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**A method for setting the equi-inclination angle.** By D. SAYRE, *Johnson Foundation for Medical Physics, University of Pennsylvania, Philadelphia 4, Pennsylvania, U.S.A.*

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It sometimes happens that the equi-inclination angle  $\mu$  cannot be set precisely in advance, either because the lattice-level coordinate  $\zeta$  is not yet known accurately or because the instrument has fallen out of adjustment (see Buerger, 1942; the nomenclature in this note is the same as his). The most important consequence of mis-setting  $\mu$  is not, as is sometimes thought, that reflections will be lost (though this can happen) but that the Lorentz factor can be seriously affected, especially for near-in spots. This note describes a method for finding the correction  $d\mu$  to be applied to  $\mu$ . It takes only a few minutes, gives accurate results, and can be applied to any crystal whose symmetry is monoclinic or higher.

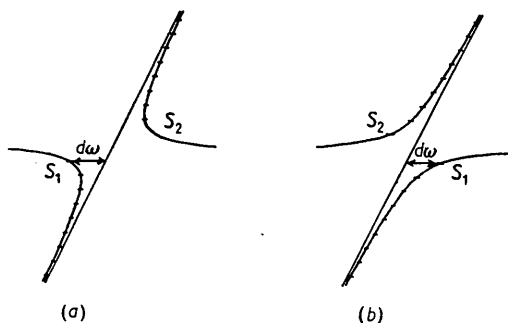


Fig. 1. Appearance of a central lattice line (a) when the  $\mu$  used was too small, and (b) when the  $\mu$  used was too large. Compare Buerger's Fig. 164.

An error in  $\mu$  will be revealed by the fact that a central lattice line (row of reciprocal-lattice points which passes through the rotation axis) appears on the photograph not as a straight line but as one of the forms shown in Fig. 1. What has happened is that each spot has been formed at

a moment when the rotation angle  $\omega$  differed by  $d\omega$  from what it should have been.

How is  $d\omega$  related to  $d\mu$ ? As shown in Fig. 2(a), when  $\mu$  is correctly set the reflecting circle for the net being photographed passes through the rotation axis, but when there is an error  $d\mu$  the rotation axis misses the circle by  $\zeta d\mu$ , passing inside the circle if  $\mu$  is too large and outside it if  $\mu$  is too small. Then, as is evident from Fig. 2(b),  $\xi d\omega = \zeta d\mu$ , or

$$d\mu = \frac{\xi}{\zeta} d\omega. \quad (1)$$

The method rests on this formula. A test Weissenberg is taken, which need be only wide enough to include such a pair of spots as  $S_1$  and  $S_2$  in Fig. 1, and exposed only long enough to make them visible. It is convenient to take this photograph twice on the same film, displaced horizontally by a few centimeters, to give an accurate horizontal. Two ten-minute exposures should be enough. The error  $d\omega$  is read with the aid of a sheet of transparent plastic scribed with a horizontal line and one inclined at an angle (for most cameras) of  $\tan^{-1} 2 = 63.4^\circ$ . Lastly,  $d\mu$  is calculated from (1); the sign of  $d\mu$  is obtained by reference to Fig. 1.

The method is applicable whenever there is a central lattice line. With a monoclinic crystal mounted on  $a$  or  $c$  this will be, say, the  $40l$ 's or the  $h03$ 's, respectively. A crystal of higher symmetry, or a monoclinic crystal mounted on  $b$ , will have many central lattice lines.

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#### Reference

BUERGER, M. J. (1942). *X-ray Crystallography*. New York: Wiley.

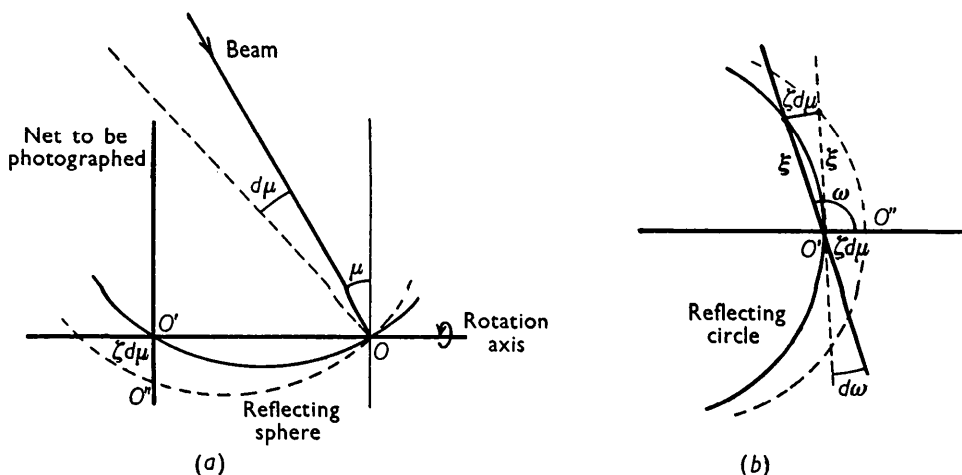


Fig. 2. (a) View from above, showing that the circle of reflection misses the rotation axis by  $\zeta d\mu$ . The circle of reflection is not explicitly shown here, because it is edge-on in this view, but its trace lies in the net to be photographed. (b) View down the rotation axis, showing that  $\xi d\omega = \zeta d\mu$ . Here the reflecting circle is explicitly shown. In both drawings the parts shown in broken lines refer to the case when  $\mu$  is mis-set. These drawings correspond to the lower and upper parts of Buerger's Fig. 139.