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Study of ferrite ferrofluids by small-angle scattering of polarized neutrons

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Nanoparticles consisting of a magnetic core (Fe₃O₄, CoFe₂O₄ and CuFe₂O₄) and a hydrophobic shell were prepared by chemical co-precipitation of the inorganic cores and by subsequently modifying the surface with dodecanoic acid. The nanoparticles were then dispersed in cyclohexane to form stable ferrofluids. These dispersions were investigated by small-angle scattering of polarized neutrons and the data were interpreted according to a 'pearl-necklace' model, opportunely modified to account for the core–shell structure of the particles. Results of the fitting show that the particles consist of a magnetic core with a mean radius of 40–50 Å and an organic shell with a thickness of 7–8 Å. These nanoparticles assemble in fractal aggregates when a magnetic field is applied.

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1. Introduction

Ferrofluids are stable colloidal suspensions of magnetic nanoparticles dispersed in a liquid (Leslie-Pelecky & Rieke, 1996). Since their first appearance (Papell, 1965), magnetic fluids have been studied especially because of their potentially large number of applications in different fields such as magnetism, optics, rheology, biophysics, medicine and thermodynamics (Berkovsky & Bashtovoy, 1996; Bonini *et al.*, 2004*a*,*b*). Many synthetic methodologies have been developed to prepare magnetic nanoparticles and magnetic fluids. Among them, the mechanical processes (grinding, milling *etc.*) (Berbenni *et al.*, 2003), synthesis from supersaturated solutions (Massart, 1980, 1981, 1982), the thermal decomposition of precursors (Sun & Murray, 1999; Hyeon *et al.*, 2001; Hyeon, 2003; Park *et al.*, 2005) and the use of microemulsions as nanoreactors are probably the most used (Bonini *et al.*, 2002, 2004*a*,*b*).

In particular, there has been great interest in ferrofluids synthesized by chemical co-precipitation from supersaturated solutions, *i.e.* dispersions in water of ultra small magnetic nanoparticles, stabilized by an appropriate particle surface treatment. In this kind of ferrofluid, each single particle behaves as a single magnetic domain, giving rise to so-called superparamagnetic behaviour. Due to the easy and economic preparation methodology, these magnetic fluids are ideal for several technological applications, especially when production costs are prominent. Unfortunately, especially when directly exposed to oxygen, magnetic nanoparticles may undergo degradation, resulting in the alteration of their magnetic properties.

In surfactant-stabilized ferrofluids, the stability of the suspension is due to the steric hindrance of the surfactant molecules that counteracts the dipolar attraction among the magnetic cores, producing a dispersion of the particles with randomly oriented magnetic moments. Moreover, the presence of a shell of an inert material such as a fatty acid on the surface of ferrite nanoparticles prevents their aggregation and protects the magnetic particles from possible decomposition induced by the surrounding environment.

Small-angle scattering is a technique well suited for the characterization of complex colloidal fluids (Guinier & Fournet, 1955). In particular, the size and size distribution of suspensions of nanoparticles can be obtained from the intensity of small-angle neutron scattering patterns. It has been shown that when using polarized neutrons the relative contrasts for small-angle scattering of magnetic systems are strongly modified (Keller et al., 2000; Wiedenmann, 2000, 2002; Wiedenmann et al., 2002). In this paper, we used this property to study magnetic fluids obtained from the dispersion in cyclohexane of hydrophobically modified ferrite nanoparticles. The magnetic nanoparticles were obtained through the co-precipitation of the precursors in alkaline conditions and by subsequently grafting a fatty acid onto the surface of the particles. The analysis of the scattering data allowed a complete description of the size, size distribution and layer thickness of the core-shell ferrite nanoparticles. Moreover, the results of the fitting provided important information about the formation of aggregates under an external magnetic field. It is well known that some ferrofluids form aggregates under an applied magnetic field through the alignment of the magnetic dipoles along the direction of the field, while others do not (Jacobs & Bean, 1963; de Gennes & Pincus, 1970; Liu et al., 1995). Several experimental and theoretical studies have been performed in order to explain the formation of these aggregates; nevertheless, this process is still not completely understood (Toor, 1993; Gross & Kiskamp, 1997; Lalatonne et al., 2004). Here we report an analysis based on the so-called 'pearlnecklace' model, originally applied to protein micellized surfactant systems.

2. Experimental

2.1. Reagents

Iron(II) chloride tetrahydrate (99%), iron(III) chloride hexahydrate (97%), tetramethylammonium hydroxide (25% solution in water) and deuterated cyclohexane (99.9%) were purchased from Aldrich. Copper(II) chloride dihydrate (99%), sodium hydroxide

(99%), cobalt(II) nitrate hexahydrate (99%), concentrated nitric acid (90%), iron(III) nitrate nonahydrate (>98%), dodecanoic acid (99%), methyl alcohol (99.5%) and acetone (99.5%) were purchased from Fluka. Cobalt(II) chloride hexahydrate (99%) was purchased from Carlo Erba. All the reagents were used as received.

2.2. Synthesis of magnetic nanoparticles

Ferrofluids were synthesized using minor modifications of Massart's method (Massart, 1980, 1981). Aqueous solutions with 1 M concentration of the M^{2+} and Fe³⁺ cations (where M^{2+} is Fe²⁺, Co²⁺ or Cu²⁺) were prepared by dissolving the corresponding chloride salts in deoxygenated water (nitrogen bubbling for 0.5 h before preparation of the solutions). Solutions containing Fe^{3+} (10 ml) and M^{2+} (5 ml) were mixed and added to concentrated nitric acid (0.5 ml). At this stage, the M^{2+}/Fe^{3+} mixture is kept in an acidic medium in order to avoid possible metal hydrolysis. This mixture and 65 ml of 1 M sodium hydroxide aqueous solution were separately heated up to boiling point and then mixed as fast as possible under vigorous stirring. The boiling temperature and the stirring were maintained for 2 h. The precipitate was then collected by magnetic decantation, washed twice with water and dispersed under vigorous stirring in a 2 M HNO₃ solution. The precipitate was isolated again by magnetic decantation and dispersed in 15 ml of a boiling solution containing $M(NO_3)_2$ (0.15 M) and Fe(NO₃)₃. The precipitate obtained after this treatment was isolated, washed once with water and twice with acetone, and dispersed in 5 ml of water by adding tetramethylammonium hydroxide until a stable ferrofluid was obtained. Residual acetone was removed in a moderate vacuum at 313 K. The fluid was finally centrifuged at 4500 g for 0.35 h and the precipitate was discarded. The concentration of the nanoparticles was checked by thermogravimetric analysis and water was eventually added to the resulting ferrofluid so as to obtain a 5 wt% solid content.

2.3. Hydrophobic modification

An aliquot of the previously described ferrofluid (2 ml, 100 mg of nanoparticles) was diluted with water to 50 ml. 5 ml of a 2 wt% dodecanoic acid solution in acetone was then added to the diluted ferrofluid. The solution was heated to 353 K for 0.5 h under stirring to produce a water-based suspension, which was cooled to room temperature. Acetone and MeOH were added to precipitate the particles, which were then isolated by magnetic decantation and washed three times with acetone and MeOH. The particles were dried and finally dispersed in deuterated cyclohexane to form a stable magnetic fluid.

2.4. Small-angle scattering of polarized neutrons

Small-angle scattering of polarized neutrons (SANSPOL) measurements were performed with the V4 instrument at the BERII reactor of the Hahn-Meitner Institute, Berlin (Keller *et al.*, 2000). A neutron wavelength λ of 6 Å and detector distances of 1, 4 and 12 m were used, corresponding to a Q range [$Q = (4\pi/\lambda) \sin(\theta/2)$, where θ is the scattering angle] of 0.005–0.3 Å⁻¹. A horizontal magnetic field strength up to about 1 T was applied at the sample position, oriented perpendicularly to the incoming neutrons. Polarized neutrons are provided by a transmission polarizing supermirror cavity. The polarization direction is reversed using a spin flipper in front of the sample.

For polarized neutrons, where the neutron spins are aligned antiparallel (+) or parallel (-) to the magnetic field vector **H**, the scattering cross sections depend on the polarization of the incident neutrons $I^+(Q)$ and $I^-(Q)$, respectively. The scattering intensity relationships (denoted here as SANSPOL intensities) have been previously derived (Wiedenmann, 2000, 2002). When the magnetic moments and neutron polarization are fully aligned along the external field, the SANSPOL intensities perpendicular to the applied field are given for the two states by

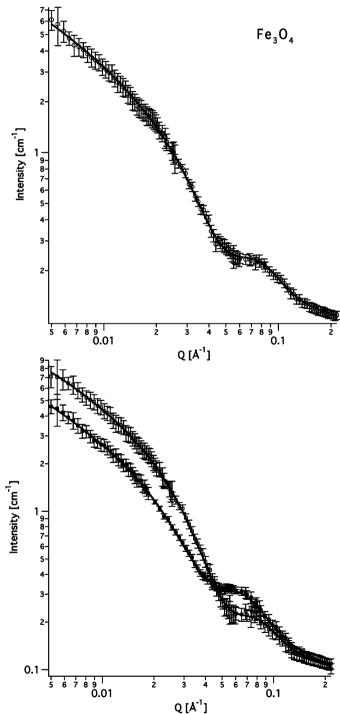


Figure 1

SANSPOL intensities parallel (top) and perpendicular [bottom, $I^+(Q \perp H)$ indicated by open squares and $I^-(Q \perp H)$ indicated by filled squares] to the applied field for Fe₃O₄ ferrofluid. Solid lines represent the best fitting results according to the pearl-necklace model.

Table 1

Results obtained by fitting SANSPOL data to the pearl-necklace model.

	Fe ₃ O ₄	CoFe ₂ O ₄	CuFe ₂ O ₄
Volume fraction ($\times 10^{-2}$)	1.070 ± 0.135	0.753 ± 0.036	2.241 ± 0.147
Core radius (Å)	38.9 ± 1.9	49.1 ± 1.6	39.1 ± 4.3
Core polydispersity, σ_c	0.30 ± 0.03	0.32 ± 0.02	0.48 ± 0.05
Shell thickness (Å)	7.6 ± 1.3	8.0 ± 1.1	6.7 ± 2.1
SLD core, parallel $(\times 10^{-6} \text{\AA}^{-2})$	6.933 ± 0.009	$5.901E - 6 \pm 0.008$	6.491 ± 0.016
SLD core, perpendicular, on (× 10^{-6} Å ⁻²)	7.258 ± 0.009	$6.253E - 6 \pm 0.008$	6.630 ± 0.017
SLD core, perpendicular, off (× 10^{-6} Å ⁻²)	6.606 ± 0.009	$5.557E-6 \pm 0.008$	6.352 ± 0.015
SLD shell ($\times 10^{-6} \text{ Å}^{-2}$)	0.089 ± 0.012	0.089 ± 0.018	0.089 ± 0.013
Fractal dimension, D	1.076 ± 0.166	1.621 ± 0.285	1.176 ± 0.264
Correlation length (Å)	544.5 ± 163.5	192.3 ± 73.6	158.0 ± 89.0

$$I^{(-,+)}(Q \perp H) \propto [P_{\rm N} \pm P_{\rm M}]^2 S(Q),$$
 (1)

where $P_{\rm N}$ and $P_{\rm M}$ represent the nuclear and magnetic form factors, respectively, and S(Q) is the interparticle structure factor.

The arithmetic mean of the parallel and antiparallel intensities perpendicular to the applied field corresponds to the cross section for unpolarized neutrons:

$$[I^{-}(Q \perp H) + I^{+}(Q \perp H)]/2 = I^{\text{unpol}}(Q \perp H) \propto [P_{\text{N}}^{2} + P_{\text{M}}^{2}]S(Q).$$
(2)

The scattering cross section parallel to \mathbf{H} is independent of the polarization state since it depends on pure nuclear contrast and is given by

$$I(Q \parallel H) \propto P_{\rm N}^2 S(Q). \tag{3}$$

The difference between the two intensities represents a magnetic nuclear cross term, allowing the magnetic contrast with respect to the nuclear contrast to be determined:

$$I^{-}(Q,\alpha) - I^{+}(Q,\alpha) \propto P_{\rm N} P_{\rm M} S(Q), \tag{4}$$

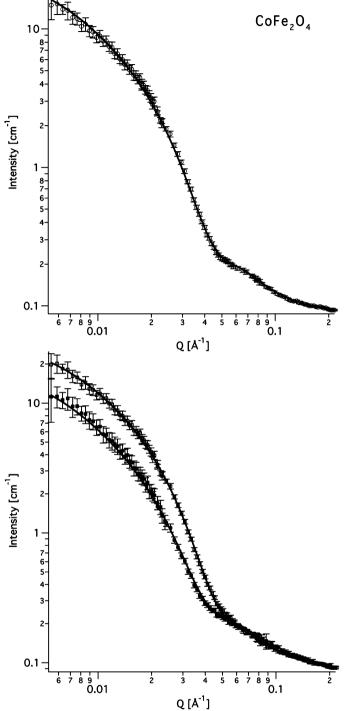
where α is the azimuth angle between the magnetic field vector **H** and the scattering vector **Q** (**Q** = **k**_i - **k**_s, where **k**_i and **k**_s are the incident and scattering wavevectors, respectively).

Both the perpendicular and the parallel intensities have been calculated in two separate ways, obtaining identical results: (i) by adjusting the two-dimensional (2D) pattern to the $\sin^2 \alpha$ dependence, and (ii) by averaging the 2D pattern only over sectors with a width of 5° and centred at $\alpha = 90$ and 270° for the perpendicular intensities, and centred at $\alpha = 0$ and 180° for the parallel intensities. As expected, the parallel intensities for the two flipper states were identical: in fact, as indicated in equation (4), these intensities account only for the nuclear scattering.

3. Results and discussion

Hydrophobic iron ferrite nanoparticles have been synthesized by grafting dodecanoic acid onto the surface of ferrite nanoparticles prepared through alkaline co-precipitation. These hydrophobically modified nanoparticles were dispersed in cyclohexane to form stable ferrofluids that were investigated by using the SANSPOL approach.

Scattering results were fitted according to the model introduced by Chen & Teixeira (1986) for the analysis of the structure and the fractal dimension of protein-detergent complexes. This model was developed to describe the scattering pattern produced by a string of spherical micelles distributed along a polypeptide chain, nicknamed a 'pearl necklace'. Chen and Teixeira's pearl-necklace model neglects the contribution arising from the peptide chain. This approximation





SANSPOL intensities parallel (top) and perpendicular [bottom, $I^*(Q \perp H)$ indicated by open squares and $\Gamma(Q \perp H)$ indicated by filled squares] to the applied field for CoFe₂O₄ ferrofluid. Solid lines represent the best fitting results according to the pearl-necklace model.

was justified by the fact that the major contrast was between the micelles and the solvent, *i.e.* the radiation was scattered only by the 'pearls' and not by the backbone. In our case the same approximation is legitimate because of the absence of a backbone, since the nano-particles are eventually assembled in aggregates only because of their magnetic moment interactions.

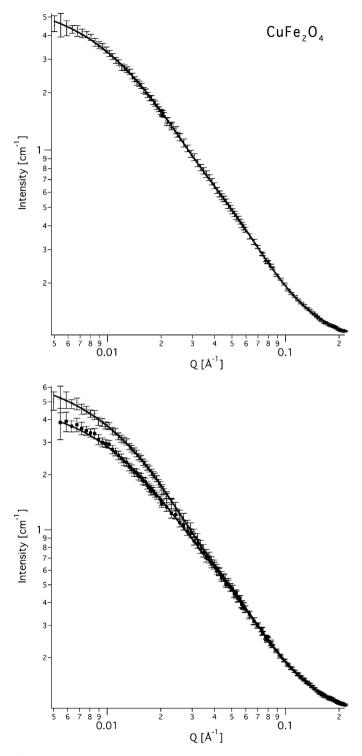


Figure 3

SANSPOL intensities parallel (top) and perpendicular [bottom, $I^+(Q \perp H)$ indicated by open squares and $\Gamma(Q \perp H)$ indicated by filled squares] to the applied field for CuFe₂O₄ ferrofluid. Solid lines represent the best fitting results according to the pearl-necklace model.

In a SANS experiment, the measured intensity of the radiation, I(Q), scattered by a collection of uniform particles is given by (Guinier & Fournet, 1955; Chen & Teixeira, 1986)

$$I(Q) = \phi P(Q)S(Q) + bkg, \tag{5}$$

where ϕ is the particle volume fraction, P(Q) is the form factor, S(Q) is the interparticle structure factor accounting for the interparticle correlations, and bkg is the incoherent background.

Chen and Teixeira used the form factor P(Q) of a sphere to describe the micelles. In this study we cannot consider a simple sphere as form factor since the magnetic particles comprise a metallic core and an organic shell. Therefore, we modified the model by introducing the particle form factor proposed by Bartlett and Ottewill for polydisperse spherical particles with a core-shell structure (Bartlett & Ottewill, 1992). In this form factor the spherical particles have a constant shell thickness and a core with a Schulz distribution of radii. The contribution to the total scattering intensity arising from these objects was calculated according to

$$P(Q) = (1/V_{\rm p}) \int_{0}^{\infty} G(r_{\rm c}) F^{2}(Qr_{\rm c}) \, \mathrm{d}r_{\rm c}, \tag{6}$$

$$F(Qr_{\rm c}) = (4\pi/Q^3)(\rho_{\rm shell} - \rho_{\rm core}) \big\{ \rho_{\rm scaled} j[Qr_{\rm c} + (t/r_{\rm c})Qr_{\rm c}] - j(Qr_{\rm c}) \big\},\tag{7}$$

$$\rho_{\rm scaled} = (\rho_{\rm solv} - \rho_{\rm shell})(\rho_{\rm core} - \rho_{\rm shell}) \tag{8}$$

and

$$i(Qr_{\rm c}) = \sin(Qr_{\rm c}) - (Qr_{\rm c})\cos(Qr_{\rm c}), \qquad (9)$$

where $r_{\rm c}$ is the core radius, *t* is the shell thickness, $V_{\rm p}$ is the particle volume, and $\rho_{\rm core}$, $\rho_{\rm shell}$ and $\rho_{\rm solv}$ are the scattering length densities (SLDs) of the core, shell and solvent, respectively.

The function $G(r_c)$ is the normalized probability of finding a particle with a core radius between r_c and $r_c + dr_c$, and it accounts for the polydispersity of the cores according to a Schultz distribution (Hayter & Penfold, 1981; Hayter, 1983):

$$G(r_{\rm c}) = \frac{r_{\rm c}^Z}{\Gamma(Z+1)} \left(\frac{Z+1}{\langle r_{\rm c} \rangle}\right)^{Z+1} \exp\left[-\frac{r_{\rm c}}{r_{\rm avg}}(Z+1)\right], \quad (10)$$

where $\Gamma(Z + 1)$ is the gamma function and the parameter Z is related to the polydispersity σ_c of the core radius by the expression

$$\sigma_{\rm c} = \frac{\left(\left\langle r_{\rm c}^2 \right\rangle - \left\langle r_{\rm c} \right\rangle^2 \right)^{1/2}}{\left\langle r_{\rm c} \right\rangle} = \frac{1}{\left(Z+1\right)^{1/2}}.$$
 (11)

The interparticle structure factor S(Q) describes how the scattering intensity is modulated by interference effects between radiation scattered by different scattering objects. In our case, it should account for the aggregation of the magnetic nanoparticles, in analogy with the distribution of micelles along the polypeptide backbone. Therefore, we used the same expression derived by Chen and Teixeira,

$$S(Q) = 1 + \frac{D\Gamma(D-1)}{(Qr)^{D}} \sin[(D-1)\tan^{-1}(Q\xi)] \left(1 + \frac{1}{Q^{2}\xi^{2}}\right)^{(1-D)/2},$$
(12)

where *r* is the mean radius of the particles as resulting from the sum of the core radius r_c and the shell thickness *t*, Γ is the gamma function and ξ is the correlation length, *i.e.* a cut-off factor related to the dimensions of the aggregates that are eventually formed by the particles. *D* is the fractal dimension that describes the spatial distribution of the individual scatterers and it is related to their number N(R) within a sphere of radius *R* through

$$N(R) = (R/r)^{D}.$$
(13)

SANSPOL intensities of Fe_3O_4 , $CoFe_2O_4$ and $CuFe_2O_4$ are shown in Figs. 1, 2 and 3, respectively. The curves resulting from the fitting

obtained according to the modified pearl-necklace model are shown as full lines in the corresponding figures, while the parameters extracted from the analysis of the SANSPOL data are reported in Table 1. The fitting routine has been constrained to globally fit all the SANSPOL curves for each sample, *i.e.* the fitting parameters are the same for the SANSPOL intensities parallel and perpendicular (flipper on and off) to the magnetic field, except for the core scattering length density that changes as a function of the polarization of the neutrons and the angle between **Q** and **H**. This is summarized in equation (14), where the nuclear part of the core scattering length density is the same for all the SANSPOL intensities, while the magnetic contribution is null for the parallel direction and it has the same value for the two perpendicular curves:

$$\rho_{\rm core} = \rho_{\rm core}^{\rm nucl} \pm \rho_{\rm core}^{\rm mag}.$$
 (14)

Results of the fitting show that the nanoparticles comprise a magnetic core with a mean radius of about 40–50 Å and a polydispersity ranging from 0.3 to 0.5. In detail, the mean radii of the magnetic cores are very similar in the cases of Fe₃O₄ and CuFe₂O₄ (about 40 Å), while the value is slightly higher in the case of CoFe₂O₄ (about 50 Å). Moreover, the polydispersity value is very similar in the cases of Fe₃O₄ and CuFe₂O₄ (close to 0.5). The shell thickness is similar in all the samples, ranging from 6.7 to 8.0 Å.

The SANSPOL analysis shows that fractal aggregates are present in all the samples, with different fractal dimensions and correlation lengths. In Fe₃O₄ and CuFe₂O₄ the fractal dimension is quite close to one, accounting for almost linear aggregates, while the fractal dimension is about 1.6 in CoFe₂O₄. The correlation length values range from about 160 Å for the copper ferrite to 190 Å for the cobalt ferrite and 550 Å for the iron ferrite sample. It is important to note that the correlation length values are close to the higher limit of the instrumental size range. This is the main reason why the error values in their determination are quite high, indicating a low accuracy in the obtained correlation lengths.

4. Conclusions

This work reports the synthesis and the SANSPOL characterization of ferrofluids comprising ferrite nanoparticles coated by dodecanoic acid and dispersed in cyclohexane. Small-angle scattering of polarized neutrons takes advantage of the modification of the magnetic cross section and allows the determination of both magnetic and diamagnetic domains that could be present in nanostructured magnetic fluids. The results obtained from the pearl-necklace model show that the composition of the magnetic cores of the ferrite nanoparticles affects both the mean size of the particles and the particle size distribution. These, in turn, affect the formation of aggregates under an applied magnetic field, both in terms of fractal dimension and correlation lengths.

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