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Piperazine-1,4-dium pyridine-2,3-dicarboxylate methanol monosolvate¹

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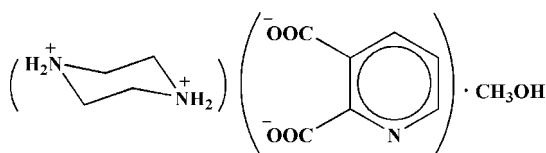
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Key indicators: single-crystal X-ray study; $T = 100$ K; mean $\sigma(\text{C}-\text{C}) = 0.001$ Å; R factor = 0.034; wR factor = 0.085; data-to-parameter ratio = 19.7.

The title solvated molecular salt, $\text{C}_4\text{H}_{12}\text{N}_2^{2+} \cdot \text{C}_7\text{H}_3\text{NO}_4^{2-} \cdot \text{CH}_3\text{OH}$ or $(\text{pipzH}_2)(\text{py-2,3-dc}) \cdot \text{MeOH}$, was prepared by the reaction of pyridine-2,3-dicarboxylic acid (py-2,3-dcH_2) and piperazine (pipz) in methanol (MeOH) as solvent. One of the two carboxylate groups of the acid fragment is nearly perpendicular to the pyridine ring and the other is almost in its plane [$\text{C}-\text{C}-\text{O}$ torsion angles = -85.50 (11) and 88.07 (11)° and $\text{N}-\text{C}-\text{C}-\text{O}$ torsion angles = -176.31 (8) and 5.41 (13)°]. In the crystal, the components are linked by $\text{O}-\text{H} \cdots \text{O}$, $\text{N}-\text{H} \cdots \text{O}$ and $\text{C}-\text{H} \cdots \text{O}$ hydrogen bonds, generating a three-dimensional network.

Related literature

For similar ion pairs, see: Aghabozorg, Manteghi & Ghadermazi (2008); Aghabozorg, Manteghi & Sheshmani (2008). For related metal complexes, see: Barszcz *et al.* (2010); Li & Li (2004).



Experimental

Crystal data

$\text{C}_4\text{H}_{12}\text{N}_2^{2+} \cdot \text{C}_7\text{H}_3\text{NO}_4^{2-} \cdot \text{CH}_4\text{O}$

$M_r = 285.30$

Monoclinic, $P2_1/n$

$a = 8.2541$ (6) Å

$b = 11.8988$ (8) Å

$c = 13.8197$ (9) Å

$\beta = 90.288$ (2)°
 $V = 1357.27$ (16) Å³
 $Z = 4$
Mo $K\alpha$ radiation

$\mu = 0.11$ mm⁻¹
 $T = 100$ K
 $0.25 \times 0.20 \times 0.10$ mm

Data collection

Bruker SMART APEXII
diffractometer
16044 measured reflections

3579 independent reflections
3189 reflections with $I > 2\sigma(I)$
 $R_{\text{int}} = 0.023$

Refinement

$R[F^2 > 2\sigma(F^2)] = 0.034$
 $wR(F^2) = 0.085$
 $S = 1.03$
3579 reflections

182 parameters
H-atom parameters constrained
 $\Delta\rho_{\text{max}} = 0.42$ e Å⁻³
 $\Delta\rho_{\text{min}} = -0.21$ e Å⁻³

Table 1

Hydrogen-bond geometry (Å, °).

$D-H \cdots A$	$D-H$	$H \cdots A$	$D \cdots A$	$D-H \cdots A$
$\text{N2}-\text{H2A} \cdots \text{O4}^{\text{i}}$	0.90	1.74	2.6257 (11)	168
$\text{N2}-\text{H2B} \cdots \text{O2}$	0.90	1.89	2.7274 (11)	155
$\text{N3}-\text{H3A} \cdots \text{O1}^{\text{ii}}$	0.90	1.85	2.7379 (11)	169
$\text{N3}-\text{H3B} \cdots \text{O3}^{\text{iii}}$	0.90	1.86	2.7393 (11)	166
$\text{O5}-\text{H5A} \cdots \text{O1}$	0.85	1.84	2.6867 (10)	171
$\text{C3}-\text{H3} \cdots \text{O5}^{\text{iv}}$	0.95	2.41	3.3163 (13)	159

Symmetry codes: (i) $-x, -y + 2, -z$; (ii) $-x + \frac{1}{2}, y + \frac{1}{2}, -z + \frac{1}{2}$; (iii) $x + \frac{1}{2}, -y + \frac{3}{2}, z + \frac{1}{2}$; (iv) $x - 1, y, z$.

Data collection: *APEX2* (Bruker, 2005); cell refinement: *SAINT* (Bruker, 2005); data reduction: *SAINT*; program(s) used to solve structure: *SHELXS97* (Sheldrick, 2008); program(s) used to refine structure: *SHELXL97* (Sheldrick, 2008); molecular graphics: *PLATON* (Spek, 2009) and *Mercury* (Macrae *et al.*, 2008); software used to prepare material for publication: *SHELXL97*.

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: OM2416).

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¹ In memory of our great professor, Dr Hossein Aghabozorg, who passed away recently.

supporting information

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Piperazine-1,4-diium pyridine-2,3-dicarboxylate methanol monosolvate**Faranak Manteghi, Mohammad Ghadermazi and Nasrin Kakaei****S1. Comment**

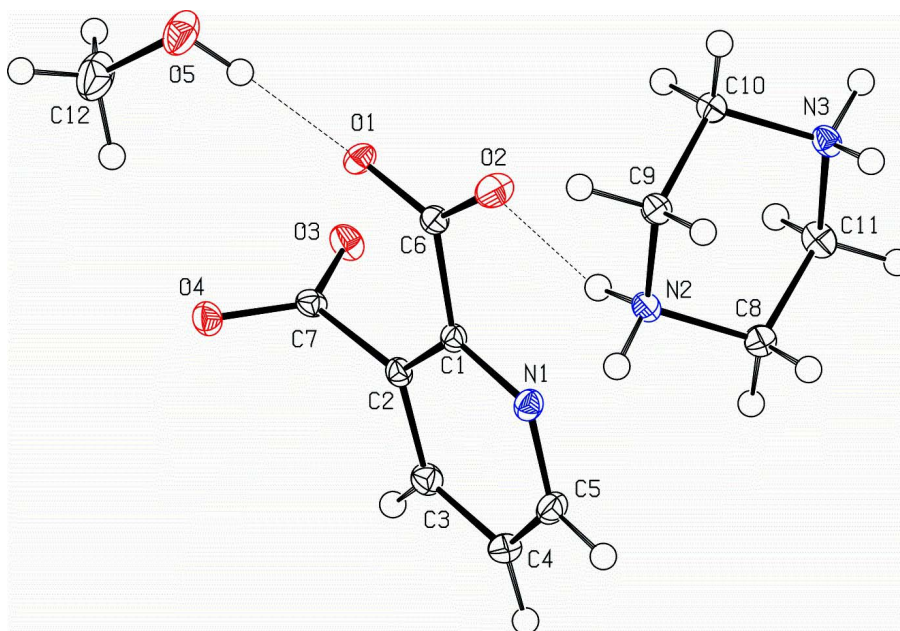
Pyridine-2,3-dicarboxylic acid is remarkably attractive for its flexible and variable coordination modes to construct polymeric architecture. It can act as monodicarboxylate chelating anion, or tridentate coordinating anion with acid hydrogen on nitrogen and doubly deprotonated, tridentate dicarboxylate anion (py-2,3-dc) and even in Mn(II) complexes as tetradentate and pentadentate ligands (Barszcz *et al.*, 2010; Li & Li, 2004). Preparation of ion pairs with the acid increases the chance of its coordination to metals. Therefore, in our work to obtain proton transfer ion pairs, we have reviewed many ion pairs and their metal complexes (Aghabozorg, Manteghi & Sheshmani, 2008). Also, we have reported a similar ion pair formulated as (pipzH₂)(pydcH)₂, (Aghabozorg, Manteghi & Ghadermazi, 2008). The title structure, as shown in Fig. 1, has an asymmetric unit constructed by (pipzH₂)²⁺ and (py-2,3-dc)²⁻ and a neutral methanol molecule with two hydrogen bonds. There are varieties of other strong and weak hydrogen bonds in the structure, shown in Table 1. Also, a C–O... π stacking, between C6–O2 and N1/C1–C5 ring ($-x, -y + 2, -z$) with the distance of 3.5240 (9) Å, and a C–H... π stacking, between C12–H1A and N1/C1–C5 ring ($x + 1/2, -y + 3/2, z - 1/2$), with the distance of 2.791 (1) Å, shown in Fig. 2 are observed.

S2. Experimental

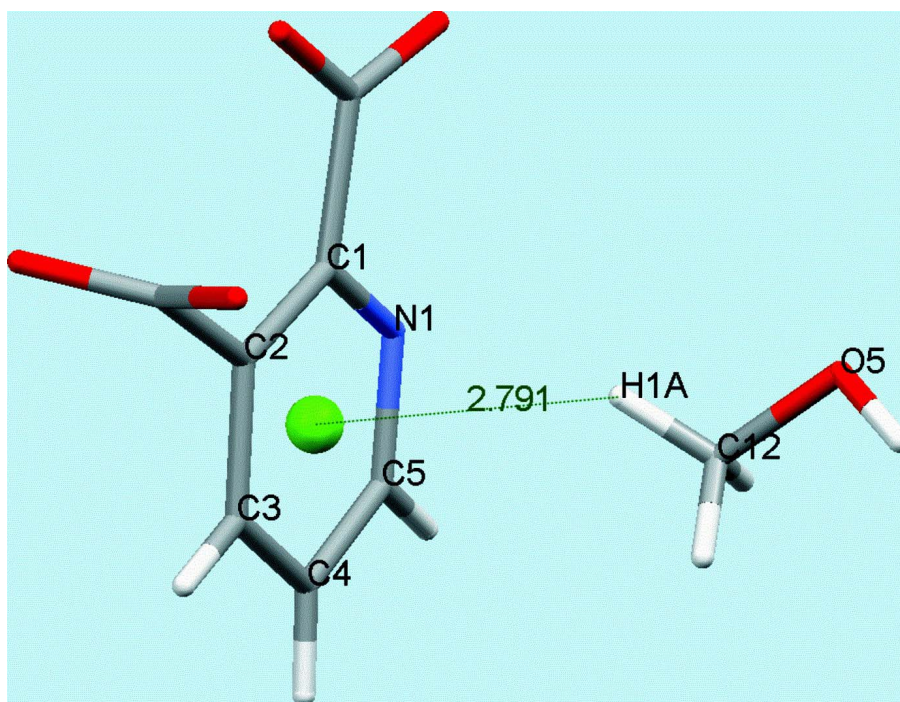
The title compound was synthesized *via* reaction of 1670 mg (10 mmol) pyridine-2,3-dicarboxylic acid with 860 mg (10 mmol) piperazine in a methanol solution (60 ml). The obtained white precipitate was filtered out and dissolved in water to recrystallize. Colorless crystals of the title compound were obtained after 14 days.

S3. Refinement

The H(N) and H(O) atoms were found from a difference Fourier map. The H(C) atom positions were calculated. All the hydrogen atoms were refined with isotropic displacement parameters using a riding model with the $U_{\text{iso}}(\text{H})$ parameters equal to 1.2 times the equivalent isotropic thermal parameter of the bonded C(CH₂) or N(NH₂) or 1.5 times that of C(CH₃) and O(H₂O). Distances were 0.90 Å for N–H, 0.85 Å for O–H, and 0.95 – 0.99 Å for C–H.

**Figure 1**

The molecular structure of (pipzH₂)(py-2,3-dc).MeOH

**Figure 2**

The C–H... π stacking between C12–H1A of methanol and N1/C1–C5 ring of py-2,3-dc.

Piperazine-1,4-diium pyridine-2,3-dicarboxylate methanol monosolvate

Crystal data

 $\text{C}_4\text{H}_{12}\text{N}_2^{2+} \cdot \text{C}_5\text{H}_3\text{NO}_4^{2-} \cdot \text{CH}_4\text{O}$ $M_r = 285.30$ Monoclinic, $P2_1/n$ Hall symbol: $-P\ 2_1n$ $a = 8.2541\ (6)\ \text{\AA}$ $b = 11.8988\ (8)\ \text{\AA}$ $c = 13.8197\ (9)\ \text{\AA}$ $\beta = 90.288\ (2)^\circ$ $V = 1357.27\ (16)\ \text{\AA}^3$ $Z = 4$ $F(000) = 608$ $D_x = 1.396\ \text{Mg m}^{-3}$ Mo $K\alpha$ radiation, $\lambda = 0.71073\ \text{\AA}$

Cell parameters from 7483 reflections

 $\theta = 2.3\text{--}28.1^\circ$ $\mu = 0.11\ \text{mm}^{-1}$ $T = 100\ \text{K}$

Prism, colourless

 $0.25 \times 0.20 \times 0.10\ \text{mm}$

Data collection

Bruker SMART APEXII

diffractometer

Radiation source: fine-focus sealed tube

Graphite monochromator

Detector resolution: $8.3\ \text{pixels mm}^{-1}$ φ and ω scans

16044 measured reflections

3579 independent reflections

3189 reflections with $I > 2\sigma(I)$ $R_{\text{int}} = 0.023$ $\theta_{\text{max}} = 29.0^\circ$, $\theta_{\text{min}} = 2.3^\circ$ $h = -11 \rightarrow 11$ $k = -16 \rightarrow 16$ $l = -18 \rightarrow 18$

Refinement

Refinement on F^2

Least-squares matrix: full

 $R[F^2 > 2\sigma(F^2)] = 0.034$ $wR(F^2) = 0.085$ $S = 1.02$

3579 reflections

182 parameters

0 restraints

Primary atom site location: structure-invariant

direct methods

Secondary atom site location: difference Fourier map

Hydrogen site location: difference Fourier map

H-atom parameters constrained

 $w = 1/[\sigma^2(F_o^2) + (0.035P)^2 + 0.650P]$ where $P = (F_o^2 + 2F_c^2)/3$ $(\Delta/\sigma)_{\text{max}} = 0.001$ $\Delta\rho_{\text{max}} = 0.42\ \text{e \AA}^{-3}$ $\Delta\rho_{\text{min}} = -0.21\ \text{e \AA}^{-3}$

Special details

Geometry. All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

Refinement. Refinement of F^2 against ALL reflections. The weighted R -factor wR and goodness of fit S are based on F^2 , conventional R -factors R are based on F , with F set to zero for negative F^2 . The threshold expression of $F^2 > \sigma(F^2)$ is used only for calculating R -factors(gt) etc. and is not relevant to the choice of reflections for refinement. R -factors based on F^2 are statistically about twice as large as those based on F , and R -factors based on ALL data will be even larger.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters ($\text{\AA}^2$)

	<i>x</i>	<i>y</i>	<i>z</i>	$U_{\text{iso}}^*/U_{\text{eq}}$
O1	0.16285 (8)	0.76486 (6)	0.03344 (5)	0.01401 (15)
O2	0.21626 (9)	0.91599 (6)	0.12414 (6)	0.01918 (16)
O3	−0.13943 (9)	0.61040 (6)	0.03291 (5)	0.01666 (16)
O4	−0.11791 (9)	0.70279 (6)	−0.10648 (5)	0.01627 (15)
N1	−0.09833 (10)	0.97903 (7)	0.11968 (6)	0.01339 (17)

N2	0.17152 (10)	1.11819 (7)	0.21302 (6)	0.01264 (16)
H2A	0.1410	1.1746	0.1735	0.015*
H2B	0.1538	1.0523	0.1828	0.015*
N3	0.31476 (10)	1.05117 (7)	0.39424 (6)	0.01304 (16)
H3A	0.3349	1.1189	0.4206	0.016*
H3B	0.3473	0.9987	0.4371	0.016*
C1	−0.05754 (11)	0.88142 (8)	0.07675 (6)	0.01078 (17)
C2	−0.17210 (11)	0.80866 (8)	0.03586 (7)	0.01165 (18)
C3	−0.33567 (12)	0.83780 (9)	0.04316 (7)	0.01506 (19)
H3	−0.4169	0.7896	0.0175	0.018*
C4	−0.37860 (12)	0.93756 (9)	0.08809 (7)	0.0166 (2)
H4	−0.4891	0.9585	0.0943	0.020*
C5	−0.25545 (12)	1.00615 (9)	0.12379 (7)	0.01563 (19)
H5	−0.2845	1.0758	0.1525	0.019*
C6	0.12243 (11)	0.85332 (8)	0.07816 (7)	0.01183 (18)
C7	−0.13540 (11)	0.69936 (8)	−0.01603 (7)	0.01243 (18)
C8	0.07828 (12)	1.12692 (9)	0.30451 (7)	0.01538 (19)
H8A	−0.0383	1.1149	0.2908	0.018*
H8B	0.0914	1.2032	0.3320	0.018*
C9	0.34843 (12)	1.13038 (8)	0.23146 (7)	0.01367 (18)
H9A	0.3709	1.2059	0.2584	0.016*
H9B	0.4080	1.1231	0.1698	0.016*
C10	0.40670 (12)	1.04139 (8)	0.30194 (7)	0.01438 (19)
H10A	0.3901	0.9658	0.2737	0.017*
H10B	0.5239	1.0513	0.3148	0.017*
C11	0.13684 (12)	1.04015 (9)	0.37760 (7)	0.0162 (2)
H11A	0.0790	1.0508	0.4395	0.019*
H11B	0.1121	0.9637	0.3533	0.019*
O5	0.39165 (9)	0.71135 (8)	−0.09625 (6)	0.02485 (19)
H5A	0.3255	0.7344	−0.0537	0.037*
C12	0.29401 (15)	0.65794 (12)	−0.16692 (9)	0.0302 (3)
H1A	0.3427	0.6679	−0.2309	0.045*
H1B	0.1855	0.6913	−0.1667	0.045*
H1C	0.2861	0.5776	−0.1522	0.045*

Atomic displacement parameters ($\text{\AA}^2$)

	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
O1	0.0156 (3)	0.0103 (3)	0.0162 (3)	0.0017 (2)	0.0019 (3)	−0.0011 (3)
O2	0.0139 (3)	0.0188 (4)	0.0248 (4)	0.0001 (3)	−0.0031 (3)	−0.0083 (3)
O3	0.0236 (4)	0.0110 (3)	0.0153 (3)	−0.0009 (3)	−0.0041 (3)	0.0011 (3)
O4	0.0233 (4)	0.0130 (3)	0.0124 (3)	0.0028 (3)	−0.0019 (3)	−0.0007 (3)
N1	0.0154 (4)	0.0117 (4)	0.0130 (4)	0.0005 (3)	0.0011 (3)	−0.0010 (3)
N2	0.0152 (4)	0.0111 (4)	0.0116 (4)	0.0003 (3)	−0.0022 (3)	0.0000 (3)
N3	0.0168 (4)	0.0105 (4)	0.0118 (4)	−0.0007 (3)	−0.0025 (3)	0.0007 (3)
C1	0.0128 (4)	0.0103 (4)	0.0093 (4)	0.0003 (3)	0.0007 (3)	0.0009 (3)
C2	0.0143 (4)	0.0109 (4)	0.0097 (4)	0.0003 (3)	−0.0006 (3)	0.0008 (3)
C3	0.0135 (4)	0.0173 (5)	0.0144 (4)	−0.0005 (3)	−0.0013 (3)	−0.0005 (4)

C4	0.0134 (4)	0.0201 (5)	0.0163 (4)	0.0037 (4)	0.0002 (3)	0.0002 (4)
C5	0.0181 (5)	0.0136 (4)	0.0152 (4)	0.0032 (4)	0.0023 (3)	−0.0016 (3)
C6	0.0132 (4)	0.0111 (4)	0.0112 (4)	0.0005 (3)	0.0006 (3)	0.0015 (3)
C7	0.0117 (4)	0.0115 (4)	0.0141 (4)	0.0001 (3)	−0.0035 (3)	−0.0015 (3)
C8	0.0142 (4)	0.0172 (5)	0.0148 (4)	0.0009 (4)	0.0003 (3)	0.0002 (4)
C9	0.0142 (4)	0.0137 (4)	0.0132 (4)	−0.0004 (3)	−0.0002 (3)	0.0007 (3)
C10	0.0154 (4)	0.0146 (4)	0.0130 (4)	0.0021 (3)	−0.0011 (3)	−0.0002 (3)
C11	0.0160 (5)	0.0168 (5)	0.0159 (4)	−0.0040 (4)	−0.0006 (3)	0.0028 (4)
O5	0.0159 (4)	0.0345 (5)	0.0242 (4)	−0.0027 (3)	0.0035 (3)	−0.0117 (3)
C12	0.0239 (6)	0.0398 (7)	0.0269 (6)	−0.0016 (5)	0.0002 (5)	−0.0160 (5)

Geometric parameters (Å, °)

O1—C6	1.2662 (12)	C3—H3	0.9500
O2—C6	1.2469 (12)	C4—C5	1.3920 (14)
O3—C7	1.2566 (12)	C4—H4	0.9500
O4—C7	1.2597 (12)	C5—H5	0.9500
N1—C5	1.3379 (13)	C8—C11	1.5215 (14)
N1—C1	1.3477 (12)	C8—H8A	0.9900
N2—C8	1.4871 (12)	C8—H8B	0.9900
N2—C9	1.4881 (12)	C9—C10	1.5155 (13)
N2—H2A	0.9001	C9—H9A	0.9900
N2—H2B	0.9001	C9—H9B	0.9900
N3—C11	1.4911 (13)	C10—H10A	0.9900
N3—C10	1.4920 (12)	C10—H10B	0.9900
N3—H3A	0.9000	C11—H11A	0.9900
N3—H3B	0.9001	C11—H11B	0.9900
C1—C2	1.3992 (13)	O5—C12	1.4139 (14)
C1—C6	1.5227 (13)	O5—H5A	0.8500
C2—C3	1.3981 (13)	C12—H1A	0.9800
C2—C7	1.5164 (13)	C12—H1B	0.9800
C3—C4	1.3864 (14)	C12—H1C	0.9800
C5—N1—C1	118.09 (8)	O4—C7—C2	117.75 (8)
C8—N2—C9	111.05 (7)	N2—C8—C11	110.67 (8)
C8—N2—H2A	108.6	N2—C8—H8A	109.5
C9—N2—H2A	107.6	C11—C8—H8A	109.5
C8—N2—H2B	111.9	N2—C8—H8B	109.5
C9—N2—H2B	108.8	C11—C8—H8B	109.5
H2A—N2—H2B	108.9	H8A—C8—H8B	108.1
C11—N3—C10	111.47 (7)	N2—C9—C10	110.48 (8)
C11—N3—H3A	108.7	N2—C9—H9A	109.6
C10—N3—H3A	108.9	C10—C9—H9A	109.6
C11—N3—H3B	109.3	N2—C9—H9B	109.6
C10—N3—H3B	110.9	C10—C9—H9B	109.6
H3A—N3—H3B	107.5	H9A—C9—H9B	108.1
N1—C1—C2	122.77 (9)	N3—C10—C9	109.50 (8)
N1—C1—C6	115.44 (8)	N3—C10—H10A	109.8

C2—C1—C6	121.77 (8)	C9—C10—H10A	109.8
C3—C2—C1	117.92 (9)	N3—C10—H10B	109.8
C3—C2—C7	116.24 (8)	C9—C10—H10B	109.8
C1—C2—C7	125.84 (8)	H10A—C10—H10B	108.2
C4—C3—C2	119.59 (9)	N3—C11—C8	110.61 (8)
C4—C3—H3	120.2	N3—C11—H11A	109.5
C2—C3—H3	120.2	C8—C11—H11A	109.5
C3—C4—C5	118.22 (9)	N3—C11—H11B	109.5
C3—C4—H4	120.9	C8—C11—H11B	109.5
C5—C4—H4	120.9	H11A—C11—H11B	108.1
N1—C5—C4	123.36 (9)	C12—O5—H5A	104.9
N1—C5—H5	118.3	O5—C12—H1A	109.5
C4—C5—H5	118.3	O5—C12—H1B	109.5
O2—C6—O1	125.55 (9)	H1A—C12—H1B	109.5
O2—C6—C1	118.59 (8)	O5—C12—H1C	109.5
O1—C6—C1	115.84 (8)	H1A—C12—H1C	109.5
O3—C7—O4	124.39 (9)	H1B—C12—H1C	109.5
O3—C7—C2	117.52 (8)		
C5—N1—C1—C2	0.66 (14)	N1—C1—C6—O1	−176.31 (8)
C5—N1—C1—C6	−177.60 (8)	C2—C1—C6—O1	5.41 (13)
N1—C1—C2—C3	−2.12 (14)	C3—C2—C7—O3	−85.50 (11)
C6—C1—C2—C3	176.03 (8)	C1—C2—C7—O3	94.23 (12)
N1—C1—C2—C7	178.16 (9)	C3—C2—C7—O4	88.07 (11)
C6—C1—C2—C7	−3.69 (14)	C1—C2—C7—O4	−92.20 (12)
C1—C2—C3—C4	1.40 (14)	C9—N2—C8—C11	−56.46 (10)
C7—C2—C3—C4	−178.84 (9)	C8—N2—C9—C10	58.30 (10)
C2—C3—C4—C5	0.61 (15)	C11—N3—C10—C9	57.68 (10)
C1—N1—C5—C4	1.56 (15)	N2—C9—C10—N3	−58.17 (10)
C3—C4—C5—N1	−2.20 (15)	C10—N3—C11—C8	−56.39 (11)
N1—C1—C6—O2	5.41 (13)	N2—C8—C11—N3	55.14 (11)
C2—C1—C6—O2	−172.86 (9)		

Hydrogen-bond geometry ($\text{\AA}$, $^\circ$)

$D\cdots H\cdots A$	$D\cdots H$	$H\cdots A$	$D\cdots A$	$D\cdots H\cdots A$
N2—H2A $\cdots$ O4 ⁱ	0.90	1.74	2.6257 (11)	168
N2—H2B $\cdots$ O2	0.90	1.89	2.7274 (11)	155
N3—H3A $\cdots$ O1 ⁱⁱ	0.90	1.85	2.7379 (11)	169
N3—H3B $\cdots$ O3 ⁱⁱⁱ	0.90	1.86	2.7393 (11)	166
O5—H5A $\cdots$ O1	0.85	1.84	2.6867 (10)	171
C3—H3 $\cdots$ O5 ^{iv}	0.95	2.41	3.3163 (13)	159

Symmetry codes: (i) $-x, -y+2, -z$; (ii) $-x+1/2, y+1/2, -z+1/2$; (iii) $x+1/2, -y+3/2, z+1/2$; (iv) $x-1, y, z$.