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## Redetermination of tricalcium trilanthanum pentakis(orthoborate) from single-crystal data

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Received 30 April 2008; accepted 15 May 2008
Key indicators: single-crystal X-ray study; $T=293 \mathrm{~K}$; mean $\sigma(\mathrm{La}-\mathrm{B})=0.004 \AA$; $R$ factor $=0.012 ; w R$ factor $=0.031$; data-to-parameter ratio $=10.1$.

Single crystals of the title compound, $\mathrm{Ca}_{3} \mathrm{La}_{3}\left(\mathrm{BO}_{3}\right)_{5}$, were obtained by spontaneous nucleation from a high-temperature melt. The crystal structure of $\mathrm{Ca}_{3} \mathrm{La}_{3}\left(\mathrm{BO}_{3}\right)_{5}$ has been determined previously from X-ray powder data [Zhang, Liang, Chen, He \& Xu (2001). J. Alloys Compd, 327, 96-99]. The present refinement shows a significant improvement in terms of the precision of the geometric parameters and the correct determination of the absolute configuration in space group $P 6_{3} m c$ with all atoms refined with anisotropic displacement parameters. The structure consists of isolated $\mathrm{BO}_{3}$ triangles and distorted $\left[\mathrm{CaO}_{8}\right]$ and $\left[\mathrm{LaO}_{10}\right]$ polyhedra. Except for one O atom, all other atoms are situated on special positions: La, all O and one B atom on mirror planes, and two $B$ atoms with site symmetry $3 m$.

## Related literature

For phase equilibria in the system $\mathrm{La}_{2} \mathrm{O}_{3}-\mathrm{CaO}-\mathrm{B}_{2} \mathrm{O}_{3}$, see: Zhang et al. (2001a). For a previous structure analysis of $\mathrm{Ca}_{3} \mathrm{La}_{3}\left(\mathrm{BO}_{3}\right)_{5}$ based on X-ray powder diffraction data, see: Zhang et al. (2001b). For non-linear optical (NLO) applications of borate crystals containing triangular $\mathrm{BO}_{3}$ anions, see: Chen et al. (1999). For a review of the geometry of the $\mathrm{BO}_{3}$ group, see: Zobetz (1982). For the potential applications of $\mathrm{Ca}_{3} \mathrm{La}_{3}\left(\mathrm{BO}_{3}\right)_{5}$ for photoluminescence, see: Zhang et al. (2005); Han et al. (2007).

## Experimental

## Crystal data

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\(\mathrm{Ca}_{3} \mathrm{La}_{3}\left(\mathrm{BO}_{3}\right)_{5}\)
\(M_{r}=831.02\)
Hexagonal, \(P 6_{3} m c\)
\(a=10.530\) (3) A
\(c=6.398\) (2) \(\AA\)
\(V=614.4(3) \AA^{3}\)
```


## Data collection

Rigaku Mercury CCD
diffractometer
Absorption correction: multi-scan (CrystalClear; Rigaku, 2000)
$T_{\text {min }}=0.206, T_{\text {max }}=0.304$
4065 measured reflections 534 independent reflections 534 reflections with $I>2 \sigma(I)$ $R_{\text {int }}=0.035$

## Refinement

$R\left[F^{2}>2 \sigma\left(F^{2}\right)\right]=0.012$
$w R\left(F^{2}\right)=0.030$
$S=0.89$
534 reflections
53 parameters
1 restraint
$\Delta \rho_{\text {max }}=0.41 \mathrm{e} \AA^{-3}$
$\Delta \rho_{\text {min }}=-0.59 \mathrm{e}^{-3}$
Absolute structure: Flack (1983),
236 Friedel pairs
Flack parameter: -0.03 (3)

## Table 1

Selected geometric parameters ( $\left(\mathrm{A},{ }^{\circ}\right)$.

| $\mathrm{Ca} 1-\mathrm{O} 4^{\mathrm{i}}$ | $2.3139(13)$ | $\mathrm{La} 1-\mathrm{O} 3^{\text {vii }}$ | $2.8112(8)$ |
| :--- | :--- | :--- | :--- |
| $\mathrm{Ca} 1-\mathrm{O} 1^{\mathrm{ii}}$ | $2.376(3)$ | $\mathrm{B} 1-\mathrm{O} 4$ | $1.358(6)$ |
| $\mathrm{Ca} 1-\mathrm{O} 3$ | $2.382(4)$ | $\mathrm{B} 1-\mathrm{O} 1^{\mathrm{i}}$ | $1.384(3)$ |
| $\mathrm{Ca} 1-\mathrm{O} 1^{\mathrm{iii}}$ | $2.662(3)$ | $\mathrm{B} 2-\mathrm{O} 2^{\text {viii }}$ | $1.374(3)$ |
| $\mathrm{La} 1-\mathrm{O} 1^{\text {iv }}$ | $2.501(2)$ | $\mathrm{B} 3-\mathrm{O} 3$ | $1.389(3)$ |
| $\mathrm{La} 1-\mathrm{O} 4^{\mathrm{v}}$ | $2.516(4)$ |  |  |
| $\mathrm{La} 1-\mathrm{O} 2^{\text {vi }}$ | $2.6639(15)$ |  |  |
| $\mathrm{O} 4-\mathrm{B} 1-\mathrm{O}^{\mathrm{i}}$ | $119.7(2)$ | $\mathrm{O}^{\text {viii }}-\mathrm{B} 2-\mathrm{O} 2^{\mathrm{xi}}$ | 120 |
| $\mathrm{O}^{\mathrm{i}}-\mathrm{B} 1-\mathrm{O}^{\mathrm{x}}$ | $120.6(4)$ | $\mathrm{O}^{\mathrm{ix}}-\mathrm{B} 3-\mathrm{O} 3$ | 120 |

Symmetry codes: (i) $-y+1, x-y+1, z$; (ii) $x-y+1, x, z+\frac{1}{2}$; (iii) $-x+y,-x+1, z$; (iv) $y-1, x, z-\frac{1}{2}$; (v) $x, y, z-1$; (vi) $x-y+1, x+1, z-\frac{1}{2}$; (vii) $x-y, x, z-\frac{1}{2}$; (viii) $y-1,-x+y-1, z-\frac{1}{2} ; \quad$ (ix) $\quad-x+y+1,-x+1, z ; \quad$ (x) $\quad-x+y, y, z$; (xi) $x-y+1, x, z-\frac{1}{2}$.

Data collection: CrystalClear (Rigaku, 2000); cell refinement: CrystalClear; data reduction: CrystalClear; program(s) used to solve structure: SHELXS97 (Sheldrick, 2008); program(s) used to refine structure: SHELXL97 (Sheldrick, 2008); molecular graphics: DIAMOND (Brandenburg, 2004); software used to prepare material for publication: enCIFer (Allen et al., 2004).

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: WM2179).

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## supporting information

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# Redetermination of tricalcium trilanthanum pentakis(orthoborate) from singlecrystal data 

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## S1. Comment

Borate crystals containing parallel aligned $\mathrm{BO}_{3}$ anions are predicted to have large nonlinear optical (NLO) coefficients, moderate birefringence and wide transparency in the UV-region. Therefore they are considered to be good candidates for NLO applications (Chen, 1999). The title compound $\mathrm{Ca}_{3} \mathrm{La}_{3}\left(\mathrm{BO}_{3}\right)_{5}$, (I), has been investigated previously by Zhang et al. (2001a) during analysis of phase equilibria in the system $\mathrm{La}_{2} \mathrm{O}_{3}-\mathrm{CaO}-\mathrm{B}_{2} \mathrm{O}_{3}$, and NLO and luminescent properties of this material have also been reported (Zhang, 2005; Han, 2007). The crystal structure of $\mathrm{Ca}_{3} \mathrm{La}_{3}\left(\mathrm{BO}_{3}\right)_{5}$ was originally determined from X-ray powder diffraction data in conjunction with IR spectroscopy (Zhang et al., 2001b).
The structure of compound (I) can be described in terms of $\mathrm{BO}_{3}$ triangles and complex irregular [ $\mathrm{CaO}_{8}$ ] and $\left[\mathrm{LaO}_{10}\right]$ polyhedra. Each of the three crystallographically different B atoms is coordinated to three O atoms to form planar $\mathrm{BO}_{3}$ triangles. The B-O bond lengths range from 1.384 (3) to 1.389 (3) $\AA$, which is in good agreement with the results of geometric studies of the $\mathrm{BO}_{3}$ unit (Zobetz, 1982). Two of the three $\mathrm{BO}_{3}$ groups exhibit $3 m$ symmetry, and the third $\mathrm{BO}_{3}$ group has $m$ symmetry with $\mathrm{O}-\mathrm{B}-\mathrm{O}$ angles very close to $120^{\circ}$. The $\mathrm{La}^{3+}$ cations are 10 -fold coordinated by oxygen atoms with $\mathrm{La}-\mathrm{O}$ bond lengths ranging from 2.501 (2) to 2.812 (2) $\AA$. The $\left[\mathrm{LaO}_{10}\right]$ polyhedra are connected to each other and to the borate groups by sharing corners and edges forming a three-dimensional network with channels running parallel to [001]. In these channels the $\mathrm{Ca}^{2+}$ cations are situated and are surrounded by eight oxygen atoms with $\mathrm{Ca}-\mathrm{O}$ bond lengths ranging from 2.3139 (13) to 2.662 (3) $\AA$ (Table 1).

## S2. Experimental

Single crystals of compound (I) were grown using a $\mathrm{LiBO}_{2}$-containing flux. The composition of the mixture for crystal growth was 1:1:4:3 of $\mathrm{CaCO}_{3}$ (Sinopharm Regent, AR ), $\mathrm{La}_{2} \mathrm{O}_{3}$ (Materials, 99.8\%), $\mathrm{H}_{3} \mathrm{BO}_{3}$ (Sinopharm Regent, 99.99\%), and $\mathrm{Li}_{2} \mathrm{CO}_{3}$ (Sinopharm Reagent, AR). The mixture was heated in a platinum crucible to 1373 K , held at this temperature for several hours, and then cooled at a rate of $10 \mathrm{~K} / \mathrm{h}$ from 1373 to 873 K . The remaining solified flux attached to the crystals was readily dissolved in water. Crystals with an average size of 0.5 mm and mostly rod shaped habit were obtained.

## S3. Refinement

The present study confirms the basic structural features determined from the previous investigation by Zhang et al. (2001b) with a much higher precesion and with all displacement parameters refined anisotropically.


## Figure 1

The structure of (I) in a projection approximatly along the [001] direction with displacement ellipsoids drawn at the $85 \%$ probability level.


Figure 2
Packing diagram of the structure of $(\mathrm{I}) .\left[\mathrm{CaO}_{8}\right]$ polyhedra are yellow, $\left[\mathrm{LaO}_{10}\right]$ polyhedra are blue and $\left[\mathrm{BO}_{3}\right]$ units are green.

## tricalcium trilanthanum pentakis(orthoborate)

## Crystal data

$\mathrm{Ca}_{3} \mathrm{La}_{3}\left(\mathrm{BO}_{3}\right)_{5}$
$M_{r}=831.02$
Hexagonal, $P 6_{3} m c$
Hall symbol: P 6c - 2 c
$a=10.530$ (3) $\AA$
$c=6.398(2) \AA$
$V=614.4(3) \AA^{3}$
$Z=2$
$F(000)=752$

## Data collection

Rigaku Mercury CCD
diffractometer
Radiation source: Sealed Tube
Graphite Monochromator monochromator
Detector resolution: 14.6306 pixels $\mathrm{mm}^{-1}$
CCD_Profile_fitting scans
Absorption correction: multi-scan
(CrystalClear; Rigaku, 2000)
$T_{\text {min }}=0.206, T_{\text {max }}=0.304$

## Refinement

Refinement on $F^{2}$
Least-squares matrix: full
$R\left[F^{2}>2 \sigma\left(F^{2}\right)\right]=0.012$
$w R\left(F^{2}\right)=0.030$
$S=0.89$
534 reflections
53 parameters
1 restraint
Primary atom site location: structure-invariant direct methods
Secondary atom site location: difference Fourier map
$D_{\mathrm{x}}=4.492 \mathrm{Mg} \mathrm{m}^{-3}$
Mo $K \alpha$ radiation, $\lambda=0.71073 \AA$
Cell parameters from 1909 reflections
$\theta=2.2-27.5^{\circ}$
$\mu=11.59 \mathrm{~mm}^{-1}$
$T=293 \mathrm{~K}$
Rod, colourless
$0.22 \times 0.12 \times 0.10 \mathrm{~mm}$

4065 measured reflections
534 independent reflections
534 reflections with $I>2 \sigma(I)$
$R_{\text {int }}=0.035$
$\theta_{\text {max }}=27.5^{\circ}, \theta_{\text {min }}=2.2^{\circ}$
$h=-13 \rightarrow 13$
$k=-13 \rightarrow 13$
$l=-8 \rightarrow 7$

$$
\begin{aligned}
& w=1 /\left[\sigma^{2}\left(F_{\mathrm{o}}^{2}\right)+(0.02 P)^{2}+1.5843 P\right] \\
& \text { where } P=\left(F_{\mathrm{o}}^{2}+2 F_{\mathrm{c}}^{2}\right) / 3 \\
& (\Delta / \sigma)_{\max }<0.001 \\
& \Delta \rho_{\max }=0.41 \mathrm{e} \AA^{-3} \\
& \Delta \rho_{\min }=-0.59 \mathrm{e}^{-3}
\end{aligned}
$$

Extinction correction: SHELXL97 (Sheldrick, 2008), $\mathrm{Fc}^{*}=\mathrm{kFc}\left[1+0.001 \mathrm{xFc}^{2} \lambda^{3} / \sin (2 \theta)\right]^{-1 / 4}$

Extinction coefficient: 0.0632 (12)
Absolute structure: Flack (1983), 236 Friedel pairs
Absolute structure parameter: -0.03 (3)

## Special details

Geometry. All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.
Refinement. Refinement of $F^{2}$ against ALL reflections. The weighted $R$-factor $w R$ and goodness of fit $S$ are based on $F^{2}$, conventional $R$-factors $R$ are based on $F$, with $F$ set to zero for negative $F^{2}$. The threshold expression of $F^{2}>\sigma\left(F^{2}\right)$ is used only for calculating $R$-factors $(\mathrm{gt})$ etc. and is not relevant to the choice of reflections for refinement. $R$-factors based on $F^{2}$ are statistically about twice as large as those based on $F$, and $R$ - factors based on ALL data will be even larger.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters ( $\hat{A}^{2}$ )

|  | $x$ | $y$ | $z$ | $U_{\text {iso }} * / U_{\mathrm{eq}}$ |
| :--- | :--- | :--- | :--- | :--- |
| Ca1 | $0.47334(5)$ | $0.52666(5)$ | $0.76261(15)$ | $0.00673(19)$ |
| La1 | $0.156065(12)$ | $0.843935(12)$ | $0.08229(8)$ | $0.00493(11)$ |
| B1 | $0.1989(3)$ | $0.8011(3)$ | $0.5473(8)$ | $0.0049(10)$ |


| B2 | 0 | 0 | $0.2435(15)$ | $0.0086(17)$ |
| :--- | :--- | :--- | :--- | :--- |
| B3 | 0.6667 | 0.3333 | $0.598(3)$ | $0.0092(19)$ |
| O1 | $0.6272(3)$ | $0.9278(2)$ | $0.4462(4)$ | $0.0067(5)$ |
| O2 | $0.07534(16)$ | $0.92466(16)$ | $0.7399(6)$ | $0.0097(7)$ |
| O3 | $0.59052(16)$ | $0.40948(16)$ | $0.5984(8)$ | $0.0083(6)$ |
| O4 | $0.22657(17)$ | $0.77343(17)$ | $0.7443(5)$ | $0.0066(6)$ |

Atomic displacement parameters $\left(\AA^{2}\right)$

|  | $U^{11}$ | $U^{22}$ | $U^{33}$ | $U^{12}$ | $U^{13}$ | $U^{23}$ |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| Ca1 | $0.0060(3)$ | $0.0060(3)$ | $0.0073(4)$ | $0.0023(3)$ | $-0.0001(2)$ | $0.0001(2)$ |
| La1 | $0.00442(12)$ | $0.00442(12)$ | $0.00474(14)$ | $0.00129(9)$ | $0.00003(8)$ | $-0.00003(8)$ |
| B1 | $0.0052(15)$ | $0.0052(15)$ | $0.007(3)$ | $0.0044(18)$ | $-0.0006(10)$ | $0.0006(10)$ |
| B2 | $0.011(3)$ | $0.011(3)$ | $0.003(4)$ | $0.0057(13)$ | 0 | 0 |
| B3 | $0.009(2)$ | $0.009(2)$ | $0.009(6)$ | $0.0046(11)$ | 0 | 0 |
| O1 | $0.0069(10)$ | $0.0056(10)$ | $0.0073(11)$ | $0.0029(9)$ | $-0.0014(10)$ | $0.0016(9)$ |
| O2 | $0.0090(12)$ | $0.0090(12)$ | $0.0124(16)$ | $0.0055(14)$ | $-0.0005(7)$ | $0.0005(7)$ |
| O3 | $0.0101(10)$ | $0.0101(10)$ | $0.0067(17)$ | $0.0065(11)$ | $0.0005(9)$ | $-0.0005(9)$ |
| O4 | $0.0067(11)$ | $0.0067(11)$ | $0.0055(16)$ | $0.0026(13)$ | $-0.0014(7)$ | $0.0014(7)$ |

Geometric parameters ( $A,{ }^{\circ}$ )

| $\mathrm{Ca} 1-\mathrm{O} 4^{\mathrm{i}}$ | 2.3139 (13) | $\mathrm{La} 1-\mathrm{Ol}^{\text {i }}$ | 2.678 (3) |
| :---: | :---: | :---: | :---: |
| $\mathrm{Ca} 1-\mathrm{O} 4{ }^{\text {ii }}$ | 2.3139 (13) | La1-O3 ${ }^{\text {xiv }}$ | 2.8112 (8) |
| $\mathrm{Cal}-\mathrm{Ol}^{\text {iii }}$ | 2.376 (3) | La1-O3 ${ }^{\text {xv }}$ | 2.8112 (8) |
| $\mathrm{Ca}-\mathrm{Ol}^{\text {iv }}$ | 2.376 (3) | La1-B2 ${ }^{\text {xvi }}$ | 3.028 (3) |
| $\mathrm{Ca1}-\mathrm{O} 3$ | 2.382 (4) | La1-B1 | 3.076 (5) |
| $\mathrm{Ca} 1-\mathrm{O}^{\text {v }}$ | 2.444 (5) | B1-O4 | 1.358 (6) |
| $\mathrm{Ca} 1-\mathrm{Ol}^{\text {ii }}$ | 2.662 (3) | $\mathrm{B} 1-\mathrm{O} 1^{\mathrm{i}}$ | 1.384 (3) |
| $\mathrm{Cal}-\mathrm{Ol}^{\text {vi }}$ | 2.662 (3) | $\mathrm{B} 1-\mathrm{O} 1^{\text {xiii }}$ | 1.384 (3) |
| Cal-B1 ${ }^{\text {i }}$ | 2.858 (4) | $\mathrm{B} 1-\mathrm{Ca} 1^{\text {i }}$ | 2.858 (4) |
| $\mathrm{Ca} 1-\mathrm{B} 1^{\text {ii }}$ | 2.858 (4) | $\mathrm{B} 1-\mathrm{Ca} 1^{\text {ii }}$ | 2.858 (4) |
| $\mathrm{Ca} 1-\mathrm{Ca} 1^{v}$ | 3.3435 (11) | $\mathrm{B} 2-\mathrm{O} 2^{\text {xvii }}$ | 1.374 (3) |
| $\mathrm{Ca} 1-\mathrm{Ca} 1^{\text {vii }}$ | 3.3435 (11) | $\mathrm{B} 2-\mathrm{O} 2^{\text {xvii }}$ | 1.374 (3) |
| La1-O1 ${ }^{\text {viii }}$ | 2.501 (2) | $\mathrm{B} 2-\mathrm{O} 2^{\text {xix }}$ | 1.374 (3) |
| Lal-O1 ${ }^{\text {ix }}$ | 2.501 (2) | B2-La ${ }^{\text {xx }}$ | 3.028 (3) |
| $\mathrm{La} 1-\mathrm{O} 4^{\text {x }}$ | 2.516 (4) | B2- $\mathrm{La} 1^{\text {i }}$ | 3.028 (3) |
| $\mathrm{La} 1-\mathrm{O} 2^{\text {x }}$ | 2.639 (3) | B2-La1 ${ }^{\text {xi }}$ | 3.028 (3) |
| $\mathrm{La} 1-\mathrm{O} 2^{\text {xi }}$ | 2.6639 (15) | B3-O3 ${ }^{\text {xxii }}$ | 1.389 (3) |
| $\mathrm{La}-\mathrm{O} 2^{\text {xii }}$ | 2.6639 (15) | B3-O3xxiii | 1.389 (3) |
| $\mathrm{La} 1-\mathrm{O} 1^{\text {xiii }}$ | 2.678 (3) | B3-O3 | 1.389 (3) |
| $\mathrm{O} 4-\mathrm{Ca} 1-\mathrm{O} 4^{\text {ii }}$ | 93.58 (15) | $\mathrm{O} 1^{\mathrm{ix}}$ - $\mathrm{La} 1-\mathrm{O} 3^{\text {xiv }}$ | 116.83 (10) |
| $\mathrm{O} 4-\mathrm{Ca} 1-\mathrm{O} 1^{\text {iii }}$ | 151.80 (11) | O4 ${ }^{\text {x }} \mathrm{La} 1-\mathrm{O}^{\text {xiv }}$ | 64.52 (12) |
| $\mathrm{O} 4{ }^{\text {ii }}-\mathrm{Ca} 1-\mathrm{O} 1^{\text {iii }}$ | 80.01 (9) | $\mathrm{O} 2^{\mathrm{x}}-\mathrm{La} 1-\mathrm{O}^{\text {xiv }}$ | 122.29 (12) |
| $\mathrm{O} 4-\mathrm{Ca} 1-\mathrm{O}^{\text {iv }}$ | 80.01 (9) | $\mathrm{O} 2{ }^{\text {xi }}$-La1-O3 ${ }^{\text {xiv }}$ | 155.42 (13) |
| $\mathrm{O} 4{ }^{\mathrm{ii}}-\mathrm{Ca} 1-\mathrm{O}^{\text {iv }}$ | 151.80 (11) | $\mathrm{O} 2{ }^{\text {xii }}$ - $\mathrm{La} 1-\mathrm{O} 3^{\text {xiv }}$ | 121.81 (10) |
| $\mathrm{O} 1^{\text {iii }}-\mathrm{Ca} 1-\mathrm{O} 1^{\text {iv }}$ | 92.72 (12) | O1 ${ }^{\text {xiii }}$-La1-O3 ${ }^{\text {xiv }}$ | 88.50 (10) |


| $\mathrm{O} 4-\mathrm{Cal}-\mathrm{O} 3$ | 126.18 (10) |
| :---: | :---: |
| $\mathrm{O} 4{ }^{\text {ii }}-\mathrm{Ca} 1-\mathrm{O} 3$ | 126.18 (10) |
| O1iii-Ca1-O3 | 77.64 (10) |
| $\mathrm{O} 1{ }^{\text {iv }}-\mathrm{Ca} 1-\mathrm{O} 3$ | 77.64 (10) |
| $\mathrm{O} 4{ }^{\mathrm{i}}-\mathrm{Ca} 1-\mathrm{O}^{\text {v }}$ | 73.69 (10) |
| $\mathrm{O} 4{ }^{\text {ii }}-\mathrm{Ca} 1-\mathrm{O}^{v}$ | 73.69 (10) |
| $\mathrm{O} 1^{\text {iii }}-\mathrm{Ca} 1-\mathrm{O}^{\text {v }}$ | 78.17 (9) |
| $\mathrm{O} 1^{\text {iv }}-\mathrm{Ca} 1-\mathrm{O}^{\text {v }}$ | 78.17 (9) |
| $\mathrm{O} 3-\mathrm{Ca} 1-\mathrm{O}^{\text {v }}$ | 144.65 (19) |
| $\mathrm{O} 4{ }^{\text {i }}-\mathrm{Ca} 1-\mathrm{O} 1^{\text {ii }}$ | 56.39 (9) |
| $\mathrm{O} 4{ }^{\text {ii }}-\mathrm{Ca} 1-\mathrm{O} 1^{\text {ii }}$ | 112.85 (10) |
| $\mathrm{O}{ }^{\text {iii }}-\mathrm{Ca} 1-\mathrm{O} 1^{\text {ii }}$ | 151.00 (8) |
| $\mathrm{O}{ }^{12}-\mathrm{Ca}-\mathrm{O} 1^{\text {ii }}$ | 86.53 (8) |
| $\mathrm{O} 3-\mathrm{Ca} 1-\mathrm{O}^{1 i}$ | 73.88 (10) |
| $\mathrm{O} 3^{v}-\mathrm{Ca} 1-\mathrm{O} 1^{\text {ii }}$ | 129.62 (7) |
| $\mathrm{O} 4-\mathrm{Ca} 1-\mathrm{O} 1^{\text {vi }}$ | 112.85 (10) |
| $\mathrm{O} 4{ }^{\text {ii }}-\mathrm{Ca} 1-\mathrm{O}^{\text {vi }}$ | 56.39 (9) |
| $\mathrm{O} 1^{\text {iiii }}-\mathrm{Ca} 1-\mathrm{Ol}^{\text {vi }}$ | 86.53 (8) |
| $\mathrm{O} 1^{\text {iv }}-\mathrm{Ca}-\mathrm{Ol}^{\text {vi }}$ | 151.00 (8) |
| $\mathrm{O} 3-\mathrm{Ca} 1-\mathrm{O} 1^{\text {vi }}$ | 73.88 (10) |
| $\mathrm{O}^{\mathrm{v}}-\mathrm{Ca} 1-\mathrm{Ol}^{\text {vi }}$ | 129.62 (7) |
| $\mathrm{O}{ }^{1 i}-\mathrm{Ca}-\mathrm{Ol}^{\text {vi }}$ | 80.50 (11) |
| O1 ${ }^{\text {viii }}$-La1-O1 $1^{\text {ix }}$ | 138.96 (12) |
| O1 ${ }^{\text {viii- }} \mathrm{La} 1-\mathrm{O} 4^{\text {x }}$ | 73.88 (6) |
| $\mathrm{O} 1^{\mathrm{ix}}$ - La $-\mathrm{O} 4^{\mathrm{x}}$ | 73.88 (6) |
| $\mathrm{O} 1^{\text {viii- }} \mathrm{La} 1-\mathrm{O} 2^{\text {x }}$ | 71.80 (6) |
| $\mathrm{O} 1^{\mathrm{ix}}-\mathrm{La} 1-\mathrm{O} 2^{\mathrm{x}}$ | 71.80 (6) |
| $\mathrm{O} 4 \times-\mathrm{La} 1-\mathrm{O} 2^{\mathrm{x}}$ | 64.64 (11) |
| $\mathrm{O} 1^{\text {viii }}-\mathrm{La} 1-\mathrm{O} 2^{\text {xi }}$ | 121.07 (8) |
| $\mathrm{O} 1^{\mathrm{ix}}$ - $\mathrm{La} 1-\mathrm{O} 2^{\text {xi }}$ | 71.30 (9) |
| $\mathrm{O} 4^{\mathrm{x}}-\mathrm{La} 1-\mathrm{O} 2^{\mathrm{xi}}$ | 137.71 (9) |
| $\mathrm{O} 2{ }^{\mathrm{x}}-\mathrm{La} 1-\mathrm{O} 2^{\mathrm{xi}}$ | 82.07 (7) |
| $\mathrm{O} 1^{\text {viii }} \mathrm{La} 1-\mathrm{O} 2^{\text {xii }}$ | 71.30 (9) |
| $\mathrm{O} 1^{\mathrm{ix}}$ - La $1-\mathrm{O} 2^{\text {xii }}$ | 121.07 (8) |
| O4*-La1-O2 ${ }^{\text {xii }}$ | 137.71 (9) |
| $\mathrm{O} 2^{\mathrm{x}}-\mathrm{La} 1-\mathrm{O} 2^{\text {xii }}$ | 82.07 (7) |
| $\mathrm{O} 2{ }^{\text {xi }}$ - $\mathrm{La} 1-\mathrm{O} 2^{\text {xii }}$ | 53.07 (13) |
| O1 ${ }^{\text {viii }} \mathrm{La} 1-\mathrm{O} 1^{\text {xiii }}$ | 137.03 (9) |
| $\mathrm{O} 1^{\text {ix }}$ - $\mathrm{La} 1-\mathrm{O} 1^{\text {xiii }}$ | 83.72 (6) |
| $\mathrm{O} 4{ }^{\mathrm{x}}-\mathrm{La} 1-\mathrm{O}^{\text {xiii }}$ | 129.92 (8) |
| $\mathrm{O} 2 \times$ - $\mathrm{La} 1-\mathrm{O} 1^{\text {xiii }}$ | 146.79 (6) |
| $\mathrm{O} 2^{\text {xi }}-\mathrm{La} 1-\mathrm{O} 1^{\text {xiii }}$ | 68.76 (8) |
| $\mathrm{O} 2{ }^{\text {xii }}$-La1-O1 ${ }^{\text {xiii }}$ | 92.23 (9) |
| $\mathrm{O} 1^{\text {viii }} \mathrm{La} 1-\mathrm{Ol}^{1}$ | 83.72 (6) |
| $\mathrm{O} 1^{\mathrm{ix}}$ - La $-\mathrm{O} 1^{\mathrm{i}}$ | 137.03 (9) |
| $\mathrm{O} 4 \times-\mathrm{La} 1-\mathrm{O} 1^{\mathrm{i}}$ | 129.92 (8) |
| $\mathrm{O} 2{ }^{\mathrm{x}}-\mathrm{La} 1-\mathrm{O} 1^{\mathrm{i}}$ | 146.79 (6) |
| $\mathrm{O} 2{ }^{\text {xi }}-\mathrm{La} 1-\mathrm{O} 1^{\text {i }}$ | 92.23 (9) |

126.18 (10)
126.18 (10)
77.64 (10)
77.64 (10)
73.69 (10)
73.69 (10)
78.17 (9)
78.17 (9)
144.65 (19)
56.39 (9)
112.85 (10)
151.00 (8)
86.53 (8)
73.88 (10)
129.62 (7)
56.89(9)
86.53 (8)
151.00 (8)
73.88 (10)
129.62 (7)
80.50 (11)
138.96 (12)
73.88 (6)
73.88 (6)
71.80 (6)
71.80 (6)
64.64 (11)
121.07 (8)
71.30 (9)
137.71 (9)
82.07 (7)
71.30 (9)
121.07 (8)
137.71 (9)
82.07 (7)
53.07 (13)
137.03 (9)
83.72 (6)
129.92 (8)
146.79 (6)
68.76 (8)
92.23 (9)
83.72 (6)
137.03 (9)
146.79 (6)
92.23 (9)
$\mathrm{O} 1^{\mathrm{i}}-\mathrm{La} 1-\mathrm{O} 3^{\text {xi }}$
O1 $1^{\text {viii- }} \mathrm{La} 1-\mathrm{O} 3^{\mathrm{xv}}$
$\mathrm{O} 1^{\mathrm{ix}}-\mathrm{La} 1-\mathrm{O}^{\mathrm{xv}}$
$\mathrm{O} 4^{\mathrm{x}}-\mathrm{La} 1-\mathrm{O}^{\mathrm{xv}}$
$\mathrm{O} 2^{\mathrm{x}}-\mathrm{La} 1-\mathrm{O}^{\mathrm{xv}}$
$\mathrm{O} 2^{\mathrm{xi}}-\mathrm{La} 1-\mathrm{O}^{\mathrm{xv}}$
$\mathrm{O} 2^{\mathrm{xii}}-\mathrm{La} 1-\mathrm{O}^{\mathrm{xv}}$
$\mathrm{O} 1^{\text {xiii- }} \mathrm{La} 1-\mathrm{O} 3^{\mathrm{xv}}$
O1 ${ }^{\mathrm{i}-\mathrm{La} 1-O 3^{\mathrm{xv}}}$
$\mathrm{O} 3^{\mathrm{xiv}}-\mathrm{La} 1-\mathrm{O}^{\mathrm{xv}}$
$\mathrm{O} 4-\mathrm{B} 1-\mathrm{Ol}^{\mathrm{i}}$
$\mathrm{O} 4-\mathrm{B} 1-\mathrm{O} 1^{\text {xiii }}$
$\mathrm{O} 1^{\mathrm{i}}-\mathrm{B} 1-\mathrm{O} 1^{\text {xiii }}$
$\mathrm{O} 2^{\mathrm{xvii}}-\mathrm{B} 2-\mathrm{O} 2^{\mathrm{xviii}}$
$\mathrm{O} 2^{\mathrm{xvii}}-\mathrm{B} 2-\mathrm{O} 2^{\text {xix }}$
$\mathrm{O} 2^{\mathrm{xviii}}-\mathrm{B} 2-\mathrm{O} 2^{\mathrm{xix}}$
O3xxii-B3-O3xxiii
O3 ${ }^{x i i}-\mathrm{B} 3-\mathrm{O} 3$
$\mathrm{O} 3 \times x i i i-\mathrm{B} 3-\mathrm{O} 3$
B1ii-O1-Ca1 ${ }^{\mathrm{xv}}$
$\mathrm{B} 1^{\mathrm{ii}}-\mathrm{O} 1-\mathrm{La} 1^{\text {xxiv }}$
$\mathrm{Ca} 1^{\mathrm{xv}}-\mathrm{O} 1-\mathrm{La} 1^{\text {xiv }}$
B1 ${ }^{\text {ii- }}-\mathrm{O} 1-\mathrm{Ca}^{\mathrm{i}}$
$\mathrm{Ca} 1^{\mathrm{xv}}-\mathrm{O} 1-\mathrm{Ca} 1^{\mathrm{i}}$
$\mathrm{La} 1^{\text {xxiv }}-\mathrm{O} 1-\mathrm{Ca} 1^{\mathrm{i}}$
B1 ${ }^{\text {ii }}-\mathrm{O} 1-\mathrm{La} 1^{1 i}$
$\mathrm{Ca} 1^{\mathrm{xv}}-\mathrm{O} 1-\mathrm{La} 1^{\text {ii }}$
La $1^{\text {xxiv }}-\mathrm{O} 1-\mathrm{La} 1^{\text {ii }}$
$\mathrm{Ca} 1^{\mathrm{i}}-\mathrm{O} 1-\mathrm{La} 1^{\mathrm{ii}}$
B2 ${ }^{\mathrm{xxv}}-\mathrm{O} 2-\mathrm{La} 1^{\mathrm{xxvi}}$
$\mathrm{B} 2^{\mathrm{xxv}}-\mathrm{O} 2-\mathrm{La} 1^{\mathrm{xxvii}}$
La1 ${ }^{\text {xxvi }}-\mathrm{O} 2-\mathrm{La} 1^{\text {xxvii }}$
B2 ${ }^{\mathrm{xxv}}-\mathrm{O} 2-\mathrm{La} 1^{\text {xxviii }}$
La1 ${ }^{\text {xxvi }}-\mathrm{O} 2-\mathrm{La} 1^{\text {xxviii }}$
La1 ${ }^{\text {xxvii }-O 2-L a 1 ~}{ }^{\text {xxviii }}$
B3-O3-Ca1
B3-O3-Ca1 ${ }^{\text {vii }}$
$\mathrm{Ca} 1-\mathrm{O} 3-\mathrm{Ca} 1^{\text {vii }}$
B3-O3-La1 ${ }^{\text {xxix }}$
Ca1-O3-La1 ${ }^{\text {xxix }}$
Ca1 ${ }^{\text {vii }-O 3-L a 1 ~}{ }^{\text {xxix }}$
B3-O3-La $1^{\text {iii }}$
$\mathrm{Ca} 1-\mathrm{O} 3-\mathrm{La} 1^{\text {iii }}$
$\mathrm{Ca} 1^{\text {vii- }} \mathrm{O} 3-\mathrm{La} 1^{\text {iii }}$
La1 ${ }^{\text {xxix }}-\mathrm{O} 3-\mathrm{La} 1^{\text {iii }}$
$\mathrm{B} 1-\mathrm{O} 4-\mathrm{Ca} 1^{\mathrm{ii}}$
$\mathrm{B} 1-\mathrm{O} 4-\mathrm{Ca} 1^{\mathrm{i}}$
$\mathrm{Ca} 1^{\mathrm{ii}}-\mathrm{O} 4-\mathrm{Ca} 1^{\mathrm{i}}$
65.77 (12)
116.83 (9)
69.51 (8)
64.52 (12)
122.29 (12)
121.81 (10)
155.42 (13)
65.77 (12)
88.50 (10)
50.66 (12)
119.7 (2)
119.7 (2)
120.6 (4)
120.00 (1)
120.00 (1)
120.00 (1)
120.00 (1)
120.00 (1)
120.00 (1)
147.6 (3)
114.0 (3)
94.81 (8)
83.5 (2)
82.95 (8)
87.75 (8)
92.9 (2)
89.98 (9)
111.47 (9)
160.08 (10)
123.0 (5)
91.42 (19)
107.69 (7)
91.42 (19)
107.69 (7)
135.45 (14)
154.0 (8)
118.3 (8)
87.71 (10)
94.64 (7)
86.76 (7)
85.94 (9)
94.64 (7)
86.76 (7)
85.94 (9)
169.80 (13)
98.91 (12)
98.91 (12)
145.78 (15)
$\mathrm{O} 2^{\mathrm{xii}}-\mathrm{La} 1-\mathrm{O} 1^{\mathrm{i}}$
68.76 (8)
$\mathrm{O} 1^{\text {xiii- }} \mathrm{La} 1-\mathrm{Ol}^{\mathrm{i}}$
O1 ${ }^{\text {viii- }} \mathrm{La} 1-\mathrm{O} 3^{\text {xiv }}$
53.37 (10)
69.51 (8)

B1-O4—La1 ${ }^{\text {xxvi }}$
127.4 (3)
$\mathrm{Ca} 1^{\mathrm{iii}}-\mathrm{O} 4-\mathrm{La} 1^{\mathrm{xxvi}}$
96.00 (9)
$\mathrm{Ca} 1^{\mathrm{i}}-\mathrm{O} 4-\mathrm{La} 1^{\mathrm{xxvi}}$
96.00 (9)

Symmetry codes: (i) $-y+1, x-y+1, z$; (ii) $-x+y,-x+1, z$; (iii) $x-y+1, x, z+1 / 2$; (iv) $-x+1,-x+y, z+1 / 2$; (v) $-x+1,-y+1, z+1 / 2$; (vi) $x, x-y+1, z$; (vii) $-x+1$, $-y+1, z-1 / 2$; (viii) $y-1, x, z-1 / 2$; (ix) $-x+1,-y+2, z-1 / 2$; (x) $x, y, z-1$; (xi) $x-y+1, x+1, z-1 / 2$; (xii) $y-1,-x+y, z-1 / 2$; (xiii) $-x+y, y, z$; (xiv) $x-y, x, z-1 / 2$; (xv) $y,-x+y+1, z-1 / 2$; (xvi) $x, y+1, z$; (xvii) $y-1,-x+y-1, z-1 / 2$; (xviii) $x-y+1, x, z-1 / 2$; (xix) $-x,-y+1, z-1 / 2$; (xx) $-x+y-1,-x, z$; (xxi) $x, y-1, z$; (xxii) $-x+y+1,-x+1, z$; (xxiii) $-y+1, x-y, z$; (xxiv) $-x+1,-y+2, z+1 / 2$; (xxv) $-x,-y+1, z+1 / 2$; (xxvi) $x, y, z+1$; (xxvii) $y-1,-x+y, z+1 / 2$; (xxviii) $x-y+1, x+1$, $z+1 / 2$; (xxix) $y,-x+y, z+1 / 2$.

