Lattice disorder in strongly correlated lanthanide and actinide intermetallics

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Lanthanide and actinide intermetallic compounds display a wide range of correlated-electron behavior, including ferromagnetism, antiferromagnetism, nonmagnetic (Kondo) ground states, and socalled 'non-Fermi liquid' (NFL) behavior. The interaction between felectrons and the conduction band is a dominant factor in determining the ground state of a given system. However, lattice disorder can create a distribution of interactions, generating unusual physical properties. These properties may include NFL behavior in many materials. In addition, lattice disorder can cause deviations from standard Kondo behavior that is less severe than NFL behavior. A review of the lattice disorder mechanism within a tight-binding model is presented, along with measurements of the YbBCu₄ and UPd_xCu_{5-x} systems, demonstrating the applicability of the model. These measurements indicate that while the YbBCu₄ system appears to be well ordered, both site interchange and continuous bond-length disorder occur in the UPd_rCu_{5-r} series. Nevertheless, the measured bond-length disorder in UPdCu₄ does not appear to be enough to explain the NFL properties simply with the Kondo disorder model.

Keywords: disordered materials; non-Fermi liquids; Kondo effect.

1. Introduction

Many heavy-fermion *f*-electron compounds exhibit magnetic and electronic properties which do not behave as expected from the Landau Fermi-liquid theory thought to be applicable to heavyfermion systems. When these anomalies include a certain subset of behavior, the materials are said to be non-Fermi liquids (NFL) (for a review, see Coleman *et al.*, 1996). These behaviors include logarithmic or weak power-law dependences of the Sommerfeld specific heat coefficient $\gamma(T) = C(T)/T$ and the magnetic susceptibility $\chi(T)$, and a deviation from T^2 of the temperature dependence of the electrical resistivity as $T \rightarrow 0$ K (typically linear). Most but not all NFL materials are known to be crystallographically or chemically disordered, but theoretical treatments differ with regard to whether or not this disorder is important to the NFL behavior (Millis, 1993; Bernal *et al.*, 1995).

One focus of research has been to find NFL behavior in well ordered materials. However, such materials are, by definition, stoichiometric and therefore the single-impurity Anderson model (SIAM) should no longer apply at some level. Unfortunately, the periodic Anderson model (PAM) that should apply to *f* ions on a periodic well ordered lattice has not been solved, although progress is being made (Tahvildar-Zadeh *et al.*, 1997). In any case, the search for well ordered NFL materials must necessarily include attempts to isolate coherence effects as would be described by the PAM from those effects that will require a truly new description of the ground state, such as quantum critical behavior (Millis, 1993).

Lattice disorder plays a pivotal role both in attempts to understand coherence effects in Anderson lattice systems and in the search for NFL mechanisms and materials. In Anderson lattice systems, lattice disorder is a potential mask of real coherence effects because it can create a distribution of behavior in a material that may be difficult to assign to the lattice disorder. In NFL studies, disorder can cause NFL behavior (Bernal et al., 1995; Miranda et al., 1997) and therefore can also be viewed as a mask to discovering well ordered NFL materials. Moreover, the role of disorder in generating NFL behavior is still an open question. Kondo disorder models, whereby a distribution of Kondo temperatures (T_K) extends to sufficiently low temperatures, have been shown to be capable of generating NFL behavior without including any essentially new physical mechanisms. Recently, Castro-Neto et al. (1998) proposed that the presence of sufficient disorder (lattice or otherwise) can drive a system into a Griffiths' phase, creating a distribution of quantum critical points. A Griffiths' phase has the potential of generating more universal behavior than the Kondo disorder model, and so may be a better candidate for NFL behavior in materials that are known to possess some lattice disorder.

Searching for lattice disorder can be a much more complicated and self-deceiving task than many researchers outside of crystallography realise. A common procedure in characterizing any material is to perform a powder diffraction measurement and to perform a Rietveld refinement of a proposed crystal structure at room temperature. If any lattice disorder is indicated by enhanced displacement parameters (u^2) , it is often ignored in this procedure because only a temperature-dependent measurement is capable of discerning between a large u^2 that is caused by significant weight in the phonon spectrum at low frequencies (i.e. a low Debye temperature for a given site) and one that is caused by static (i.e. non-phonon) disorder due to, for instance, off-center displacements or site-interchange between two atomic species within a given compound. Even if temperaturedependent diffraction data are collected, it can be difficult to identify the source of disorder if it is particularly pathological, as in a case where site-interchange occurs but insufficient contrast exists between the scattering factors for the two species of atoms [for example, see Chau et al. (1998) for the case of UPdCu₄].

X-ray absorption spectroscopy can be an excellent tool for identifying certain kinds of disorder when used in conjunction with diffraction results. Perhaps the most unique feature is the ability to probe uniquely the local atomic arrangement around a given species of atom with the X-ray absorption fine structure (XAFS) technique. With this measurement, one can distinguish between a given atomic species that is sitting on two distinct sites in a structure as long as those two sites have significant differences in their local atomic arrangement.

The remainder of this paper begins with a discussion of how disorder can affect magnetic susceptibility. Experimental XAFS data will be presented for two systems: the Anderson lattice YbBCu₄ system and the NFL UPd_xCu_{5-x} system. The possibility of *B*/Cu site interchange will be explored and temperature-dependent displacement parameters will be carefully considered in the search for any lattice disorder. Many of the details of the experimental analysis and the results are described elsewhere (Booth *et al.*, 1998; Lawrence *et al.*, 2001; Bauer *et al.*, 2001).

2. Lattice disorder in the single-impurity model

A hallmark of the SIAM is the pronounced maximum in the magnetic susceptibility that occurs for J > 1/2 as the Kondo singlet is formed at low temperatures. As one decreases temperatures from well above T_K , $\chi(T)$ increases following a typical Curie–Weiss form. This increase slows down near T_K and at approximately one-third of T_K , $\chi(T)$ begins to decrease, going to a constant at zero temperature that is inversely proportional to T_K . The relative size of the maximum in $\chi(T)$ to the zero-temperature constant $\chi(0)$ is only a function of the total angular moment J on the f ion, with the maximum $\chi(T)$ decreasing with decreasing J (Rajan, 1983).

Another way to decrease the relative size of the maximum is to include lattice disorder. Such disorder will produce a distribution $P(T_K)$ of Kondo temperatures. The susceptibility can be calculated with $P(T_K)$ and a Bethe-ansatz calculation of the susceptibility of a single Kondo impurity, $\chi(T, T_K)$ (Rajan, 1983):

$$\chi(T) = \int \chi(T, T_K) P(T_K) \,\mathrm{d}T_K. \tag{1}$$

 $P(T_K)$ is calculated by starting with the expession for T_K :

$$T_K = E_F \exp[-1/(\rho \mathfrak{F})], \qquad (2)$$

where E_F is the Fermi energy, ρ is the density of states at the Fermi level and \mathcal{J} is the conduction-electron/local-moment exchange energy. The coupling energy V_{tot} is related to the exchange energy in Kondo theory simply by $\mathcal{J} = V_{\text{tot}}^2 / \varepsilon_f$, where ε_f is the *f*-level energy. At this stage, we have described the generic Kondo disorder model put forth by Bernal *et al.* (1995). We now choose lattice disorder as the microscopic origin of the Kondo disorder. In order to include the lattice, we use a tight-binding approximation to obtain the contribution to the coupling energy of each pair of atoms *A* (*f* ion) and *B* (assuming *d* electrons in the conduction band):

$$V_{A,B} = (\eta_{fd} \hbar^2 / m_e) [(r_{Af}^5 r_{Bd}^3)^{1/2} / R_{A-B}^6],$$
(3)

where $r_{X\ell}$ is the radius of the electronic shell with angular momentum ℓ for atom X [tabulated by Straub & Harrison (1985)], and R is the bond length between the atoms with $\ell = f$ and d. The coefficient η_{fd} depends only on ℓ and the bond symmetry (see Appendix B of Harrison & Straub, 1987). We will assume that all bonds are σ bonds. The total hybridization energy is then $V_{\text{tot}} = \sum_{A,B\text{pairs}} V_{A,B}$. Within this tight-binding approach, calculated energies are often too high by a factor of two compared with experimental values (Harrison & Straub, 1987). However, we are only interested in relative trends because we choose other parameters (such as E_F and ρ) to account for this absolute error.

With this model as a framework, the connection between neighboring species is made through r_B and through the actual bond length with R_{A-B} . Therefore, bond-length disorder will create a distribution of $V_{A,B}$ values by replacing R_{A-B} with a distribution of bond lengths, and site interchange will create a distribution of $V_{A,B}$ values by varying r_B . An important difference between these two types of disorder is that bond-length disorder is defined to be continuous in this model (we will use a Gaussian distribution) and site-interchange is defined to be discrete: if one considers only the nearest neighbors in a calculation, there are only a finite number of possible combinations of the various $V_{A,B}$ terms.

Before we can demonstrate this model, we need to pick a system for which we can perform the sum over $V_{A,B}$. Consider the case of the C15b structure that is formed by some compounds of the form $ABCu_4$. All atoms sit on the cubic $\overline{4}3m$ face-centered cubic (f.c.c.) lattice, with A atoms sitting on the 4a site at (0,0,0), B atoms on the 4c sites at (1/4,1/4,1/4) and Cu atoms on 16e sites forming a cornershared tetrahedral network centered at (3/4,3/4,3/4). Band-structure calculations for the C15b material YbAgCu₄ indicate that the Cu and Ag *d* electrons make the main contributions to the conduction band (Monachesi & Continenza, 1996). Therefore, in the calculations that follow, we will sum over the 12 *A*-Cu nearest neighbors at ~2.93 Å and over the 4 *A*-*B* next-nearest neighbors at ~3.06 Å, as shown in Fig. 1(*a*). We also assume that E_F and ρ are fixed within a given compound and do not have their own distributions.

Fig. 2 shows how the addition of (continuous) bond-length disorder can affect the susceptibility within this Kondo disorder model. The effect on the actual width of the distribution is pronounced, with only ~ 0.01 Å of extra bond-length disorder necessary to produce a width of the $P(T_K)$ of ~40%. Surprisingly, this apparently large width of $P(T_K)$ has little effect on the calculated $\chi(T)$. In fact, lattice disorder continues to have little effect on $\chi(T)$ until one reaches a Debye-Waller width of $\sigma \simeq 0.04$ Å. At this point, a significant amount of weight in $P(T_K)$ exists at lower temperatures. A previous study of the Kondo disorder model (Bernal et al., 1995) has shown that if enough weight exists near 0 K, logarithmic divergences in the magnetic susceptibility and the heat capacity are generated. Moreover, it has been shown (Miranda et al., 1997) that a linear temperature dependence of the resistivity is also generated when enough low- T_K weight exists in $P(T_K)$. Therefore, one should appreciate how little intrinsic bond-length disorder is necessary to produce such a situation. Although such a distortion would be difficult to attain by applying external pressure, it is quite common to see changes in local bond lengths of this magnitude with chemical doping.



Figure 1

The local structure in the C15b crystal structure. Panel (a) shows the local structure around the f ion (atom A), but also represents the environment around atom B by switching all A and B atoms in the panel. Panel (b) shows the local structure around the Cu atoms. Bond lengths are for YbAgCu₄.

Another mechanism for creating a distribution of Kondo temperatures is site interchange, whereby two atomic species that nominally sit on distinct sites have a propensity to exchange sites. The ideas presented here are easily applied to off-stoichiometric samples where, for instance, in UPd_{0.5}Cu_{4.5} one can expect to find copper atoms on 4c sites, even in the nominal structure. The case we consider now is when in ABCu₄, some percentage of the B atoms interchange sites with copper atoms. In this case, a distribution of possible local environments around the f-ion sites is created. Consider the nominally ordered case shown in Fig. 1(a) with A as uranium and B as Pd, as in UPdCu₄. If each 4c site has a 25% probability of being Cu rather than Pd, then each 16e site has a 25/4 = 6.25% chance of being Pd rather than Cu (four times as many 16e sites). With these probabilities, a binomial distribution of possible environments can be calculated. Using values of E_F and ρ/ε_f from Booth *et al.* (1998), we can calculate a discrete distribution of Kondo temperatures, as shown in Fig. 3. As should be immediately appreciated, there is roughly equal weight for Kondo temperatures ranging from ~100 to 250 K with this degree of site interchange.

A material that exhibits site interchange can be thought of as a material that is chemically 'self-doped' in that ions with different atomic radii now sit on nominally the same sites. Such site interchange can also create a distribution of bond lengths, as discussed above. For instance, the atomic radius of Cu is ~1.57 Å, while that of Pd is ~1.79 Å. Therefore, local distortions of 0.2 Å may exist in the local environment around U atoms. Consequently, if site interchange exists, some level of bond-length disorder likely also exists. We have calculated the effect of bond-length disorder on the distribution of T_K values and display the results in Fig. 3(*b*). The calculations show that the discrete nature of the underlying distribution is quickly washed out by a bond-length disorder of only about 0.01 Å. This result attests to the overwhelming sensitivity of this model to bond-length disorder.

Again, significant weight is not generated in the low- T_K region until about 0.04 Å of disorder is included.

To summarize the results of this section, both continuous and discrete distributions of Kondo temperatures can be generated with various types of disorder. Truly discrete distributions seem unlikely, since even when the conditions necessary to create a discrete distribution exist, namely some kind of chemical substitution occurs, these substitutions will also generate some bond-length disorder, which will quickly overwhelm the discrete character of any $P(T_K)$. However, the width of a distribution created by chemical substitution can readily be quite large, thus enhancing the overall width when bond-length disorder is included.

3. Experimental examples

3.1. Experimental details

XAFS experiments were performed at the *B* edges for B = Tl, In, Cd and Ag in samples of YbBCu₄ and at the U L_{III} , Pd *K* and Cu *K* edges for members of the UPd_xCu_{5-x} series. Data were collected on BL 4-3 at the Stanford Synchrotron Radiation Laboratory (SSRL) using a half-tuned Si(220) double-crystal monochromator. Samples were ground, typically passed through a 30 µm sieve and brushed onto scotch tape to obtain a uniform thickness. Strips of tape were stacked to obtain an absorption jump at the various edges of less than unity. The YbBCu₄ samples are the same flux-grown crystals described by Sarrao *et al.* (1999). Preparation of the UPd_xCu_{5-x} samples is consistent with that described by Chau *et al.* (1998) and will be described elsewhere (Lawrence *et al.*, 2001). Samples with $1.0 \le x \le 1.5$ show NFL behavior both in resistivity and magnetic susceptibility measurements.



Figure 2

(a) The calculated distribution of Kondo temperatures assuming a Gaussian distribution of near-neighbor bond lengths in the C15b crystal structure of YbAgCu₄. Other input parameters, such as atomic species, E_F , and ρ/ε_f , were chosen to give $T_K = 150$ K. (b) The calculated $\chi(T)$ using the distributions in panel (a).



Figure 3

(a) The discrete distribution of T_K values based on 25% Pd/Cu site interchange in UPdCu₄. (b) The same distribution as in panel (a) convolved with the indicated amount of bond-length disorder.

3.2. Kondo coherence and YbBCu₄

In a recent paper, the properties of many members of the YbBCu₄ series were compared (Sarrao *et al.*, 1999). Kondo temperatures range from ~60 K for YbZnCu₄ to ~750 K for YbTlCu₄. Although many properties of these materials can be explained with the SIAM, $\chi_{max}/\chi(0)$ was significantly less than predicted by the SIAM for YbZnCu₄, YbCdCu₄ and YbMgCu₄. The possibility that crystal fields were responsible for this disagreement has been ruled out by recent inelastic neutron scattering measurements (Lawrence *et al.*, 2001). As is clear from Fig. 2, the reduction in $\chi_{max}/\chi(0)$ could very easily be caused by lattice disorder. If this final possibility is ruled out, then coherence effects can be seriously taken as a possible explanation, opening the door for comparisons with PAM theories.

Since the Yb $L_{\rm III}$ and Cu K edges nearly overlap, we restrict this study to the XAFS from the B atoms. We searched for two kinds of disorder: B/Cu site interchange, as indicated by the presence of a short B-Cu bond (see Fig. 1b), and any other disorder by measuring the temperature dependence of the B-Cu and B-Yb Debye-Waller factors and comparing the measurements with the correlated-Debye model (Crozier *et al.*, 1988).

The XAFS technique is very well suited for searching for *B*/Cu site interchange in these compounds because the nominal local environment around the *B* (4c) sites is very different than around the Cu (16*e* sites). As shown in Fig. 1, the nearest neighbors around the 4*c* (*B*) sites are 12 Cu atoms at ~2.9 Å, followed by 4 Yb atoms at ~3.06 Å. This environment differs from the 16*e* sites, which have 6 Cu neighbors at ~2.5 Å. Our task is therefore reduced to looking for a peak in the XAFS spectrum corresponding to a *B*-Cu neighbor at ~2.5 Å, which is ~0.4 Å shorter than in the nominal structure.



Figure 4

The Fourier transform (FT) of $k^3 \chi(k)$ for (a) YbAgCu₄ and (b) YbCdCu₄. The outer envelope represents \pm the amplitude and the oscillatory line within the envelope is the real part of the complex transform. These transforms are from 2.5 to 15 Å⁻¹ and are Gaussian narrowed by 0.3 Å⁻¹. Fits are from 2.0 to 3.2 Å.

Details of the data reduction methods can be found elsewhere (Lawrence *et al.*, 2001). The data are presented and fitted in *r* space. Fig. 4 shows data for YbCdCu₄ and YbAgCu₄, using only scattering paths corresponding to the nominal structure; that is, site interchange was not included. The quality of the fit is very high. When some B/Cu site interchange is included in the fit, the fit quality does not improve significantly and we place an upper limit of 5% of the B atoms possibly sitting on 16*e* sites.

With site interchange removed as a potential source of disorder, we choose the nominal crystal structure for our fitting model. Data were collected at various temperatures between 20 and 300 K. The variances of the B-Cu and B-Yb bond-length distributions are shown in Fig. 5. The variance results were then fit to the following equation:

$$\sigma_{\rm fit}^2(T) = \sigma_{\rm stat}^2 + F(T, \Theta_{\rm cD}), \tag{4}$$

where σ_{stat}^2 is a temperature-independent offset due to positional disorder and $F(T, \Theta_{cD})$ is given by the correlated-Debye model, with Θ_{cD} as the correlated-Debye temperature. The fits shown in Fig. 5 use $\Theta_{cD} \simeq 250$ K for all pairs, and a maximum level of σ_{stat}^2 of <0.001 Å² was obtained. The estimated error of this measurement of σ_{stat}^2 is 0.0005 Å², so all of these measurements are generally consistent with no lattice disorder.

3.3. Disorder models and NFL behavior in $UPd_{x}Cu_{5-x}$

Our previous study (Booth *et al.*, 1998) of UPdCu₄ found that \sim 25% of Pd atoms sit on nominally Cu sites. As shown in Figs. 2 and 3, this level of site interchange will have a large effect on the measured magnetic susceptibility. Therefore, the disorder must be accounted for in any theory of the magnetic susceptibility in these materials. By including \sim 0.05 Å of additional bond-length disorder,



Figure 5

The measured variance (σ^2) of the bond-length distribution for the *B*-Cu pairs at ~2.93 Å and the *B*-Yb pairs at ~3.06 Å for *B* = Tl, In, Cd and Ag. The fits are to a correlated-Debye model, as described in the text.

the magnetic susceptibility could be reasonably reproduced by the model in §2. The addition of this extra disorder was necessary to obtain enough weight in the $P(T_K)$ distribution near 0 K to generate the NFL behavior. However, it is also possible to create a collection of 0 K quantum critical points with sufficient disorder. Such a phase is called a Griffiths' phase. Within the Griffiths' phase model, a range in phase space is created that might be called a 'critical line' at 0 K. In UPd_xCu_{5-x} , this line would extend from $x \simeq 1.0$ to x > 1.5. At the present time, it is difficult to compare the Kondo disorder and Griffiths' phase models directly because there is no Griffiths' phase calculation starting from a measured amount of lattice disorder and arriving at a magnetic susceptibility. In any case, we expect that less disorder is necessary in a Griffiths' phase model than in a Kondo disorder model. It is therefore very important to test whether the assumed addition of ~ 0.05 Å of bond-length disorder can be verified by experiment.

Such a verification requires a study of many members of the UPd_xCu_{5-x} series in order better to determine certain factors such as the site interchange and amplitude reduction factors (S_0^2) . We have performed XAFS measurements of samples with various x and have successfully isolated the Debye–Waller factors for the U–Cu nearest-neighbor peaks. These fits are complex because the site interchange must be known (as measured from the Pd-edge data) and then applied to the U-edge fits so that the number of U–Pd(16e) pairs underneath the main U–Cu(16e) peak can be properly accounted for. In each case, the Cu-edge fits were used as a cross check. These data were collected as a function of temperature and the same analysis as described in §3.2 was applied. The results are summarized in Fig. 6.

Interestingly, although some residual static disorder is measured (especially for x = 1), the measured level of disorder is less than that required for this Kondo disorder model for all *x*. Further details will be given in a future article (Bauer *et al.*, 2001).

4. Discussion and conclusions

We have tried to demonstrate the significance of lattice disorder in *f*-electron systems, both as a potential source of 'uncharacteristic'



Figure 6

The bond-length distribution variance for the U–Cu pairs at ~2.93 Å as a function of x in UPd_xCu_{5-x}. The 'cold' results are for the lowest temperature collected for that value of x, between 4 and 20 K. σ_{static}^2 was determined by fits of the temperature-dependent data to the correlated-Debye model, as described in the text. The hatched area shows the approximate amount of disorder necessary for lattice disorder to explain fully NFL behavior in the x = 1.0 and 1.5 compounds based on the Kondo disorder model.

behavior in the temperature dependence of materials that otherwise obey a single impurity model, and in systems where the lowtemperature properties are not well described by any model, namely the non-Fermi liquids. The problem of identifying gross disorder and applying knowledge of this disorder is relatively straightforward when the tight-binding approximation is employed, but it is nevertheless important to recognize certain distinctions. For instance, although a small amount of lattice disorder can produce a very wide distribution of T_K values, such a distribution can still produce a magnetic susceptibility consistent with no disorder. However, if enough disorder exists such that weight at low T_K values develops, large effects in the magnetic susceptibility can be expected, possibly even NFL behavior.

Applying these concepts to the YbBCu₄ series, we find that lattice disorder is likely not the cause of deviations from the SIAM. We now believe that no other explanation exists for these deviations other than collective effects that are only possible in a lattice of f ions, that is, some form of the PAM is necessary to describe the deviations from the SIAM. We note that other behavior is consistent with a slower-than-expected crossover from the low-temperature Fermi liquid state to the high-temperature local moment state (Lawrence *et al.*, 2001). This result likely corresponds to the 'protracted screening' recently predicted for the Anderson lattice (Tahvildar-Zadeh *et al.*, 1997).

Our previous measurements of UPdCu₄ demonstrated the importance of accounting for Pd/Cu site interchange in understanding the magnetic and electronic properties. However, a closer look at the U— Cu bond-length disorder indicates that there does not appear to be enough for a simple Kondo disorder model to apply, opening the door to other theories that include disorder, such as the Griffiths' phase.

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