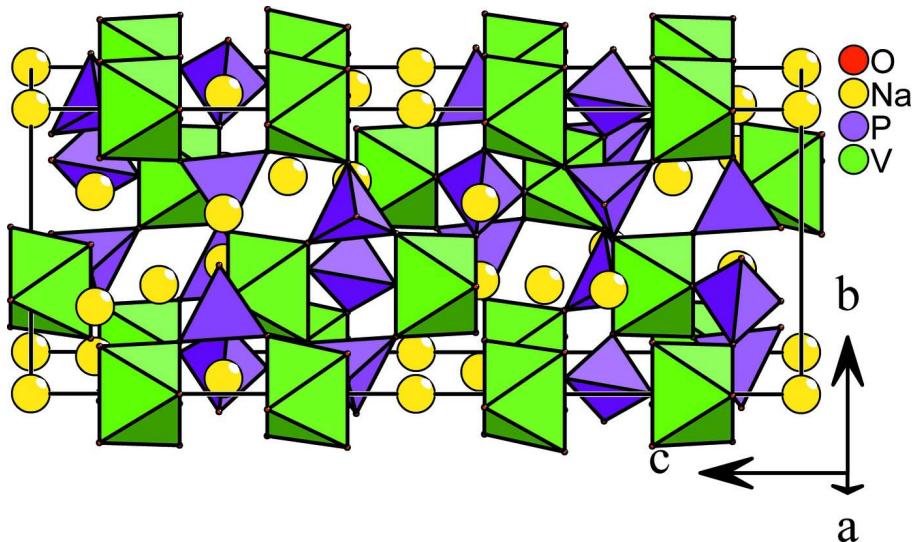
After refinement of a basic model and an accurate definition of the atom positions, the occupancy of Na1 and Na2 sites were refined freely and were finally restrained to meet the criterion for charge balance. The highest peak and the deepest hole in the final difference map is located at 0.00 Å from Na1 (1.12 e/Å<sup>3</sup>) and 0.60 from Na2 (-0.74 e/Å<sup>3</sup>) respectively.

**Figure 1**

The asymmetric unit of  $\text{Na}_3\text{V}_2(\text{PO}_4)_3$  with displacement ellipsoids at the 50% probability level.

**Figure 2**

The central building block  $[\text{V}_2(\text{PO}_4)_3]$  in the structure of compound (I).

**Figure 3**

The view of the structure of compound (I) on the *ab* plane.

#### trisodium divanadium(III) tris(orthophosphate)

##### Crystal data

$\text{Na}_3\text{V}_2(\text{PO}_4)_3$   
 $M_r = 455.76$   
Trigonal,  $R\bar{3}c$   
Hall symbol: -R 3 2 "c  
 $a = 8.7288 (2) \text{ \AA}$   
 $c = 21.8042 (7) \text{ \AA}$   
 $V = 1438.73 (7) \text{ \AA}^3$   
 $Z = 6$   
 $F(000) = 1320$

$D_x = 3.156 \text{ Mg m}^{-3}$   
Mo  $K\alpha$  radiation,  $\lambda = 0.71073 \text{ \AA}$   
Cell parameters from 12580 reflections  
 $\theta = 3.3\text{--}45.0^\circ$   
 $\mu = 2.66 \text{ mm}^{-1}$   
 $T = 293 \text{ K}$   
Prism, green  
 $0.20 \times 0.15 \times 0.10 \text{ mm}$

##### Data collection

Oxford Diffraction Xcalibur-3 CCD  
diffractometer  
Radiation source: fine-focus sealed tube  
Graphite monochromator  
 $\varphi$  and  $\omega$  scans  
Absorption correction: multi-scan  
(Blessing, 1995)  
 $T_{\min} = 0.635$ ,  $T_{\max} = 0.780$

12580 measured reflections  
1331 independent reflections  
1153 reflections with  $I > 2\sigma(I)$   
 $R_{\text{int}} = 0.063$   
 $\theta_{\max} = 45^\circ$ ,  $\theta_{\min} = 3.3^\circ$   
 $h = -17 \rightarrow 16$   
 $k = -17 \rightarrow 17$   
 $l = -43 \rightarrow 41$

##### Refinement

Refinement on  $F^2$   
Least-squares matrix: full  
 $R[F^2 > 2\sigma(F^2)] = 0.032$   
 $wR(F^2) = 0.075$   
 $S = 1.1$   
1331 reflections  
37 parameters  
0 restraints  
Primary atom site location: structure-invariant  
direct methods

Secondary atom site location: difference Fourier  
map  
 $w = 1/[\sigma^2(F_o^2) + (0.0264P)^2 + 5.1429P]$   
where  $P = (F_o^2 + 2F_c^2)/3$   
 $(\Delta/\sigma)_{\max} < 0.001$   
 $\Delta\rho_{\max} = 1.12 \text{ e \AA}^{-3}$   
 $\Delta\rho_{\min} = -0.74 \text{ e \AA}^{-3}$   
Extinction correction: *SHELXL97* (Sheldrick,  
2008)  
Extinction coefficient: 0.0056 (4)

*Special details*

**Geometry.** All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

**Refinement.** Refinement of  $F^2$  against ALL reflections. The weighted  $R$ -factor  $wR$  and goodness of fit  $S$  are based on  $F^2$ , conventional  $R$ -factors  $R$  are based on  $F$ , with  $F$  set to zero for negative  $F^2$ . The threshold expression of  $F^2 > \sigma(F^2)$  is used only for calculating  $R$ -factors(gt) etc. and is not relevant to the choice of reflections for refinement.  $R$ -factors based on  $F^2$  are statistically about twice as large as those based on  $F$ , and  $R$ -factors based on ALL data will be even larger.

*Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters ( $\text{\AA}^2$ )*

	<i>x</i>	<i>y</i>	<i>z</i>	$U_{\text{iso}}^*$ / $U_{\text{eq}}$	Occ. (<1)
V1	0.3333	0.6667	0.019498 (13)	0.00690 (6)	
Na1	0.3333	0.6667	0.1667	0.149 (5)	0.805 (18)
Na2	0.6667	0.96726 (19)	0.0833	0.0522 (10)	0.731 (7)
P1	-0.04273 (5)	0.3333	0.0833	0.00866 (8)	
O1	0.14193 (13)	0.49765 (14)	0.07762 (5)	0.01643 (16)	
O2	0.54047 (16)	0.84480 (17)	-0.02643 (7)	0.0259 (2)	

*Atomic displacement parameters ( $\text{\AA}^2$ )*

	$U^{11}$	$U^{22}$	$U^{33}$	$U^{12}$	$U^{13}$	$U^{23}$
V1	0.00643 (7)	0.00643 (7)	0.00784 (10)	0.00321 (4)	0	0
Na1	0.218 (8)	0.218 (8)	0.0111 (14)	0.109 (4)	0	0
Na2	0.0224 (8)	0.0170 (5)	0.119 (2)	0.0112 (4)	-0.0354 (11)	-0.0177 (5)
P1	0.00635 (10)	0.00714 (14)	0.01276 (15)	0.00357 (7)	0.00152 (5)	0.00305 (11)
O1	0.0089 (3)	0.0130 (3)	0.0220 (4)	0.0015 (3)	0.0048 (3)	0.0057 (3)
O2	0.0185 (4)	0.0223 (5)	0.0322 (6)	0.0067 (4)	0.0143 (4)	0.0151 (4)

*Geometric parameters ( $\text{\AA}$ ,  $\text{^\circ}$ )*

V1—O2 <sup>i</sup>	1.9693 (10)	Na2—O1 <sup>ii</sup>	2.3883 (12)
V1—O2	1.9693 (11)	Na2—O1 <sup>vi</sup>	2.3883 (12)
V1—O2 <sup>ii</sup>	1.9693 (10)	Na2—O1 <sup>i</sup>	2.4448 (19)
V1—O1 <sup>ii</sup>	2.0271 (9)	Na2—O1 <sup>vii</sup>	2.4449 (19)
V1—O1	2.0271 (9)	Na2—O2 <sup>viii</sup>	2.6280 (16)
V1—O1 <sup>i</sup>	2.0271 (9)	Na2—O2	2.6281 (16)
V1—Na2 <sup>i</sup>	3.1070 (6)	Na2—O2 <sup>ix</sup>	2.8352 (19)
V1—Na2	3.1070 (7)	Na2—O2 <sup>x</sup>	2.8352 (19)
V1—Na2 <sup>ii</sup>	3.1070 (6)	Na2—P1 <sup>xi</sup>	2.9222 (11)
V1—Na1	3.2096 (3)	Na2—P1 <sup>ii</sup>	2.9222 (11)
Na1—O1	2.5045 (11)	Na2—P1 <sup>i</sup>	2.9968 (17)
Na1—O1 <sup>ii</sup>	2.5045 (11)	P1—O2 <sup>xii</sup>	1.5227 (12)
Na1—O1 <sup>i</sup>	2.5045 (11)	P1—O2 <sup>xiii</sup>	1.5227 (12)
Na1—O1 <sup>iii</sup>	2.5045 (11)	P1—O1	1.5358 (10)
Na1—O1 <sup>iv</sup>	2.5045 (11)	P1—O1 <sup>xiv</sup>	1.5359 (10)
Na1—O1 <sup>v</sup>	2.5046 (11)	P1—Na2 <sup>xv</sup>	2.9222 (11)
Na1—V1 <sup>iv</sup>	3.2081 (2)	P1—Na2 <sup>i</sup>	2.9222 (11)

Na1—Na2 <sup>i</sup>	3.3193 (6)	P1—Na2 <sup>ii</sup>	2.9968 (17)
Na1—Na2 <sup>v</sup>	3.3193 (6)	O1—Na2 <sup>i</sup>	2.3883 (12)
Na1—Na2	3.3193 (6)	O1—Na2 <sup>ii</sup>	2.4448 (19)
Na1—Na2 <sup>ii</sup>	3.3205 (6)		
O2 <sup>i</sup> —V1—O2	96.44 (6)	O1 <sup>ii</sup> —Na2—O2	68.20 (4)
O2 <sup>i</sup> —V1—O2 <sup>ii</sup>	96.44 (6)	O1 <sup>vi</sup> —Na2—O2	115.98 (4)
O2—V1—O2 <sup>ii</sup>	96.44 (6)	O1 <sup>i</sup> —Na2—O2	66.40 (4)
O2 <sup>i</sup> —V1—O1 <sup>ii</sup>	88.22 (5)	O1 <sup>vii</sup> —Na2—O2	93.51 (6)
O2—V1—O1 <sup>ii</sup>	89.72 (5)	O2 <sup>viii</sup> —Na2—O2	157.25 (9)
O2 <sup>ii</sup> —V1—O1 <sup>ii</sup>	171.80 (6)	O1 <sup>ii</sup> —Na2—O2 <sup>ix</sup>	54.99 (4)
O2 <sup>i</sup> —V1—O1	89.72 (5)	O1 <sup>vi</sup> —Na2—O2 <sup>ix</sup>	108.39 (6)
O2—V1—O1	171.80 (6)	O1 <sup>i</sup> —Na2—O2 <sup>ix</sup>	115.94 (4)
O2 <sup>ii</sup> —V1—O1	88.22 (5)	O1 <sup>vii</sup> —Na2—O2 <sup>ix</sup>	151.11 (4)
O1 <sup>ii</sup> —V1—O1	85.05 (5)	O2 <sup>viii</sup> —Na2—O2 <sup>ix</sup>	85.67 (3)
O2 <sup>i</sup> —V1—O1 <sup>i</sup>	171.80 (6)	O2—Na2—O2 <sup>ix</sup>	112.13 (5)
O2—V1—O1 <sup>i</sup>	88.22 (5)	O1 <sup>ii</sup> —Na2—O2 <sup>x</sup>	108.39 (6)
O2 <sup>ii</sup> —V1—O1 <sup>i</sup>	89.72 (5)	O1 <sup>vi</sup> —Na2—O2 <sup>x</sup>	54.99 (4)
O1 <sup>ii</sup> —V1—O1 <sup>i</sup>	85.05 (5)	O1 <sup>i</sup> —Na2—O2 <sup>x</sup>	151.10 (4)
O1—V1—O1 <sup>i</sup>	85.05 (5)	O1 <sup>vii</sup> —Na2—O2 <sup>x</sup>	115.94 (4)
O1—Na1—O1 <sup>ii</sup>	66.33 (3)	O2 <sup>viii</sup> —Na2—O2 <sup>x</sup>	112.13 (5)
O1—Na1—O1 <sup>i</sup>	66.33 (3)	O2—Na2—O2 <sup>x</sup>	85.67 (3)
O1 <sup>ii</sup> —Na1—O1 <sup>i</sup>	66.33 (3)	O2 <sup>ix</sup> —Na2—O2 <sup>x</sup>	80.45 (7)
O1—Na1—O1 <sup>iii</sup>	113.67 (3)	O2 <sup>xii</sup> —P1—O2 <sup>xiii</sup>	111.67 (12)
O1 <sup>ii</sup> —Na1—O1 <sup>iii</sup>	180	O2 <sup>xii</sup> —P1—O1	106.07 (7)
O1 <sup>i</sup> —Na1—O1 <sup>iii</sup>	113.67 (3)	O2 <sup>xiii</sup> —P1—O1	112.18 (7)
O1—Na1—O1 <sup>iv</sup>	180	O2 <sup>xii</sup> —P1—O1 <sup>xiv</sup>	112.19 (7)
O1 <sup>ii</sup> —Na1—O1 <sup>iv</sup>	113.67 (3)	O2 <sup>xiii</sup> —P1—O1 <sup>xiv</sup>	106.07 (7)
O1 <sup>i</sup> —Na1—O1 <sup>iv</sup>	113.67 (3)	O1—P1—O1 <sup>xiv</sup>	108.74 (9)
O1 <sup>iii</sup> —Na1—O1 <sup>iv</sup>	66.33 (3)	P1—O1—V1	145.95 (7)
O1—Na1—O1 <sup>v</sup>	113.67 (3)	P1—O1—Na2 <sup>i</sup>	93.73 (6)
O1 <sup>ii</sup> —Na1—O1 <sup>v</sup>	113.67 (3)	V1—O1—Na2 <sup>i</sup>	89.05 (5)
O1 <sup>i</sup> —Na1—O1 <sup>v</sup>	180	P1—O1—Na2 <sup>ii</sup>	94.93 (5)
O1 <sup>iii</sup> —Na1—O1 <sup>v</sup>	66.33 (3)	V1—O1—Na2 <sup>ii</sup>	87.50 (4)
O1 <sup>iv</sup> —Na1—O1 <sup>v</sup>	66.33 (3)	Na2 <sup>i</sup> —O1—Na2 <sup>ii</sup>	169.09 (5)
O1 <sup>ii</sup> —Na2—O1 <sup>vi</sup>	160.52 (9)	P1—O1—Na1	124.53 (6)
O1 <sup>ii</sup> —Na2—O1 <sup>i</sup>	69.07 (5)	V1—O1—Na1	89.52 (4)
O1 <sup>vi</sup> —Na2—O1 <sup>i</sup>	130.40 (6)	Na2 <sup>i</sup> —O1—Na1	85.40 (5)
O1 <sup>ii</sup> —Na2—O1 <sup>vii</sup>	130.40 (6)	Na2 <sup>ii</sup> —O1—Na1	84.23 (4)
O1 <sup>vi</sup> —Na2—O1 <sup>vii</sup>	69.07 (5)	P1 <sup>xvi</sup> —O2—V1	151.38 (10)
O1 <sup>i</sup> —Na2—O1 <sup>vii</sup>	61.41 (6)	P1 <sup>xvi</sup> —O2—Na2	120.77 (8)
O1 <sup>ii</sup> —Na2—O2 <sup>viii</sup>	115.98 (4)	V1—O2—Na2	83.72 (5)
O1 <sup>vi</sup> —Na2—O2 <sup>viii</sup>	68.20 (4)	P1 <sup>xvi</sup> —O2—Na2 <sup>xvii</sup>	77.85 (5)
O1 <sup>i</sup> —Na2—O2 <sup>viii</sup>	93.51 (6)	V1—O2—Na2 <sup>xvii</sup>	107.30 (6)
O1 <sup>vii</sup> —Na2—O2 <sup>viii</sup>	66.40 (4)	Na2—O2—Na2 <sup>xvii</sup>	113.64 (7)

Symmetry codes: (i)  $-y+1, x-y+1, z$ ; (ii)  $-x+y, -x+1, z$ ; (iii)  $x-y+2/3, x+1/3, -z+1/3$ ; (iv)  $-x+2/3, -y+4/3, -z+1/3$ ; (v)  $y-1/3, -x+y+1/3, -z+1/3$ ; (vi)  $x-y+4/3, -y+5/3, -z+1/6$ ; (vii)  $y+1/3, x+2/3, -z+1/6$ ; (viii)  $-x+4/3, -x+y+2/3, -z+1/6$ ; (ix)  $-y+4/3, -x+5/3, z+1/6$ ; (x)  $y, -x+y+1, -z$ ; (xi)  $x+1, y+1, z$ ; (xii)  $x-2/3, x-y+2/3, z+1/6$ ; (xiii)  $y-1, -x+y, -z$ ; (xiv)  $x-y+1/3, -y+2/3, -z+1/6$ ; (xv)  $x-1, y-1, z$ ; (xvi)  $x-y+1, x+1, -z$ ; (xvii)  $x-y+1, x, -z$ .