

## Poly[hexaaqua( $\mu_9$ -cyclohexane-1,2,3,4,5,6-hexacarboxylato)-trimanganese(II)]

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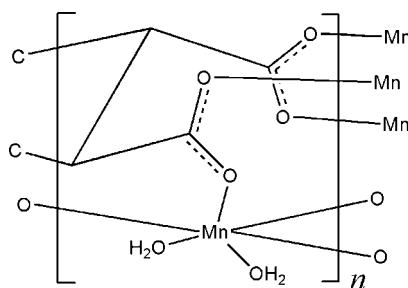
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Key indicators: single-crystal X-ray study;  $T = 185\text{ K}$ ; mean  $\sigma(\text{C}-\text{C}) = 0.004\text{ \AA}$ ;  $R$  factor = 0.025;  $wR$  factor = 0.064; data-to-parameter ratio = 10.7.

The asymmetric unit of the title compound,  $[\text{Mn}_3(\text{C}_{12}\text{H}_6\text{O}_{12})(\text{H}_2\text{O})_6]_n$ , comprises one  $\text{Mn}^{\text{II}}$  ion, one third of a cyclohexane-1,2,3,4,5,6-hexacarboxylate anion and two aqua ligands. The anion is completed by application of a  $\bar{3}$  axis. The  $\text{Mn}^{\text{II}}$  ion is six-coordinated by six O atoms from two aqua ligands and three different cyclohexacarboxylate anions in an octahedral geometry. The six carboxylate groups adopt a bridging bidentate mode to ligate the  $\text{Mn}^{\text{II}}$  ions. Thus, each cyclohexane-1,2,3,4,5,6-hexacarboxylate anion adopts a  $\mu_9$ -connected mode, ligating nine different  $\text{Mn}^{\text{II}}$  ions and forming a three-dimensional framework. In the framework, there are strong  $\text{O}-\text{H}\cdots\text{O}$  hydrogen-bonding interactions, which further stabilize the crystal structure.

### Related literature

For background to compounds with metal-organic framework structures, see: Wang *et al.* (2010); Bourne *et al.* (2001). For their properties, uses and topologies, see: O'Keeffe *et al.* (2000); Song *et al.* (2012).



### Experimental

#### Crystal data

$[\text{Mn}_3(\text{C}_{12}\text{H}_6\text{O}_{12})(\text{H}_2\text{O})_6]$   
 $M_r = 615.09$   
Trigonal,  $R\bar{3}$   
 $a = 14.5432 (4)\text{ \AA}$   
 $c = 14.9445 (10)\text{ \AA}$   
 $V = 2737.4 (2)\text{ \AA}^3$

$Z = 6$   
Mo  $K\alpha$  radiation  
 $\mu = 2.15\text{ mm}^{-1}$   
 $T = 185\text{ K}$   
 $0.25 \times 0.18 \times 0.16\text{ mm}$

#### Data collection

Bruker APEXII CCD diffractometer  
Absorption correction: multi-scan (*SADABS*; Bruker, 2001)  
 $R_{\text{int}} = 0.025$   
 $T_{\text{min}} = 0.616$ ,  $T_{\text{max}} = 0.725$

5063 measured reflections  
1200 independent reflections  
1098 reflections with  $I > 2\sigma(I)$   
 $R_{\text{int}} = 0.025$

#### Refinement

$R[F^2 > 2\sigma(F^2)] = 0.025$   
 $wR(F^2) = 0.064$   
 $S = 1.08$   
1200 reflections  
112 parameters  
4 restraints

H atoms treated by a mixture of independent and constrained refinement  
 $\Delta\rho_{\text{max}} = 0.75\text{ e \AA}^{-3}$   
 $\Delta\rho_{\text{min}} = -0.28\text{ e \AA}^{-3}$

**Table 1**  
Hydrogen-bond geometry ( $\text{\AA}$ ,  $^\circ$ ).

$D-\text{H}\cdots A$	$D-\text{H}$	$\text{H}\cdots A$	$D\cdots A$	$D-\text{H}\cdots A$
$\text{O}2\text{W}-\text{H}2\text{A}\cdots\text{O}2\text{W}^{\text{i}}$	0.81 (2)	2.31 (2)	3.116 (2)	178 (3)
$\text{O}2\text{W}-\text{H}2\text{A}\cdots\text{O}3^{\text{ii}}$	0.81 (2)	2.56 (3)	2.955 (2)	111 (2)
$\text{O}1\text{W}-\text{H}1\text{B}\cdots\text{O}4^{\text{iii}}$	0.87 (2)	1.92 (2)	2.774 (3)	169 (3)
$\text{O}1\text{W}-\text{H}1\text{B}\cdots\text{O}3^{\text{iii}}$	0.87 (2)	2.52 (3)	2.942 (3)	111 (2)
$\text{O}2\text{W}-\text{H}2\text{B}\cdots\text{O}1^{\text{ii}}$	0.84 (2)	2.06 (2)	2.883 (3)	169 (3)
$\text{O}1\text{W}-\text{H}1\text{A}\cdots\text{O}1\text{W}^{\text{iv}}$	0.84 (2)	2.01 (2)	2.8513 (18)	175 (3)

Symmetry codes: (i)  $x - y + 1, x, -z + 1$ ; (ii)  $-y + \frac{4}{3}, x - y + \frac{2}{3}, z - \frac{1}{3}$ ; (iii)  $x - y + \frac{2}{3}, x + \frac{1}{3}, -z + \frac{3}{3}$ ; (iv)  $y - \frac{1}{3}, -x + y + \frac{1}{3}, -z + \frac{4}{3}$ .

Data collection: *APEX2* (Bruker, 2007); cell refinement: *SAINT* (Bruker, 2007); data reduction: *SAINT*; program(s) used to solve structure: *SHELXTL* (Sheldrick, 2008); program(s) used to refine structure: *SHELXTL*; molecular graphics: *XP* in *SHELXTL* and *DIAMOND* (Brandenburg, 1999); software used to prepare material for publication: *SHELXTL*.

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: BX2441).

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# supporting information

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## Poly[hexaaqua( $\mu_9$ -cyclohexane-1,2,3,4,5,6-hexacarboxylato)trimanganese(II)]

Weixuan Sun, Hu Zang and Chengshi Quan

### S1. Comment

Metal-organic frameworks (MOFs) are an emerging class of periodic crystalline solid-state materials constructed from metal ions or polynuclear metal-oxygen clusters and multidentate organic ligands (Wang *et al.* 2010; Bourne *et al.* 2001). The potential applications in the realm of catalysis, gas separation, luminescence, as well as their intriguing nature of molecular architectures and topologies make so many chemists devote themselves to this active area (O'Keeffe *et al.* 2000; Song *et al.* 2012). The nature of the organic ligand has thus played an important role in designing special metal-organic frameworks. Herein, bicyclo[2.2.2]oct-7-ene-2,3,5,6-tetracarboxylic dianhydride was oxidized and hydrolyzed to give cyclohexacarboxylate anion *in situ*, which exhibits strong coordination ability to ligate the metal atoms.

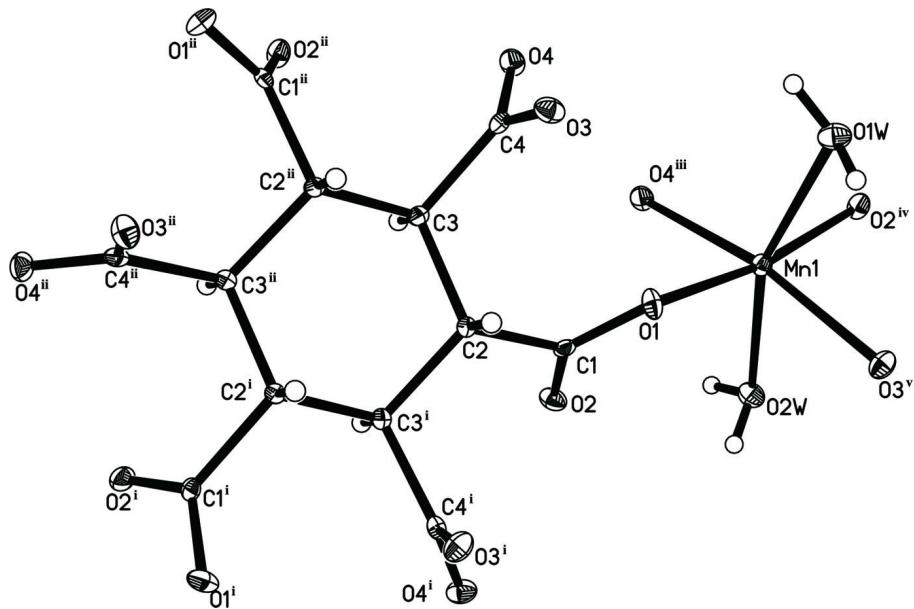
In this paper, we describe synthesis and the crystal structure of novel three-dimensional Mn<sup>II</sup>-organic compound bearing the ligand 1,2,3,4,5,6-cyclohexacarboxylic acid. X-ray diffraction analysis reveals that the title compound crystallizes in the space group *R*-3. The asymmetric unit contains one crystallographically unique manganese(II) ion, one third cyclohexacarboxylate anion and two aqua ligands (Fig. 1). The central Mn<sup>II</sup> ion exhibits the octahedral coordination geometry by six oxygen atoms from aqua ligands and different cyclohexacarboxylate anions. The whole framework composed of Mn ions and cyclohexacarboxylate anions is further stabilized by abundant and strong hydrogen bonding interactions (Fig. 2). The hydrogen bonding parameters are listed in Table 1.

### S2. Experimental

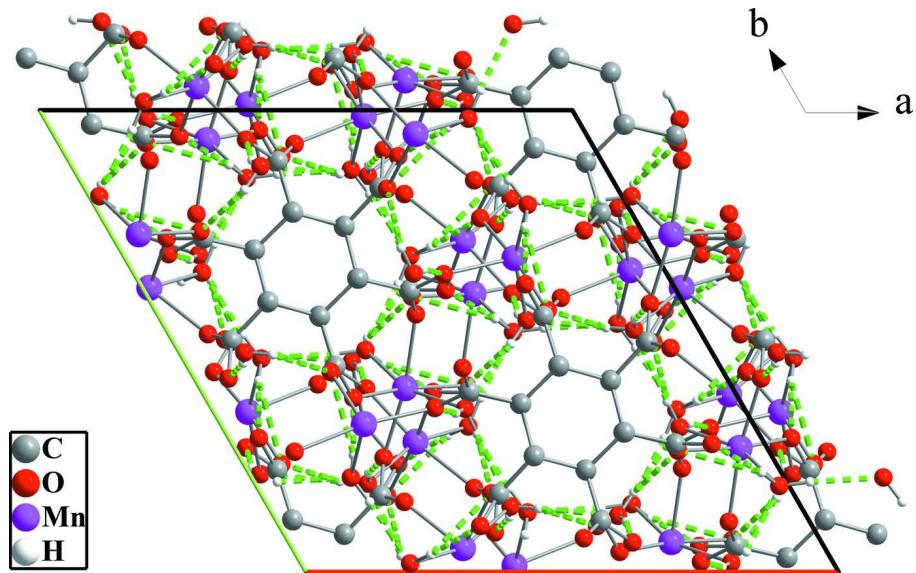
A mixture of bicyclo[2.2.2]oct-7-ene-2,3,5,6-tetracarboxylic dianhydride (0.1 mmol, 0.025 g), manganese chloride tetrahydrate (0.1 mmol, 0.02 g) were mixed with deionized water (6 ml) in a 15 ml Teflon-lined reactor, and heated at constant 433 K for 3 d. Then, the mixture was cooled to room temperature at a rate of 5 K h<sup>-1</sup>. Finally, needle-like crystals were obtained in 27% yield based on MnCl<sub>2</sub>.

### S3. Refinement

All the hydrogen atoms attached to carbon atoms were placed in calculated positions and refined as the riding model, and the water hydrogen atoms were located from the difference maps.

**Figure 1**

A view of the molecule of (I). Displacement ellipsoids are drawn at the 30% probability level. ( $i = 1 - x + y, 1 - x, z$ ;  $ii = 1 - x, x - y, z$ ;  $iii = 1 - x, 1 - y, 1 - z$ ;  $iv = y, 1 - x + y, 1 - z$ ;  $v = 2/3 + x - y, 1/3 + x, 4/3 - z$ )

**Figure 2**

A view along the  $c$  axis of the crystal packing of the title compound, hydrogen bonding interactions (dashed lines) in the whole three-dimensional framework.

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#### Crystal data

$[\text{Mn}_3(\text{C}_{12}\text{H}_6\text{O}_{12})(\text{H}_2\text{O})_6]$

$M_r = 615.09$

Trigonal,  $R\bar{3}$

Hall symbol:  $-R\bar{3}$

$a = 14.5432 (4)$  Å

$c = 14.9445 (10)$  Å

$V = 2737.4(2) \text{ \AA}^3$   
 $Z = 6$   
 $F(000) = 1854$   
 $D_x = 2.239 \text{ Mg m}^{-3}$   
Mo  $K\alpha$  radiation,  $\lambda = 0.71073 \text{ \AA}$   
Cell parameters from 11080 reflections

$\theta = 1.0\text{--}25.0^\circ$   
 $\mu = 2.15 \text{ mm}^{-1}$   
 $T = 185 \text{ K}$   
Needle, colorless  
 $0.25 \times 0.18 \times 0.16 \text{ mm}$

#### Data collection

Bruker APEXII CCD  
diffractometer  
Radiation source: fine-focus sealed tube  
Graphite monochromator  
 $\varphi$  and  $\omega$  scans  
Absorption correction: multi-scan  
(SADABS; Bruker, 2001)  
 $T_{\min} = 0.616$ ,  $T_{\max} = 0.725$

5063 measured reflections  
1200 independent reflections  
1098 reflections with  $I > 2\sigma(I)$   
 $R_{\text{int}} = 0.025$   
 $\theta_{\max} = 26.1^\circ$ ,  $\theta_{\min} = 2.1^\circ$   
 $h = -17 \rightarrow 17$   
 $k = -11 \rightarrow 17$   
 $l = -18 \rightarrow 18$

#### Refinement

Refinement on  $F^2$   
Least-squares matrix: full  
 $R[F^2 > 2\sigma(F^2)] = 0.025$   
 $wR(F^2) = 0.064$   
 $S = 1.08$   
1200 reflections  
112 parameters  
4 restraints  
Primary atom site location: structure-invariant  
direct methods

Secondary atom site location: difference Fourier  
map  
Hydrogen site location: inferred from  
neighbouring sites  
H atoms treated by a mixture of independent  
and constrained refinement  
 $w = 1/[\sigma^2(F_o^2) + (0.0259P)^2 + 11.1009P]$   
where  $P = (F_o^2 + 2F_c^2)/3$   
 $(\Delta/\sigma)_{\max} = 0.001$   
 $\Delta\rho_{\max} = 0.75 \text{ e \AA}^{-3}$   
 $\Delta\rho_{\min} = -0.28 \text{ e \AA}^{-3}$

#### Special details

**Geometry.** All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

**Refinement.** Refinement of  $F^2$  against ALL reflections. The weighted  $R$ -factor  $wR$  and goodness of fit  $S$  are based on  $F^2$ , conventional  $R$ -factors  $R$  are based on  $F$ , with  $F$  set to zero for negative  $F^2$ . The threshold expression of  $F^2 > \sigma(F^2)$  is used only for calculating  $R$ -factors(gt) etc. and is not relevant to the choice of reflections for refinement.  $R$ -factors based on  $F^2$  are statistically about twice as large as those based on  $F$ , and  $R$ -factors based on ALL data will be even larger.

#### Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters ( $\text{\AA}^2$ )

	$x$	$y$	$z$	$U_{\text{iso}}^*/U_{\text{eq}}$
C1	0.72468 (17)	0.55633 (17)	0.56658 (15)	0.0119 (5)
C2	0.69763 (17)	0.44523 (17)	0.59739 (16)	0.0124 (5)
H2	0.6975	0.4445	0.6643	0.015*
C3	0.58420 (17)	0.36429 (17)	0.56474 (16)	0.0126 (5)
H3	0.5819	0.3650	0.4979	0.015*
C4	0.50129 (18)	0.38891 (17)	0.60281 (16)	0.0139 (5)
O1	0.68842 (14)	0.60269 (13)	0.61426 (11)	0.0181 (4)
O2	0.77520 (13)	0.59359 (13)	0.49548 (12)	0.0180 (4)
O1W	0.53786 (15)	0.68488 (15)	0.66743 (13)	0.0228 (4)
O3	0.50339 (13)	0.40393 (14)	0.68557 (11)	0.0190 (4)

O2W	0.78828 (15)	0.80851 (14)	0.46574 (12)	0.0211 (4)
O4	0.43295 (13)	0.38944 (13)	0.55035 (11)	0.0187 (4)
Mn1	0.65353 (3)	0.71812 (3)	0.55736 (2)	0.01313 (13)
H2A	0.8391 (18)	0.804 (2)	0.4826 (19)	0.020*
H1B	0.5862 (19)	0.704 (2)	0.7082 (16)	0.020*
H2B	0.775 (2)	0.786 (2)	0.4129 (13)	0.020*
H1A	0.4847 (18)	0.6230 (16)	0.6686 (19)	0.020*

Atomic displacement parameters ( $\text{\AA}^2$ )

	$U^{11}$	$U^{22}$	$U^{33}$	$U^{12}$	$U^{13}$	$U^{23}$
C1	0.0076 (10)	0.0110 (11)	0.0147 (12)	0.0029 (9)	-0.0035 (8)	-0.0014 (9)
C2	0.0108 (11)	0.0094 (11)	0.0169 (12)	0.0050 (9)	0.0007 (9)	-0.0006 (9)
C3	0.0100 (11)	0.0102 (11)	0.0165 (12)	0.0043 (9)	-0.0001 (9)	0.0003 (9)
C4	0.0119 (11)	0.0081 (10)	0.0186 (12)	0.0027 (9)	0.0013 (9)	0.0002 (9)
O1	0.0263 (9)	0.0155 (8)	0.0179 (9)	0.0145 (8)	0.0027 (7)	0.0008 (7)
O2	0.0161 (8)	0.0203 (9)	0.0201 (9)	0.0108 (7)	0.0054 (7)	0.0064 (7)
O1W	0.0189 (9)	0.0241 (10)	0.0229 (10)	0.0089 (8)	0.0011 (8)	0.0057 (8)
O3	0.0166 (8)	0.0255 (9)	0.0154 (9)	0.0109 (8)	0.0008 (7)	-0.0015 (7)
O2W	0.0208 (9)	0.0246 (10)	0.0196 (10)	0.0126 (8)	0.0038 (8)	0.0016 (8)
O4	0.0179 (9)	0.0217 (9)	0.0198 (9)	0.0125 (7)	-0.0066 (7)	-0.0052 (7)
Mn1	0.0142 (2)	0.0124 (2)	0.0134 (2)	0.00709 (15)	-0.00102 (13)	0.00031 (13)

Geometric parameters ( $\text{\AA}$ ,  $^\circ$ )

C1—O2	1.251 (3)	O2—Mn1 <sup>iii</sup>	2.1866 (17)
C1—O1	1.263 (3)	O1W—Mn1	2.2263 (19)
C1—C2	1.530 (3)	O1W—H1B	0.866 (17)
C2—C3 <sup>i</sup>	1.540 (3)	O1W—H1A	0.843 (17)
C2—C3	1.550 (3)	O3—Mn1 <sup>iv</sup>	2.1581 (17)
C2—H2	1.0000	O2W—Mn1	2.2062 (18)
C3—C4	1.529 (3)	O2W—H2A	0.811 (17)
C3—C2 <sup>ii</sup>	1.540 (3)	O2W—H2B	0.838 (17)
C3—H3	1.0000	O4—Mn1 <sup>v</sup>	2.1569 (17)
C4—O3	1.254 (3)	Mn1—O4 <sup>v</sup>	2.1569 (17)
C4—O4	1.269 (3)	Mn1—O3 <sup>vi</sup>	2.1581 (17)
O1—Mn1	2.1565 (16)	Mn1—O2 <sup>vii</sup>	2.1866 (17)
O2—C1—O1	124.0 (2)	H1B—O1W—H1A	119 (3)
O2—C1—C2	119.9 (2)	C4—O3—Mn1 <sup>iv</sup>	131.39 (15)
O1—C1—C2	116.0 (2)	Mn1—O2W—H2A	110 (2)
C1—C2—C3 <sup>i</sup>	111.91 (18)	Mn1—O2W—H2B	113 (2)
C1—C2—C3	108.74 (18)	H2A—O2W—H2B	108 (3)
C3 <sup>i</sup> —C2—C3	111.7 (2)	C4—O4—Mn1 <sup>v</sup>	129.13 (15)
C1—C2—H2	108.1	O1—Mn1—O4 <sup>v</sup>	90.49 (6)
C3 <sup>i</sup> —C2—H2	108.1	O1—Mn1—O3 <sup>vi</sup>	89.74 (7)
C3—C2—H2	108.1	O4 <sup>v</sup> —Mn1—O3 <sup>vi</sup>	168.84 (7)
C4—C3—C2 <sup>ii</sup>	107.13 (18)	O1—Mn1—O2 <sup>vii</sup>	171.49 (7)

C4—C3—C2	111.68 (18)	O4 <sup>v</sup> —Mn1—O2 <sup>vii</sup>	86.09 (6)
C2 <sup>ii</sup> —C3—C2	109.3 (2)	O3 <sup>vi</sup> —Mn1—O2 <sup>vii</sup>	95.12 (6)
C4—C3—H3	109.6	O1—Mn1—O2W	102.94 (7)
C2 <sup>ii</sup> —C3—H3	109.6	O4 <sup>v</sup> —Mn1—O2W	89.49 (7)
C2—C3—H3	109.6	O3 <sup>vi</sup> —Mn1—O2W	79.59 (7)
O3—C4—O4	124.0 (2)	O2 <sup>vii</sup> —Mn1—O2W	84.84 (7)
O3—C4—C3	117.0 (2)	O1—Mn1—O1W	89.19 (7)
O4—C4—C3	118.9 (2)	O4 <sup>v</sup> —Mn1—O1W	106.90 (7)
C1—O1—Mn1	121.10 (15)	O3 <sup>vi</sup> —Mn1—O1W	84.26 (7)
C1—O2—Mn1 <sup>iii</sup>	139.24 (15)	O2 <sup>vii</sup> —Mn1—O1W	84.36 (7)
Mn1—O1W—H1B	92.6 (19)	O2W—Mn1—O1W	159.65 (7)
Mn1—O1W—H1A	116 (2)		
O2—C1—C2—C3 <sup>i</sup>	28.8 (3)	C2—C1—O1—Mn1	-151.73 (15)
O1—C1—C2—C3 <sup>i</sup>	-154.7 (2)	O1—C1—O2—Mn1 <sup>iii</sup>	113.2 (2)
O2—C1—C2—C3	-95.1 (2)	C2—C1—O2—Mn1 <sup>iii</sup>	-70.6 (3)
O1—C1—C2—C3	81.4 (2)	O4—C4—O3—Mn1 <sup>iv</sup>	16.8 (3)
C1—C2—C3—C4	-60.2 (2)	C3—C4—O3—Mn1 <sup>iv</sup>	-160.75 (15)
C3 <sup>i</sup> —C2—C3—C4	175.81 (16)	O3—C4—O4—Mn1 <sup>v</sup>	-136.2 (2)
C1—C2—C3—C2 <sup>ii</sup>	-178.55 (15)	C3—C4—O4—Mn1 <sup>v</sup>	41.3 (3)
C3 <sup>i</sup> —C2—C3—C2 <sup>ii</sup>	57.4 (3)	C1—O1—Mn1—O4 <sup>v</sup>	48.74 (18)
C2 <sup>ii</sup> —C3—C4—O3	69.9 (3)	C1—O1—Mn1—O3 <sup>vi</sup>	-120.11 (18)
C2—C3—C4—O3	-49.8 (3)	C1—O1—Mn1—O2 <sup>vii</sup>	115.0 (4)
C2 <sup>ii</sup> —C3—C4—O4	-107.7 (2)	C1—O1—Mn1—O2W	-40.85 (18)
C2—C3—C4—O4	132.6 (2)	C1—O1—Mn1—O1W	155.63 (18)
O2—C1—O1—Mn1	24.6 (3)		

Symmetry codes: (i)  $-x+y+1, -x+1, z$ ; (ii)  $-y+1, x-y, z$ ; (iii)  $x-y+1, x, -z+1$ ; (iv)  $y-1/3, -x+y+1/3, -z+4/3$ ; (v)  $-x+1, -y+1, -z+1$ ; (vi)  $x-y+2/3, x+1/3, -z+4/3$ ; (vii)  $y, -x+y+1, -z+1$ .

#### Hydrogen-bond geometry ( $\text{\AA}$ , $^\circ$ )

D—H $\cdots$ A	D—H	H $\cdots$ A	D $\cdots$ A	D—H $\cdots$ A
O2W—H2A $\cdots$ O2W <sup>iii</sup>	0.81 (2)	2.31 (2)	3.116 (2)	178 (3)
O2W—H2A $\cdots$ O3 <sup>viii</sup>	0.81 (2)	2.56 (3)	2.955 (2)	111 (2)
O1W—H1B $\cdots$ O4 <sup>vi</sup>	0.87 (2)	1.92 (2)	2.774 (3)	169 (3)
O1W—H1B $\cdots$ O3 <sup>vi</sup>	0.87 (2)	2.52 (3)	2.942 (3)	111 (2)
O2W—H2B $\cdots$ O1 <sup>viii</sup>	0.84 (2)	2.06 (2)	2.883 (3)	169 (3)
O1W—H1A $\cdots$ O1W <sup>iv</sup>	0.84 (2)	2.01 (2)	2.8513 (18)	175 (3)

Symmetry codes: (iii)  $x-y+1, x, -z+1$ ; (iv)  $y-1/3, -x+y+1/3, -z+4/3$ ; (vi)  $x-y+2/3, x+1/3, -z+4/3$ ; (viii)  $-y+4/3, x-y+2/3, z-1/3$ .