

Prince & Toby

Supplementary Material:  
Derivative of the peak shape function with respect to  $S$

The peak shape function  $F(2\theta, \mu, \sigma, {}^3\kappa, {}^4\kappa)$ , is defined by

$$F(2\theta, \mu, \sigma, {}^3\kappa, {}^4\kappa) = \frac{1}{\sqrt{2\pi}\sigma} \exp\left[-\frac{(2\theta - \mu)^2}{2\sigma^2}\right] \left[1 + \frac{{}^3\kappa}{6\sigma^3} H_3\left(\frac{2\theta - \mu}{\sigma}\right) + \frac{{}^4\kappa}{24\sigma^4} H_4\left(\frac{2\theta - \mu}{\sigma}\right)\right],$$

where

$$\begin{aligned} \mu &= 2\theta_B - 2\theta_0 + \delta_1, \\ \sigma &= \sqrt{U(\tan \theta_B - \tan \theta_m)^2 + V(\tan \theta_B - \tan \theta_m) + W + \delta_2 - \delta_1^2}, \\ {}^3\kappa &= \delta_3 - 3\delta_1\delta_2 + 2\delta_1^3, \\ {}^4\kappa &= \delta_4 - 4\delta_1\delta_3 - 3\delta_2^2 + 12\delta_2\delta_1^2 - 6\delta_1^4. \end{aligned}$$

Here  $H_3$  and  $H_4$  are the third and fourth degree Hermite polynomials,

$$\begin{aligned} H_3(x) &= x^3 - 3x, \\ H_4(x) &= x^4 - 6x^2 + 3. \end{aligned}$$

$\theta_m$  is an arbitrary offset that should be chosen close to the minimum of the resolution curve to minimize the correlations among  $U$ ,  $V$ , and  $W$ .

Although the Finger, Cox & Jephcoat model for the peak shape function, and the Edgeworth series approximation to it, appears to have no adjustable parameters, it implicitly assumes that the incident beam has no axial divergence. This can be approximately accounted for by an ‘effective’ sample height,  $2S$ . To make this a refinable parameter we need to evaluate the partial derivative of  $F$  with respect to  $S$ . First we need the partial derivatives of  $F$  with respect to its arguments,  $\mu$ ,  $\sigma$ ,  ${}^3\kappa$ , and  ${}^4\kappa$ . For convenience, let  $t = (2\theta - \mu)/\sigma$ ;  $\frac{\partial t}{\partial \mu} = -1/\sigma$ ;  $\frac{\partial t}{\partial \sigma} = (\mu - 2\theta)/\sigma^2$ . Then

$$\begin{aligned} \frac{\partial F}{\partial t} &= \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{t^2}{2}\right) \left[ -t \left(1 + \frac{{}^3\kappa}{6\sigma^3} H_3(t) + \frac{{}^4\kappa}{24\sigma^4} H_4(t)\right) \right. \\ &\quad \left. + \frac{{}^3\kappa}{6\sigma^3} H'_3(t) + \frac{{}^4\kappa}{24\sigma^4} H'_4(t) \right], \end{aligned}$$

where

$$\begin{aligned} H'_3(t) &= \frac{dH_3(t)}{dt} = 3t^2 - 3, \\ H'_4(t) &= \frac{dH_4(t)}{dt} = 4t^3 - 12t. \end{aligned}$$

The partial derivatives of  $F$  with respect to its arguments are then

$$\begin{aligned}\frac{\partial F}{\partial \mu} &= \frac{\partial F}{\partial t} \frac{\partial t}{\partial \mu}; \\ \frac{\partial F}{\partial \sigma} &= \frac{\partial F}{\partial t} \frac{\partial t}{\partial \sigma} - \frac{F}{\sigma} - \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{t^2}{2}\right) \left[ \frac{^3\kappa}{2\sigma^4} H_3(t) + \frac{^4\kappa}{6\sigma^5} H_4(t) \right]; \\ \frac{\partial F}{\partial ^3\kappa} &= \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{t^2}{2}\right) \left[ \frac{1}{6\sigma^3} H_3(t) \right]; \\ \frac{\partial F}{\partial ^4\kappa} &= \frac{1}{\sqrt{2\pi}\sigma} \exp\left(-\frac{t^2}{2}\right) \left[ \frac{1}{24\sigma^4} H_4(t) \right].\end{aligned}$$

The arguments of  $F$ ,  $\mu$ ,  $\sigma$ ,  $^3\kappa$ , and  $^4\kappa$ , are themselves functions of the moments,  $\delta_1$ ,  $\delta_2$ ,  $\delta_3$ , and  $\delta_4$ , of the function that modifies the peak shape due to the effects of the Debye-Scherrer ring. These partial derivatives are

$$\begin{aligned}\frac{\partial \mu}{\partial \delta_1} &= 1; \\ \frac{\partial \sigma}{\partial \delta_1} &= \frac{\delta_1}{\sigma}; \\ \frac{\partial \sigma}{\partial \delta_2} &= -\frac{1}{2\sigma}; \\ \frac{\partial ^3\kappa}{\partial \delta_1} &= -3\delta_2 + 6\delta_1^2; \\ \frac{\partial ^3\kappa}{\partial \delta_2} &= -3\delta_1; \\ \frac{\partial ^3\kappa}{\partial \delta_3} &= 1; \\ \frac{\partial ^4\kappa}{\partial \delta_1} &= -4\delta_3 + 24\delta_1\delta_2 - 24\delta_1^3; \\ \frac{\partial ^4\kappa}{\partial \delta_2} &= -6\delta_2 + 12\delta_1^2; \\ \frac{\partial ^4\kappa}{\partial \delta_3} &= -4\delta_1; \\ \frac{\partial ^4\kappa}{\partial \delta_4} &= 1.\end{aligned}$$

Finally

$$\begin{aligned}\frac{\partial F}{\partial \delta_1} &= \frac{\partial F}{\partial \mu} + \frac{\partial F}{\partial \sigma} \frac{\partial \sigma}{\partial \delta_1} + \frac{\partial F}{\partial^3 \kappa} \frac{\partial^3 \kappa}{\partial \delta_1} + \frac{\partial F}{\partial^4 \kappa} \frac{\partial^4 \kappa}{\partial \delta_1}; \\ \frac{\partial F}{\partial \delta_2} &= \frac{\partial F}{\partial \sigma} \frac{\partial \sigma}{\partial \delta_2} + \frac{\partial F}{\partial^3 \kappa} \frac{\partial^3 \kappa}{\partial \delta_2} + \frac{\partial F}{\partial^4 \kappa} \frac{\partial^4 \kappa}{\partial \delta_2}; \\ \frac{\partial F}{\partial \delta_3} &= \frac{\partial F}{\partial^3 \kappa} + \frac{\partial F}{\partial^4 \kappa} \frac{\partial^4 \kappa}{\partial \delta_3}; \\ \frac{\partial F}{\partial \delta_4} &= \frac{\partial F}{\partial^4 \kappa}.\end{aligned}$$

The partial derivatives of  $F$  with respect to the four moments,  $\delta_1$  to  $\delta_4$ , are all functions of  $2\theta$ , and therefore they must be evaluated for every data point. The derivatives of the moments with respect to  $S$ , however, depend only on  $S$  and  $2\theta_B$ , and they need to be evaluated only once per reflection. GSAS, in its implementation of the Finger-Cox-Jephcoat correction, uses the quantities  $s = S/R$  and  $h = H/R$ , where  $R$  is the distance from the sample to the detector slit. We shall derive the derivatives of the moments with respect to  $s$ . First, let  $\alpha = (h - s)^2$ , and  $\beta = (h + s)^2$ . Then  $\frac{d\alpha}{ds} = -2(h - s)$ , and  $\frac{d\beta}{ds} = 2(h + s)$ . In terms of  $\alpha$  and  $\beta$ ,

$$\begin{aligned}\delta_1 &= -\frac{\beta + \alpha}{12 \tan 2\theta_B}; \\ \frac{\partial \delta_1}{\partial \alpha} &= \frac{\partial \delta_1}{\partial \beta} = -\frac{1}{12 \tan 2\theta_B}; \\ \frac{d\delta_1}{ds} &= \frac{\partial \delta_1}{\partial \alpha} \frac{d\alpha}{ds} + \frac{\partial \delta_1}{\partial \beta} \frac{d\beta}{ds}.\end{aligned}$$

$$\begin{aligned}\delta_2 &= \frac{\beta^2 + \beta\alpha + \alpha^2}{60 \tan^2 2\theta_B}; \\ \frac{\partial \delta_2}{\partial \alpha} &= \frac{\beta + 2\alpha}{60 \tan^2 2\theta_B}; \\ \frac{\partial \delta_2}{\partial \beta} &= \frac{2\beta + \alpha}{60 \tan^2 2\theta_B}; \\ \frac{d\delta_2}{ds} &= \frac{\partial \delta_2}{\partial \alpha} \frac{d\alpha}{ds} + \frac{\partial \delta_2}{\partial \beta} \frac{d\beta}{ds}.\end{aligned}$$

$$\begin{aligned}\delta_3 &= -\frac{\beta^3 + \beta^2\alpha + \beta\alpha^2 + \alpha^3}{224 \tan^3 2\theta_B}; \\ \frac{\partial \delta_3}{\partial \alpha} &= -\frac{\beta^2 + 2\beta\alpha + 3\alpha^2}{224 \tan^3 2\theta_B}; \\ \frac{\partial \delta_3}{\partial \beta} &= -\frac{3\beta^2 + 2\beta\alpha + \alpha^2}{224 \tan^3 2\theta_B}; \\ \frac{d\delta_3}{ds} &= -\frac{\partial \delta_3}{\partial \alpha} \frac{d\alpha}{ds} + \frac{\partial \delta_3}{\partial \beta} \frac{d\beta}{ds}.\end{aligned}$$

$$\begin{aligned}
\delta_4 &= \frac{\beta^4 + \beta^3\alpha + \beta^2\alpha^2 + \beta\alpha^3 + \alpha^4}{720 \tan^4 2\theta_B}; \\
\frac{\partial \delta_4}{\partial \alpha} &= \frac{\beta^3 + 2\beta^2\alpha + 3\beta\alpha^2 + 4\alpha^3}{720 \tan^4 2\theta_B}; \\
\frac{\partial \delta_4}{\partial \beta} &= \frac{4\beta^3 + 3\beta^2\alpha + 2\beta\alpha^2 + \alpha^3}{720 \tan^4 2\theta_B}; \\
\frac{d\delta_4}{ds} &= \frac{\partial \delta_4}{\partial \alpha} \frac{d\alpha}{ds} + \frac{\partial \delta_4}{\partial \beta} \frac{d\beta}{ds}.
\end{aligned}$$

Then

$$\frac{\partial F}{\partial s} = \frac{\partial F}{\partial \delta_1} \frac{d\delta_1}{ds} + \frac{\partial F}{\partial \delta_2} \frac{d\delta_2}{ds} + \frac{\partial F}{\partial \delta_3} \frac{d\delta_3}{ds} + \frac{\partial F}{\partial \delta_4} \frac{d\delta_4}{ds}.$$

Also

$$\begin{aligned}
\frac{\partial F}{\partial U} &= \frac{\partial F}{\partial \sigma} \frac{(\tan \theta - \tan \theta_m)^2}{2\sigma}; \\
\frac{\partial F}{\partial V} &= \frac{\partial F}{\partial \sigma} \frac{\tan \theta - \tan \theta_m}{2\sigma}; \\
\frac{\partial F}{\partial W} &= \frac{\partial F}{\partial \sigma} \frac{1}{2\sigma}.
\end{aligned}$$

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C example Fortran code to accompany Prince & Toby, A Comparison of Methods for
C Modeling the Effect of Axial Divergence in Powder Diffraction
C
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```
PROGRAM PEAKS
CHARACTER*20 STRIN

DIMENSION VALUES(81,4)

NVALUES = 81
WRITE(*,*) 'Enter FWHM: '
READ(*,*) FWHM
WRITE(*,*) 'Enter Peak position: '
READ(*,*) TWOTH
XMIN=TWOTH-6.*FWHM
XMAX=TWOTH+2.*FWHM
WRITE(*,*) 'Enter H/R: '
READ(*,*) HOVERR
WRITE(*,*) 'Enter S/R: '
READ(*,*) SOVERR
NCURVE = 1
FACTR = 0.
CALL CALCPK(FWHM,TWOTH,0.0,0.0
1 ,FACTR,1,VALUES(1,NCURVE),NVALUES)
NCURVE = 2
CALL CALCPK(FWHM,TWOTH,HOVERR,SOVERR
1 ,FACTR,1,VALUES(1,NCURVE),NVALUES)
NCURVE = 3
CALL CALCPK(FWHM,TWOTH,HOVERR,SOVERR
1 ,FACTR,2,VALUES(1,NCURVE),NVALUES)
OPEN(UNIT=8,FORM='FORMATTED'
1 ,STATUS='UNKNOWN')
TWOTHETA=XMIN
WRITE(8,*) 'FWHM=' ,FWHM,' , TWOTHETA=' ,TWOTH,' , S/L=' ,SOVERR,
$ ' , H/L=' ,HOVERR
WRITE(8,'(4A10)') 'TWOTHETA','No Asym','Edgeworth','FCJ'

RINCR=(XMAX-XMIN)/(FLOAT(NVALUES)-1.)
DO I=1,NVALUES
  WRITE(8,9000)TWOTHETA,(VALUES(I,J),J=1,NCURVE)
9000 FORMAT(5F10.4)
  TWOTHETA=TWOTHETA+RINCR
ENDDO
CLOSE(UNIT=8)
STOP
END PROGRAM PEAKS

SUBROUTINE CALCPK(FWHM,TWOTH,HOVERR,SOVERR,FACTR,ISET,VALUES,N)
C CALCULATE AN ASYMMETRIC PEAK.
C ARGUMENTS ARE:
C FWHM = FULL WIDTH AT HALF MAXIMUM OF UNDISTORTED PEAK.
C TWOTH = 2 THETA, AS CALCULATED FROM CELL CONSTANTS.
C HOVERR = HALF HEIGHT OF RECEIVING SLIT DIVIDED BY DISTANCE FROM SAMPLE.
C VALUES = ARRAY TO STORE CURVE.
C N = NUMBER OF POINTS FROM TWOTH-6*FWHM TO TWOTH+2*FWHM.
DIMENSION VALUES(N),COEF(8),DPDF(6)
PIO180=ACOS(-1.)/180.
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SIGMA=FWHM*42.4661
COEF(1)=0.
COEF(2)=0.
COEF(3)=SIGMA**2
COEF(4)=0.
COEF(5)=SOVERR
COEF(6)=HOVERR
XLEN=8.*FWHM
XMIN=TWOTH-6.*FWHM
X=XMIN
ETA=0.
DO I=1,N
    IF(ISET.EQ.1)THEN
        CALL SIMGAUS(COEF,100.*TWOTH,100.*(X-TWOTH),TMP,DPDT
1           ,DPDF,0.)
        VALUES(I)=100.*TMP
    ELSE
        VALUES(I)=PROFVAL(ETA,FWHM,HOVERR,SOVERR,X
1           ,TWOTH,DUM1,DUM2,DUM3,DUM4,DUM5,.TRUE.)
    ENDIF
    X=XMIN+XLEN*FLOAT(I)/FLOAT(N-1)
ENDDO
RETURN
END SUBROUTINE CALCPK
SUBROUTINE SIMGAUS(COFF,TTHETA,DTTH,PRFUNC,DPRDT,DPRDCF,ZERO)

!PURPOSE: Compute function & derivatives for Edgeworth series model
! of axial divergence effects. Written by E. Prince, December, 2004.
! All calcs in centidegrees

!CALLING ARGUMENTS:

      REAL*4      COFF(1)          !Coefficients
      REAL*4      TTHETA           !2-theta in centideg
      REAL*4      DTTH              !Delta 2-theta
      REAL*4      PRFUNC             !Value of function at DTTH
      REAL*4      DPRDT              !partial df(t)/dt
      REAL*4      DPRDCF(1)         !partial df(t)/dc
      REAL*4      ZERO               !zero corrextion

```

!LOCAL VARIABLES:

REAL*4	TH	
REAL*4	ARGS(4)	!Asymmetry coefficients
REAL*4	DERVS(4)	!Derivatives wrt S/L
REAL*4	SIG	!Gaussian width
REAL*4	CUM3	!Third cumulant
REAL*4	CUM4	!Fourth cumulant
REAL*4	DFDT	
REAL*4	DTDMU	
REAL*4	DTDSIG	
REAL*4	DFDMU	
REAL*4	DFDSIG	
REAL*4	DFDCM3	
REAL*4	DFDCM4	
REAL*4	DELTA1	
REAL*4	DMUDS	

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REAL*4      DSIGDS
REAL*4      DCM3DS
REAL*4      DCM4DS
EQUIVALENCE (DELTAL,ARGS(1))
EQUIVALENCE (SIG,ARGS(2))
EQUIVALENCE (CUM3,ARGS(3))
EQUIVALENCE (CUM4,ARGS(4))
EQUIVALENCE (DMUDS,DERVS(1))
EQUIVALENCE (DSIGDS,DERVS(2))
EQUIVALENCE (DCM3DS,DERVS(3))
EQUIVALENCE (DCM4DS,DERVS(4))

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**!SUBROUTINES CALLED:**

! ASYMCDF

**!DATA STATEMENTS:**

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DATA PIO180/0.000174533/
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**!CODE:**

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TH = 0.5*PIO180*(TTHETA-ZERO)
TTH = TAN(TH)-COFF(4)
SIG = COFF(1)*TTH*TTH+COFF(2)*TTH+COFF(3)

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CALL ASYMCDF(TTHETA-ZERO,COFF(6),COFF(5),ARGS,DERVS)
IF ( SIG.LE.0.01) SIG = 0.01
SIG3=SIG*SIG*SIG
SIG4=SIG3*SIG
DSIGDW=0.5/SIG
TT = (DTTH-DELTAL)/SIG
DTDMU=-1./SIG
DTDSIG=-TT/SIG
EXPTT=EXP(-0.5*TT**2)
H3TT=TT**3-3.*TT
DH3TT=3.*TT**2-3.
H4TT=TT**4-6.*TT**2+3.
DH4TT=4.*TT**3-12.*TT
SCLNRM=1./(2.50663*SIG)
PRFUNC=SCLNRM*EXPTT*(1.+ CUM3*H3TT/(6.*SIG3)
1      + CUM4*H4TT/(24.*SIG4))
DFDT=SCLNRM*EXPTT*(-TT*(1.+ CUM3*H3TT/(6.*SIG3)
1      + CUM4*H4TT/(24.*SIG4))+ CUM3*DHTT/(6.*SIG3)
2      + CUM4*DHTT/(24.*SIG4))
DFDMU=DFDT*DTDMU
DFDSIG=DFDT*DTDSIG-PRFUNC/SIG-SCLNRM*EXPTT
1      *((CUM3/SIG3)*H3TT/(2.*SIG)+(CUM4/SIG4)*H4TT/(6.*SIG))
DFDW=DFDSIG*DSIGDW
DFDCM3=SCLNRM*EXPTT*H3TT/(6.*SIG3)
DFDCM4=SCLNRM*EXPTT*H4TT/(24.*SIG4)

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DPRDCF(1) = DFDW*TTH*TTH
DPRDCF(2) = DFDW*TTH
DPRDCF(3) = DFDW

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DPRDCF( 4 ) = 0.
DPRDCF( 5 ) = DFDMU*DMUDS + DFDSIG*DSIGDS + DFDCM3*DCM3DS
1           + DFDCM4*DCM4DS
DPRDCF( 6 ) = 0.
DPRDT=-DFDMU

RETURN
END
SUBROUTINE ASYMCOF(TTHETA,HOL,SOL,ARGS,DERVS)

!PURPOSE: Compute the coefficients of the Edgeworth series model
!          of the axial divergence effects and their derivatives.
!          Written by E. Prince, December, 2004.

```

!CALLING ARGUMENTS:

REAL*4	TTHETA	!2-theta
REAL*4	HOL	!H/L
REAL*4	SOL	!S/L
REAL*4	ARGS(4)	!Arguments of profile function
REAL*4	DERVS(4)	!Derivatives wrt S

!LOCAL VARIABLES:

REAL*4	SIG
REAL*4	CUM3
REAL*4	CUM4
REAL*4	DMUDS
REAL*4	DSIGDS
REAL*4	DCM3DS
REAL*4	DCM4DS
REAL*4	A
REAL*4	B
REAL*4	DADS
REAL*4	DBDS
REAL*4	DELTAM
REAL*4	DELTA1
REAL*4	DELTA2
REAL*4	DELTA3
REAL*4	DELTA4
REAL*4	DD1DS
REAL*4	DD2DS
REAL*4	DD3DS
REAL*4	DD4DS
REAL*4	PIO180

!DATA STATEMENTS:

```
DATA PIO180/0.000174533/
```

!CODE:

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IF(ABS(9000.-TTHETA).LT.4500.)THEN
  DELTAM=-0.5*TAN((9000.-TTHETA)*PIO180)/PIO180
ELSE
  DELTAM=-(0.5/PIO180)/TAN(TTHETA*PIO180)
ENDIF

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```

A=(HOL-SOL)**2
DADS=-2.* (HOL-SOL)
B=(HOL+SOL)**2
DBDS=2.* (HOL+SOL)
DELTAL1=((A+B)/6.)*DELTAM
ARGS(1)=DELTAL1
DELTAL2=((B**2+B*A+A**2)/15.)*DELTAM**2
DELTAL3=((B**3+B**2*A+B*A**2+A**3)/28.)*DELTAM**3
DELTAL4=((B**4+B**3*A+B**2*A**2+B*A**3+A**4)/45.)*DELTAM**4
SIG=SQRT(ARGS(2)+DELTAL2-DELTAL1**2)
ARGS(2)=SIG
CUM3=(DELTAL3-3.*DELTAL1*DELTAL2+2.*DELTAL1**3) !
ARGS(3)=CUM3
CUM4=(DELTAL4-4.*DELTAL1*DELTAL3-3.*DELTAL2**2+12.*DELTAL2*DELTAL1**2
1      -6.*DELTAL1**4)
ARGS(4)=CUM4
DD1DS=(DELTAM/6.)*(DADS+DBDS)
DD2DS=(DELTAM**2/15.)*(DADS*(2.*A+B)+DBDS*(A+2.*B))
DD3DS=(DELTAM**3/28.)*(DADS*(3.*A**2+2.*A*B+B**2)
1      +DBDS*(A**2+2.*A*B+3.*B**2))
DD4DS=(DELTAM**4/45.)
1      *(DADS*(4.*A**3+3.*A**2*B+2.*A*B**2+B**3)
2      +(DBDS*(A**3+2.*A**2*B+3.*A*B**2+4.*B**3)))
DMUDS=DD1DS
DERVS(1)=DMUDS
DSIGDS=(0.5*DD2DS-DELTAL1*DD1DS)/SIG
DERVS(2)=DSIGDS
DCM3DS=((6.*DELTAL1**2-3.*DELTAL2)*DD1DS-3.*DELTAL1*DD2DS
1      +DD3DS)
DERVS(3)=DCM3DS
DCM4DS=((24.* (DELTAL1*DELTAL2-DELTAL1**3)-4.*DELTAL3)*DD1DS
1      +6.* (2.*DELTAL1**2-DELTAL2)*DD2DS-4.*DELTAL1*DD3DS
2      +DD4DS)
DERVS(4)=DCM4DS

RETURN
END
C Implementation of Finger-Cox-Jephcoat peak asymmetry function
C subroutines taken from program PROFILE.FOR found at
C http://www ccp14.ac.uk/ccp/ccp14/ftp-mirror/larryfinger/PROFVAL/
C
      real*4 function Profval( Eta , Gamma , S_L , D_L , TwoTH ,
1      TwoTH0 , dPRdT, dPRdG, dPRdE , dPRdS , dPRdD , Use_Asym )
C
C Returns value of Profile
C   Eta is the mixing coefficient between Gaussian and Lorentzian
C   Gamma is the FWHM
C   S_L is source width/detector distance
C   D_L is detector width/detector distance
C   TwoTH is point at which to evaluate the profile
C   TwoTH0 is two theta value for peak
C   dPRdT is derivative of profile wrt TwoTH0
C   dPRdG is derivative of profile wrt Gamma
C   dPRdE is derivative of profile wrt Eta
C   dPRdS is derivative of profile wrt S_L
C   dPRdD is derivative of profile wrt D_L
C   Use_Asym is true if asymmetry to be used

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```

c
c
c Asymmetry due to axial divergence using the method of Finger, Cox and
c      Jephcoat, J. Appl. Cryst. 27, 892, 1992.

implicit none
real*4 Eta , Gamma , S_L , D_L , TwoTH
real*4 TwoTH0 , dPRdT, dPRdG, dPRdE , dPRdS , dPRdD
logical Use_Asym
integer*4 NTERMS(14)/6,10,20,40,60,80,100,150,200,300,400,
1   600,800,1000/
integer Fstterm(14)/0,3,8,18,38,68,108,158,233,333,483,
1   683,983,1383/
real*4 RAD/57.2957795/

integer*4 ArrayNum , K , NGT, ngt2 , it, i
real*4 Csth          ! cos(theta)
real*4 Tth           ! tan(theta)
real*4 SnTwoTH       ! sin(twoth)
real*4 CsTwoTH       ! cos(twoth)
real*4 ApB           ! (S + H)/L
real*4 AmB           ! (S - H)/L
real*4 ApB2          ! (ApB) **2
real*4 Einfl          ! 2phi value for inflection point
real*4 Emin          ! 2phi value for minimum
real*4 dEmindA       ! derivative of Emin wrt A
real*4 tmp , tmp1 , tmp2 ! intermediate values
real*4 WP(1883) , XP(1883)! Storage for Gauss-Legendre weights and
intervals
real*4 Delta          ! Angle of integration for convolution
real*4 dDELTAdA       ! derivative of DELTA wrt A (S/L)
real*4 sinDELTA        ! sine of DELTA
real*4 cosDELTA        ! cosine of DELTA
real*4 tanDELTA        ! tangent of DELTA
real*4 RcosDELTA       ! 1/cos(DELTA)
real*4 F , dFdA
real*4 G , dGdA , dGdB , PsVoigt
real*4 sumWG , sumWRG , sumWdGdA , sumWRdGdA ,sumWdGdB , sumWRdGdB
real*4 sumWGdRdG , sumWGdRdE , sumWGdRdA , sumWGdRdB , sumWGdRd2t
!
! Values for the abscissas and weights of the Gauss-Legendre
! N-point quadrature formula have been precomputed using routine
! Gauleg from "Numerical Recipes" (Press, Flannery, Teukolsky
! and Vetterling, 1986, Cambridge University Press,
! ISBN 0 521 30811 9), and are stored in the DATA statements
! for XP and WP below.
!
data (xp(i),i= 1, 40)/
$.2386192E+00,.6612094E+00,.9324695E+00,.1488743E+00,.4333954E+00,
$.6794096E+00,.8650634E+00,.9739065E+00,.7652652E-01,.2277859E+00,
$.3737061E+00,.5108670E+00,.6360537E+00,.7463319E+00,.8391170E+00,
$.9122344E+00,.9639719E+00,.9931286E+00,.3877242E-01,.1160841E+00,
$.1926976E+00,.2681522E+00,.3419941E+00,.4137792E+00,.4830758E+00,
$.5494671E+00,.6125539E+00,.6719567E+00,.7273183E+00,.7783057E+00,
$.8246122E+00,.8659595E+00,.9020988E+00,.9328128E+00,.9579168E+00,
$.9772599E+00,.9907262E+00,.9982377E+00,.2595977E-01,.7780933E-01/
data (xp(i),i= 41, 80)/

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$.2323025E+00,.2625881E+00,.2926172E+00,.3223603E+00,.3517885E+00/
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$.3916184E-01,.5481311E-01,.7045093E-01,.8607145E-01,.1016708E+00/
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$.6177838E+00,.6300285E+00,.6421185E+00,.6540509E+00,.6658228E+00/
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$.7329227E+00,.7434919E+00,.7538786E+00,.7640801E+00,.7740941E+00,
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$.2330638E+00,.2432175E+00,.2533446E+00,.2634441E+00,.2735147E+00/
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$.7468072E+00,.7520008E+00,.7571482E+00,.7622490E+00,.7673029E+00,
$.7723096E+00,.7772688E+00,.7821801E+00,.7870433E+00,.7918581E+00/
  data (xp(i),i= 601, 640)/
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$.8197134E+00,.8241811E+00,.8285980E+00,.8329640E+00,.8372787E+00,
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$.9981519E+00,.9985978E+00,.9989822E+00,.9993052E+00,.9995666E+00/
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$.5551622E+00,.5595059E+00,.5638343E+00,.5681473E+00,.5724448E+00/
  data (xp(i),i= 801, 840)/

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  data (xp(i),i= 881, 920)/
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$.9378397E+00,.9396426E+00,.9414198E+00,.9431712E+00,.9448967E+00/
  data (xp(i),i= 921, 960)/
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$.4903704E-01,.5295647E-01,.5687508E-01,.6079282E-01,.6470962E-01/
  data (xp(i),i=1001,1040)/
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$.4968812E+00,.5002831E+00,.5036774E+00,.5070638E+00,.5104425E+00/
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$.5305477E+00,.5338702E+00,.5371846E+00,.5404906E+00,.5437884E+00,
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$.5953790E+00,.5985276E+00,.6016669E+00,.6047970E+00,.6079177E+00,
$.6110291E+00,.6141311E+00,.6172236E+00,.6203066E+00,.6233801E+00,
$.6264440E+00,.6294982E+00,.6325427E+00,.6355775E+00,.6386024E+00/
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$.7136666E+00,.7164102E+00,.7191427E+00,.7218642E+00,.7245746E+00,
$.7272737E+00,.7299617E+00,.7326385E+00,.7353039E+00,.7379581E+00,
$.7406008E+00,.7432322E+00,.7458521E+00,.7484606E+00,.7510575E+00/
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$.7663945E+00,.7689096E+00,.7714129E+00,.7739043E+00,.7763837E+00,
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$.8256328E+00,.8278407E+00,.8300358E+00,.8322182E+00,.8343877E+00,
$.8365444E+00,.8386882E+00,.8408191E+00,.8429370E+00,.8450420E+00/
  data (xp(i),i=1241,1280)/
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$.8573972E+00,.8594104E+00,.8614104E+00,.8633970E+00,.8653704E+00,
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$.8951117E+00,.8968545E+00,.8985835E+00,.9002987E+00,.9020000E+00,
$.9036874E+00,.9053609E+00,.9070204E+00,.9086660E+00,.9102976E+00,
$.9119152E+00,.9135187E+00,.9151081E+00,.9166835E+00,.9182447E+00/
  data (xp(i),i=1281,1320)/
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$.9273143E+00,.9287760E+00,.9302235E+00,.9316566E+00,.9330754E+00,
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  data (xp(i),i=1321,1360)/
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$.9940754E+00,.9944943E+00,.9948979E+00,.9952862E+00,.9956591E+00/
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$.9975745E+00,.9978400E+00,.9980901E+00,.9983248E+00,.9985442E+00,
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$.1485987E+00,.1517031E+00,.1548060E+00,.1579074E+00,.1610073E+00,
$.1641055E+00,.1672022E+00,.1702971E+00,.1733905E+00,.1764821E+00/
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$.4041533E+00,.4070234E+00,.4098896E+00,.4127517E+00,.4156097E+00/
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$.6188318E+00,.6212953E+00,.6237527E+00,.6262040E+00,.6286490E+00/
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$.6669107E+00,.6692472E+00,.6715770E+00,.6739003E+00,.6762169E+00,
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$.6899756E+00,.6922451E+00,.6945077E+00,.6967635E+00,.6990124E+00,
$.7012544E+00,.7034895E+00,.7057176E+00,.7079388E+00,.7101530E+00,
$.7123603E+00,.7145605E+00,.7167536E+00,.7189397E+00,.7211187E+00/
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$.7340426E+00,.7361714E+00,.7382929E+00,.7404071E+00,.7425141E+00,
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$.7946656E+00,.7965678E+00,.7984622E+00,.8003486E+00,.8022273E+00/
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$.8644510E+00,.8660253E+00,.8675910E+00,.8691482E+00,.8706968E+00/
  data (xp(i),i=1721,1760)/
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$.9206172E+00,.9218387E+00,.9230511E+00,.9242545E+00,.9254487E+00/
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$.9622791E+00,.9631287E+00,.9639687E+00,.9647992E+00,.9656203E+00/
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$.9703462E+00,.9711004E+00,.9718451E+00,.9725801E+00,.9733056E+00,
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$.9887805E+00,.9892447E+00,.9896991E+00,.9901437E+00,.9905786E+00/
  data (xp(i),i=1841,1880)/
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$.9929827E+00,.9933492E+00,.9937058E+00,.9940527E+00,.9943897E+00,
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$.9984471E+00,.9986171E+00,.9987772E+00,.9989275E+00,.9990680E+00,
$.9991986E+00,.9993193E+00,.9994302E+00,.9995313E+00,.9996225E+00,
$.9997038E+00,.9997753E+00,.9998369E+00,.9998886E+00,.9999306E+00/
  data (xp(i),i=1881,1883)/
$.9999626E+00,.9999848E+00,.9999971E+00/
  data (wp(i),i= 1, 40)/
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$.2190864E+00,.1494513E+00,.6667134E-01,.1527534E+00,.1491730E+00,
$.1420961E+00,.1316886E+00,.1181945E+00,.1019301E+00,.8327674E-01,
$.6267205E-01,.4060143E-01,.1761401E-01,.7750595E-01,.7703982E-01,
$.7611036E-01,.7472317E-01,.7288658E-01,.7061165E-01,.6791205E-01,
$.6480401E-01,.6130624E-01,.5743977E-01,.5322785E-01,.4869581E-01,
$.4387091E-01,.3878217E-01,.3346020E-01,.2793701E-01,.2224585E-01,
$.1642106E-01,.1049828E-01,.4521277E-02,.5190788E-01,.5176794E-01/
  data (wp(i),i= 41, 80)/
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  data (wp(i),i= 81, 120)/
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$.2669746E-01,.2617622E-01,.2562940E-01,.2505754E-01,.2446120E-01,
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$.7499073E-02,.6546948E-02,.5588428E-02,.4624450E-02,.3655961E-02,
$.2683925E-02,.1709393E-02,.7346345E-03,.2087312E-01,.2086402E-01/
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$.2856855E-02,.2846273E-02,.2835647E-02,.2824977E-02,.2814264E-02,
$.2803508E-02,.2792708E-02,.2781865E-02,.2770980E-02,.2760052E-02,
$.2749081E-02,.2738068E-02,.2727013E-02,.2715915E-02,.2704776E-02,
$.2693596E-02,.2682374E-02,.2671110E-02,.2659805E-02,.2648460E-02,

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$.2637073E-02,.2625646E-02,.2614179E-02,.2602671E-02,.2591123E-02/
  data (wp(i),i=1201,1240)/
$.2579536E-02,.2567908E-02,.2556241E-02,.2544535E-02,.2532789E-02,
$.2521005E-02,.2509181E-02,.2497319E-02,.2485419E-02,.2473480E-02,
$.2461503E-02,.2449488E-02,.2437436E-02,.2425346E-02,.2413218E-02,
$.2401054E-02,.2388852E-02,.2376614E-02,.2364339E-02,.2352028E-02,
$.2339680E-02,.2327296E-02,.2314877E-02,.2302422E-02,.2289931E-02,
$.2277405E-02,.2264844E-02,.2252249E-02,.2239618E-02,.2226953E-02,
$.2214254E-02,.2201520E-02,.2188753E-02,.2175952E-02,.2163117E-02,
$.2150249E-02,.2137349E-02,.2124415E-02,.2111448E-02,.2098449E-02/
  data (wp(i),i=1241,1280)/
$.2085417E-02,.2072354E-02,.2059258E-02,.2046131E-02,.2032972E-02,
$.2019782E-02,.2006561E-02,.1993309E-02,.1980026E-02,.1966713E-02,
$.1953370E-02,.1939996E-02,.1926592E-02,.1913159E-02,.1899697E-02,
$.1886205E-02,.1872684E-02,.1859134E-02,.1845555E-02,.1831949E-02,
$.1818314E-02,.1804650E-02,.1790960E-02,.1777241E-02,.1763495E-02,
$.1749722E-02,.1735922E-02,.1722096E-02,.1708242E-02,.1694363E-02,
$.1680457E-02,.1666526E-02,.1652569E-02,.1638586E-02,.1624578E-02,
$.1610545E-02,.1596488E-02,.1582405E-02,.1568299E-02,.1554168E-02/
  data (wp(i),i=1281,1320)/
$.1540013E-02,.1525835E-02,.1511633E-02,.1497407E-02,.1483159E-02,
$.1468888E-02,.1454594E-02,.1440278E-02,.1425940E-02,.1411579E-02,
$.1397197E-02,.1382794E-02,.1368369E-02,.1353923E-02,.1339456E-02,
$.1324969E-02,.1310461E-02,.1295933E-02,.1281385E-02,.1266817E-02,
$.1252230E-02,.1237623E-02,.1222998E-02,.1208353E-02,.1193690E-02,
$.1179009E-02,.1164309E-02,.1149592E-02,.1134857E-02,.1120104E-02,
$.1105334E-02,.1090547E-02,.1075743E-02,.1060923E-02,.1046086E-02,
$.1031234E-02,.1016365E-02,.1001481E-02,.9865808E-03,.9716658E-03/
  data (wp(i),i=1321,1360)/
$.9567359E-03,.9417913E-03,.9268321E-03,.9118587E-03,.8968712E-03,
$.8818700E-03,.8668551E-03,.8518269E-03,.8367855E-03,.8217313E-03,
$.8066644E-03,.7915851E-03,.7764936E-03,.7613902E-03,.7462750E-03,
$.7311483E-03,.7160104E-03,.7008614E-03,.6857017E-03,.6705313E-03,
$.6553507E-03,.6401600E-03,.6249593E-03,.6097491E-03,.5945295E-03,
$.5793007E-03,.5640630E-03,.5488166E-03,.5335618E-03,.5182987E-03,
$.5030277E-03,.4877489E-03,.4724626E-03,.4571690E-03,.4418684E-03,
$.4265610E-03,.4112470E-03,.3959267E-03,.3806003E-03,.3652680E-03/
  data (wp(i),i=1361,1400)/
$.3499301E-03,.3345867E-03,.3192383E-03,.3038849E-03,.2885269E-03,
$.2731644E-03,.2577977E-03,.2424270E-03,.2270526E-03,.2116747E-03,
$.1962935E-03,.1809093E-03,.1655224E-03,.1501328E-03,.1347410E-03,
$.1193471E-03,.1039514E-03,.8855408E-04,.7315545E-04,.5775582E-04,
$.4235569E-04,.2695689E-04,.1158044E-04,.3140018E-02,.3139987E-02,
$.3139926E-02,.3139833E-02,.3139709E-02,.3139554E-02,.3139368E-02,
$.3139152E-02,.3138904E-02,.3138625E-02,.3138316E-02,.3137975E-02,
$.3137604E-02,.3137201E-02,.3136768E-02,.3136304E-02,.3135809E-02/
  data (wp(i),i=1401,1440)/
$.3135283E-02,.3134726E-02,.3134138E-02,.3133519E-02,.3132869E-02,
$.3132189E-02,.3131477E-02,.3130735E-02,.3129962E-02,.3129158E-02,
$.3128323E-02,.3127457E-02,.3126560E-02,.3125633E-02,.3124675E-02,
$.3123686E-02,.3122666E-02,.3121615E-02,.3120534E-02,.3119422E-02,
$.3118279E-02,.3117105E-02,.3115901E-02,.3114666E-02,.3113400E-02,
$.3112103E-02,.3110776E-02,.3109418E-02,.3108029E-02,.3106610E-02,
$.3105160E-02,.3103680E-02,.3102169E-02,.3100627E-02,.3099055E-02,
$.3097452E-02,.3095819E-02,.3094155E-02,.3092461E-02,.3090736E-02/
  data (wp(i),i=1441,1480)/
$.3088981E-02,.3087195E-02,.3085379E-02,.3083532E-02,.3081655E-02,

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$.3079748E-02,.3077810E-02,.3075842E-02,.3073843E-02,.3071815E-02,
$.3069756E-02,.3067666E-02,.3065547E-02,.3063397E-02,.3061217E-02,
$.3059007E-02,.3056766E-02,.3054496E-02,.3052195E-02,.3049865E-02,
$.3047504E-02,.3045113E-02,.3042692E-02,.3040242E-02,.3037761E-02,
$.3035250E-02,.3032709E-02,.3030139E-02,.3027538E-02,.3024908E-02,
$.3022248E-02,.3019558E-02,.3016838E-02,.3014089E-02,.3011310E-02,
$.3008501E-02,.3005662E-02,.3002794E-02,.2999896E-02,.2996969E-02/
  data (wp(i),i=1481,1520)/
$.2994012E-02,.2991026E-02,.2988010E-02,.2984965E-02,.2981890E-02,
$.2978786E-02,.2975652E-02,.2972489E-02,.2969297E-02,.2966075E-02,
$.2962825E-02,.2959545E-02,.2956236E-02,.2952897E-02,.2949530E-02,
$.2946134E-02,.2942708E-02,.2939254E-02,.2935770E-02,.2932258E-02,
$.2928716E-02,.2925146E-02,.2921547E-02,.2917919E-02,.2914262E-02,
$.2910577E-02,.2906863E-02,.2903120E-02,.2899349E-02,.2895549E-02,
$.2891720E-02,.2887863E-02,.2883978E-02,.2880064E-02,.2876122E-02,
$.2872151E-02,.2868152E-02,.2864125E-02,.2860069E-02,.2855985E-02/
  data (wp(i),i=1521,1560)/
$.2851873E-02,.2847734E-02,.2843565E-02,.2839369E-02,.2835145E-02,
$.2830893E-02,.2826613E-02,.2822305E-02,.2817970E-02,.2813606E-02,
$.2809215E-02,.2804796E-02,.2800350E-02,.2795875E-02,.2791374E-02,
$.2786844E-02,.2782288E-02,.2777704E-02,.2773092E-02,.2768453E-02,
$.2763787E-02,.2759094E-02,.2754373E-02,.2749625E-02,.2744850E-02,
$.2740048E-02,.2735219E-02,.2730363E-02,.2725480E-02,.2720571E-02,
$.2715634E-02,.2710671E-02,.2705681E-02,.2700664E-02,.2695621E-02,
$.2690551E-02,.2685454E-02,.2680331E-02,.2675182E-02,.2670006E-02/
  data (wp(i),i=1561,1600)/
$.2664804E-02,.2659576E-02,.2654321E-02,.2649040E-02,.2643733E-02,
$.2638400E-02,.2633041E-02,.2627657E-02,.2622246E-02,.2616809E-02,
$.2611347E-02,.2605858E-02,.2600344E-02,.2594805E-02,.2589240E-02,
$.2583649E-02,.2578033E-02,.2572391E-02,.2566724E-02,.2561032E-02,
$.2555315E-02,.2549572E-02,.2543804E-02,.2538011E-02,.2532193E-02,
$.2526350E-02,.2520483E-02,.2514590E-02,.2508672E-02,.2502730E-02,
$.2496763E-02,.2490772E-02,.2484756E-02,.2478715E-02,.2472650E-02,
$.2466561E-02,.2460447E-02,.2454309E-02,.2448147E-02,.2441961E-02/
  data (wp(i),i=1601,1640)/
$.2435751E-02,.2429516E-02,.2423258E-02,.2416976E-02,.2410670E-02,
$.2404340E-02,.2397986E-02,.2391609E-02,.2385209E-02,.2378784E-02,
$.2372337E-02,.2365866E-02,.2359371E-02,.2352853E-02,.2346312E-02,
$.2339748E-02,.2333161E-02,.2326551E-02,.2319918E-02,.2313262E-02,
$.2306584E-02,.2299882E-02,.2293158E-02,.2286411E-02,.2279642E-02,
$.2272850E-02,.2266036E-02,.2259200E-02,.2252341E-02,.2245460E-02,
$.2238557E-02,.2231631E-02,.2224684E-02,.2217715E-02,.2210724E-02,
$.2203711E-02,.2196777E-02,.2189620E-02,.2182543E-02,.2175443E-02/
  data (wp(i),i=1641,1680)/
$.2168323E-02,.2161180E-02,.2154017E-02,.2146832E-02,.2139626E-02,
$.2132400E-02,.2125152E-02,.2117833E-02,.2110593E-02,.2103282E-02,
$.2095951E-02,.2088599E-02,.2081226E-02,.2073833E-02,.2066420E-02,
$.2058986E-02,.2051531E-02,.2044057E-02,.2036562E-02,.2029047E-02,
$.2021513E-02,.2013958E-02,.2006384E-02,.1998789E-02,.1991175E-02,
$.1983542E-02,.1975888E-02,.1968216E-02,.1960524E-02,.1952812E-02,
$.1945082E-02,.1937332E-02,.1929563E-02,.1921775E-02,.1913968E-02,
$.1906142E-02,.1898298E-02,.1890434E-02,.1882552E-02,.1874652E-02/
  data (wp(i),i=1681,1720)/
$.1866733E-02,.1858795E-02,.1850840E-02,.1842866E-02,.1834874E-02,
$.1826863E-02,.1818835E-02,.1810789E-02,.1802725E-02,.1794643E-02,
$.1786544E-02,.1778427E-02,.1770292E-02,.1762140E-02,.1753970E-02,
$.1745784E-02,.1737580E-02,.1729359E-02,.1721120E-02,.1712865E-02,

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$.1704593E-02,.1696304E-02,.1687999E-02,.1679677E-02,.1671338E-02,
$.1662983E-02,.1654611E-02,.1646223E-02,.1637819E-02,.1629399E-02,
$.1620962E-02,.1612510E-02,.1604042E-02,.1595557E-02,.1587058E-02,
$.1578542E-02,.1570011E-02,.1561465E-02,.1552903E-02,.1544325E-02/
  data (wp(i),i=1721,1760)/
$.1535733E-02,.1527125E-02,.1518503E-02,.1509865E-02,.1501213E-02,
$.1492545E-02,.1483863E-02,.1475167E-02,.1466456E-02,.1457730E-02,
$.1448990E-02,.1440236E-02,.1431467E-02,.1422684E-02,.1413888E-02,
$.1405077E-02,.1396253E-02,.1387414E-02,.1378563E-02,.1369697E-02,
$.1360818E-02,.1351926E-02,.1343020E-02,.1334101E-02,.1325169E-02,
$.1316224E-02,.1307265E-02,.1298294E-02,.1289310E-02,.1280314E-02,
$.1271305E-02,.1262283E-02,.1253249E-02,.1244202E-02,.1235143E-02,
$.1226072E-02,.1216989E-02,.1207894E-02,.1198787E-02,.1189668E-02/
  data (wp(i),i=1761,1800)/
$.1180538E-02,.1171396E-02,.1162242E-02,.1153077E-02,.1143900E-02,
$.1134712E-02,.1125513E-02,.1116303E-02,.1107082E-02,.1097850E-02,
$.1088607E-02,.1079354E-02,.1070089E-02,.1060815E-02,.1051529E-02,
$.1042234E-02,.1032928E-02,.1023612E-02,.1014286E-02,.1004950E-02,
$.9956034E-03,.9862475E-03,.9768819E-03,.9675067E-03,.9581219E-03,
$.9487276E-03,.9393240E-03,.9299112E-03,.9204892E-03,.9110581E-03,
$.9016180E-03,.8921690E-03,.8827112E-03,.8732448E-03,.8637697E-03,
$.8542861E-03,.8447941E-03,.8352937E-03,.8257851E-03,.8162684E-03/
  data (wp(i),i=1801,1840)/
$.8067436E-03,.7972109E-03,.7876703E-03,.7781220E-03,.7685659E-03,
$.7590023E-03,.7494312E-03,.7398528E-03,.7302670E-03,.7206740E-03,
$.7110739E-03,.7014668E-03,.6918528E-03,.6822320E-03,.6726045E-03,
$.6629703E-03,.6533295E-03,.6436824E-03,.6340289E-03,.6243691E-03,
$.6147032E-03,.6050312E-03,.5953533E-03,.5856694E-03,.5759799E-03,
$.5662846E-03,.5565837E-03,.5468774E-03,.5371657E-03,.5274486E-03,
$.5177264E-03,.5079991E-03,.4982667E-03,.4885295E-03,.4787874E-03,
$.4690406E-03,.4592892E-03,.4495332E-03,.4397729E-03,.4300082E-03/
  data (wp(i),i=1841,1880)/
$.4202392E-03,.4104661E-03,.4006890E-03,.3909079E-03,.3811229E-03,
$.3713342E-03,.3615418E-03,.3517459E-03,.3419465E-03,.3321437E-03,
$.3223377E-03,.3125285E-03,.3027162E-03,.2929009E-03,.2830827E-03,
$.2732617E-03,.2634380E-03,.2536118E-03,.2437830E-03,.2339519E-03,
$.2241184E-03,.2142827E-03,.2044449E-03,.1946051E-03,.1847634E-03,
$.1749198E-03,.1650745E-03,.1552276E-03,.1453792E-03,.1355293E-03,
$.1256781E-03,.1158257E-03,.1059721E-03,.9611747E-04,.8626190E-04,
$.7640548E-04,.6654832E-04,.5669051E-04,.4683217E-04,.3697344E-04/
  data (wp(i),i=1881,1883)/
$.2711461E-04,.1725677E-04,.7413338E-05/

```

```

CsTH = cos(TwoTH0 * 0.5/RAD)
if (abs(CsTH) .lt. 1.0e-15) CsTH = 1.0e-15
TTH = sin(TwoTH0 * 0.5/RAD)/CsTH
CsTwoTH = cos(TwoTH0/RAD)
SnTwoTH = sin(TwoTH0/RAD)
ApB = S_L + D_L
AmB = S_L - D_L
ApB2 = ApB**2
if (((S_L .ne. 0.0) .or. (D_L .ne. 0.0)) .and. Use_Asym) then
  tmp = sqrt(1.0 + AmB**2)*CsTwoTH
  if (abs(tmp) .gt. 1.0) then
    Einfl = acos(CsTwoTH)*RAD
  else
    Einfl = acos(tmp)*RAD

```

```

        endif
        tmp2 = 1.0 + ApB2
        tmp = sqrt(tmp2) * CsTwoTH

c If S_L or D_L are zero, set Einfl = 2theta

        if ((S_L .eq. 0.0) .or. (D_L .eq. 0.0)) Einfl = TwoTH0
        if (abs(tmp) .le. 1.0) then
            Emin = acos(tmp) * RAD
            tmp1 = tmp2 * (1.0 - tmp2 * CsTwoTH**2)
        else
            tmp1 = 0.0
            if (tmp .gt. 0.0) then
                Emin = 0.0
            else
                Emin = 180.0
            endif
        endif
        if ((tmp1 .gt. 0.0) .and. (abs(tmp) .le. 1.0)) then
            dEmindA = -ApB * CsTwoTH/sqrt(tmp1)
        else
            dEmindA = 0.0
        endif
        ArrayNum = 1
        K = 400.0 * (TwoTH0 - Emin) ! Calculate number of terms needed
        do while ((ArrayNum .lt. 14) .and. (K .gt. NTERMS(ArrayNum)))
            ArrayNum = ArrayNum + 1
        enddo
        NGT = nterms(ArrayNum) ! Save number of terms
        ngt2 = ngt / 2

c Clear terms needed for summations
        sumWG = 0.0
        sumWRG = 0.0
        sumWdGdA = 0.0
        sumWRdGdA = 0.0
        sumWdGdB = 0.0
        sumWRdGdB = 0.0
        sumWGdRd2t = 0.0
        sumWGdRdG = 0.0
        sumWGdRdE = 0.0
        sumWGdRdA = 0.0
        sumWGdRdB = 0.0

c Compute the convolution integral
        it = fstterm(arraynum)-ngt2
        do K = ngt2 , NGT
            delta = Emin + (TwoTH0 - Emin) * xp(K + it)
            dDeltada = (1.0 - xp(k+it)) * dEmindA
            sinDELTA = sin(Delta/RAD)
            cosDELTA = cos(Delta/RAD)
            if (abs(cosDELTA) .lt. 1.0e-15) cosDELTA = 1.0e-15
            RcosDELTA = 1.0 / cosDELTA
            tanDELTA = tan(Delta/RAD)
            tmp = cosDELTA**2 - CsTwoTH**2
            if (tmp .gt. 0.0) then
                tmp1 = sqrt(tmp)
                F = abs(CsTwoTH) / tmp1
                dFdA = cosDELTA * CsTwoTH * sinDELTA * dDELTAdA
            endif
        enddo
    enddo

```

```

1           / (tmp1 * tmp1 * tmp1)
else
  F = 0.0
  dFdA = 0.0
endif
c calculate G(Delta,2theta) , FCJ eq. 7a and 7b
if ( abs(Delta - Emin) .gt. abs(Einfl - Emin)) then
  if (S_L .gt. D_L) then
!
! N.B. this is the only place where d()/dA <> d()/dB
!
  G = 2.0 * D_L * F * RcosDELTA
  dGdA = 2.0 * D_L * RcosDELTA * (dFdA +
    F*tanDELTA*dDELTAdA)
  1   dGdB = dGdA + 2.0 * F * RcosDELTA
else
  G = 2.0 * S_L * F * RcosDELTA
  dGdB = 2.0 * S_L * RcosDELTA
  1   *(dFdA + F * tanDELTA * dDELTAdA)
  dGdA = dGdB + 2.0 * F * RcosDELTA
endif
else
  G = (-1.0 + ApB * F) * RcosDELTA
  dGdA = RcosDELTA * (F - tanDELTA * dDELTAdA + ApB * dFdA
  1   + ApB * F * tanDELTA * dDELTAdA)
  dGdB = dGdA
endif
tmp = PsVoigt(TwoTh-DELTA+TwoTH0,TwoTH0,eta,Gamma,dPRdT
  1   ,dPRdG,dPRdE)
sumWG = sumWG + wp(k+it) * G
sumWRG = sumWRG + wp(k+it) * G * tmp
sumWdGdA = sumWdGdA + wp(k+it) * dGdA
sumWdGdB = sumWdGdB + wp(k+it) * dGdB
sumWRdGdA = sumWRdGdA + wp(k+it) * dGdA * tmp
sumWRdGdB = sumWRdGdB + wp(k+it) * dGdB * tmp
sumWGdRd2t = sumWGdRd2t + wp(k+it) * G * dPRdT
sumWGdRdG = sumWGdRdG + wp(k+it) * G * dPRdG
sumWGdRdE = sumWGdRdE + wp(k+it) * G * dPRdE
sumWGdRdA = sumWGdRdA + wp(k+it) * G * dPRdT * dDELTAdA * RAD
enddo
if (sumWG .eq. 0.0) sumWG = 1.0
Profval = sumWRG / sumWG
dPRdT = sumWGdRd2t / sumWG
dPRdG = sumWGdRdG / sumWG
dPRdE = sumWGdRdE / sumWG
dPRdS = (sumWRdGdA + sumWGdRdA/RAD) / sumWG - sumWRG *
  1   sumWdGdA/RAD/sumWG**2
dPRdD = (sumWRdGdB + sumWGdRdA/RAD) / sumWG - sumWRG *
  1   sumWdGdB/RAD/sumWG**2
else ! here for no asymmetry }
tmp = PsVoigt(TwoTH,TwoTH0,eta,Gamma,dPRdT,dPRdG,dPRdE)
Profval = tmp
dPRdS = 0.0
dPRdD = 0.0
endif
return
end

```

```

real*4 function Gauss(Pos , Pos0 , Gamma , dGdT , dGdG )

c Return value of Gaussian at 'Pos' for peak at 'Pos0' and 'Gamma'.
c dGdT is derivative of G wrt Pos0.
c dGdG is derivative of G wrt Gamma.

implicit none
real*4 Pos , Pos0 , Gamma , dGdT , dGdG
real*4 c / 1.6651092/
real*4 cg / 0.939437279/
real*4 delp , temp

delp = Pos - Pos0
if (abs(delp)/Gamma .gt. 6) then
    Gauss = 0.0
    dGdT = 0.0
    dGdG = 0.0
else
    temp = cg * exp(-(delp * c /Gamma)**2)/Gamma
    Gauss = temp
    dGdG = temp * ( -1.0 + 2.0 * (delp * c/Gamma)**2) / Gamma
    dGdT = 2.0 * c**2 * delp * temp/Gamma**2
endif
return
end

real*4 function Lorentz(Pos , Pos0 , Gamma , dLdT , dLdG )

c Return value of Lorentzian at 'Pos' for peak at 'Pos0' and 'Gamma'.
c dLdT is derivative of L wrt Pos0.
c dLdG is derivative of L wrt Gamma.

implicit none
real*4 Pos , Pos0 , Gamma , dLdT , dLdG
real*4 cl / 0.636619772/

real*4 delp , denom

delp = Pos - Pos0
denom = 4.0 * delp**2 + Gamma**2
Lorentz = cl * Gamma / denom
dLdT = 8.0 * cl * Gamma * delp / denom**2
dLdG = cl * (4.0 * delp**2 - Gamma**2) / denom**2
return
end

real*4 function PsVoigt(TwoTH , TwoTH0 , eta , Gamma,
1           dPRdT , dPRdG , dPRdE )

c
c Returns value of Pseudo Voigt
c Eta is the mixing coefficient between Gaussian and Lorentzian
c Gamma is the FWHM
c TwoTH is point at which to evaluate the profile
c TwoTH0 is two theta value for peak
c dPRdT is derivative of profile wrt TwoTH0

```

```

c      dPRdG is derivative of profile wrt Gamma
c      dPRdE is derivative of profile wrt Eta

      implicit none
      real*4 TwoTH , TwoTH0 , eta , Gamma
      real*4 dPRdT , dPRdG , dPRdE
      real*4 G,Gauss          ! Gaussian part
      real*4 L,Lorentz         ! Lorentzian part
      real*4 dGdT , dGdG , dLdT , dLdG

      G = Gauss(TwoTH , TwoTH0 , Gamma , dGdT , dGdG )
      L = Lorentz(TwoTH , TwoTH0 , Gamma , dLdT , dLdG )
      PsVoigt = Eta * L + (1.0 - Eta) * G
      dPRdT = Eta * dLdT + (1.0 - Eta) * dGdT
      dPRdG = Eta * dLdG + (1.0 - Eta) * dGdG
      dPRdE = L - G
      return
      end

```