

Pentazirconium copper tribismuth

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Key indicators: single-crystal X-ray study; $T = 293\text{ K}$; mean $\sigma(\text{Zr}-\text{Cu}) = 0.001\text{ \AA}$; R factor = 0.023; wR factor = 0.041; data-to-parameter ratio = 14.8.

Pentazirconium copper tribismuth, Zr_5CuBi_3 , crystallizes in the hexagonal Hf_5CuSn_3 structure type. The asymmetric unit contains two Zr sites (site symmetries 3.2 and $m2m$), one Cu site (site symmetry 3.m) and one Bi site (site symmetry $m2m$). The environment of the Bi atoms is a tetragonal antiprism with one added atom and a coordination number (CN) of 9. The polyhedron around the Zr1 atom is a defective cubooctahedron with CN = 11. The bicapped hexagonal antiprism (CN = 14) is typical for Zr2 atoms. The Cu atom is enclosed in a eight-vertex polyhedron (octahedron with two centered faces). The metallic type of bonding was indicated by an analysis of the interatomic distances and electronic structure calculation data.

Related literature

For general background, see: Dolotko *et al.* (2003); Giza *et al.* (2001, 2009); Zatorska *et al.* (2002a,b, 2004). For isotropic structures, see: Garcia & Corbett (1990); Pöttgen (1997); Rieger & Parthé (1965); Stetskiv *et al.* (2011). For calculation of the electronic structure using the tight-binding linear muffin-tin orbital (TB-LMTO) method in the atomic spheres approximation, see: Andersen (1975); Andersen & Jepsen (1984); Andersen *et al.* (1985, 1986).

Experimental

Crystal data

Zr_5CuBi_3
 $M_r = 1146.58$
 Hexagonal, $P6_3/mcm$

$a = 8.8712(4)\text{ \AA}$
 $c = 6.0246(3)\text{ \AA}$
 $V = 410.60(3)\text{ \AA}^3$

$Z = 2$
 Mo $K\alpha$ radiation
 $\mu = 72.54\text{ mm}^{-1}$

$T = 293\text{ K}$
 $0.08 \times 0.04 \times 0.02\text{ mm}$

Data collection

Oxford Diffraction Xcalibur3 CCD diffractometer
 Absorption correction: analytical (*CrysAlis RED*; Oxford Diffraction, 2008)
 $T_{\min} = 0.231$, $T_{\max} = 0.654$

1713 measured reflections
 193 independent reflections
 185 reflections with $I > 2\sigma(I)$
 $R_{\text{int}} = 0.136$

Refinement

$R[F^2 > 2\sigma(F^2)] = 0.023$
 $wR(F^2) = 0.041$
 $S = 0.87$
 193 reflections

13 parameters
 $\Delta\rho_{\max} = 1.92\text{ e \AA}^{-3}$
 $\Delta\rho_{\min} = -1.54\text{ e \AA}^{-3}$

Data collection: *CrysAlis CCD* (Oxford Diffraction, 2008); cell refinement: *CrysAlis CCD*; data reduction: *CrysAlis RED* (Oxford Diffraction, 2008); program(s) used to solve structure: *SHELXS97* (Sheldrick, 2008); program(s) used to refine structure: *SHELXL97* (Sheldrick, 2008); molecular graphics: *DIAMOND* (Brandenburg, 2006); software used to prepare material for publication: *SHELXL97*.

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: FF2112).

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supporting information

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Pentazirconium copper tribismuth

Agnieszka Balinska, Ivan Tarasiuk and Volodymyr Pavlyuk

S1. Comment

Zirconium intermetallic compounds are extensively investigated for the last 40 years as possible hydrogen storage materials. The results that we present in this paper is a continuation of the systematic study that we carried out for zirconium alloys with transition metals (Giza *et al.*, 2001; Dolotko *et al.*, 2003) as well as *s*-and *p*-elements (Zatorska *et al.*, 2002*a,b*; 2004; Giza *et al.*, 2009). So far, in the literature no data on ternary intermetallic compounds of Zr—Cu—Bi system has been found. However, it is known that closely related systems such as Zr—Cu—Sn (Pöttgen, 1997), Zr—Cu—Pb (Rieger & Parthé, 1965) and Zr—Cu—Sb (Garcia & Corbett, 1990) form Zr_5Cu_X_3 (where $X=\text{Sn}, \text{Pb}, \text{Sb}$) compounds with hexagonal Hf_5CuSn_3 structure type (superstructure to Ti_5Ga_4 -type) with space group $P6_3/mcm$. Studying alloys of the Zr—Cu—Bi system we found the existence of isostructural Zr_5CuBi_3 compound and investigated its structure by single-crystal method. The projection of the unit cell and coordination polyhedra of the atoms are shown in Fig. 1. The environment of the Bi atoms is a tetragonal antiprism with one added atom and a coordination number equal 9. The polyhedron of Zr1 atom is a defective cubooctahedron with a coordination number equal 11. The bicapped hexagonal antiprism (c.n.=14) is typical for Zr2 atom. The Cu atom is enclosed in a 8-vertex polyhedron (octahedron with two centered faces). The distribution of zirconium and copper atoms in three-dimensional-nets consisted of Bi atoms are shown in Fig. 2a and distribution of bismuth and copper atoms in three-dimensional-nets consisted of Zr atoms are shown in Fig. 2b. In the first case the Bi atoms form a 6_3 corrugated nets and the Zr atoms (second case) form a 3_246 nets. The similar atomic nets was described for Tb_5LiSn_3 isostructural compound (Stetskiv *et al.*, 2011).

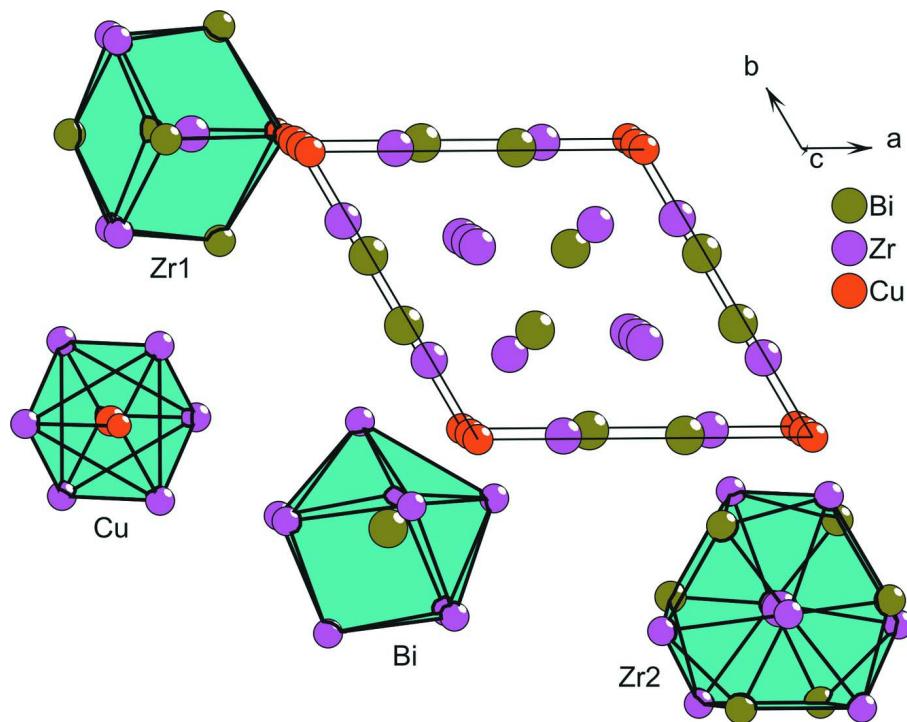
The electronic structure of the Zr_5CuBi_3 compound was calculated using the tight-binding linear muffin-tin orbital (TB-LMTO) method in the atomic spheres approximation (TB-LMTO-ASA; Andersen, 1975; Andersen & Jepsen, 1984; Andersen *et al.*, 1985, 1986), using the experimental crystallographic data which are presented here. The Zr and Cu atoms donate their electrons to the Bi atoms. Therefore positive charge density can be observed around the atoms of transition elements (Zr and Cu) and negative charge density is around the bismuth atoms. The electron localization function (ELF) mapping and isosurfaces (ISO) are presented in Fig. 3a and Fig. 3b, respectively. The total and partial densities of states (DOS) of Zr_5CuBi_3 compound calculated by the TB-LMTO-ASA method are shown in Fig. 4. The Fermi level (EF) lies in a continuous DOS region indicating a metallic character for the title compound. The metallic type of bonding was confirmed also by an analysis of the interatomic distances.

S2. Experimental

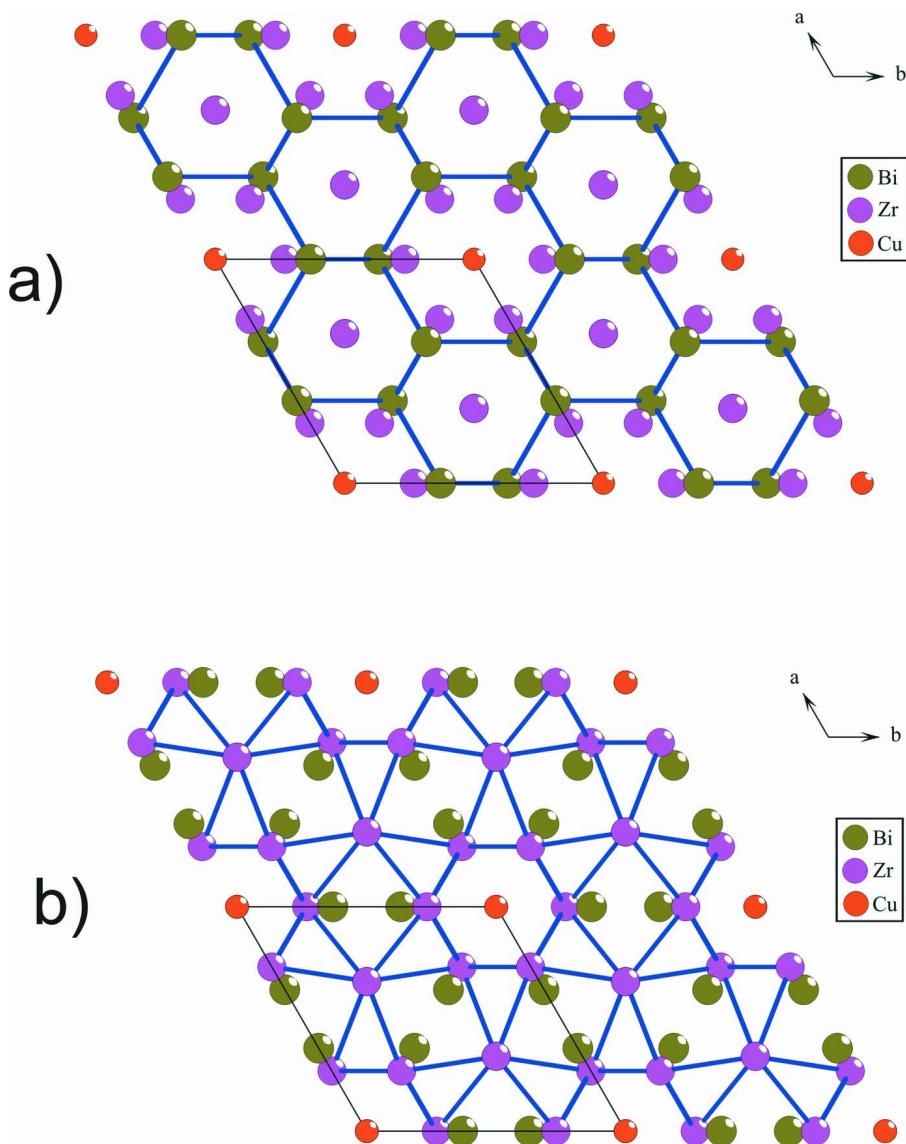
The title compound was prepared from elemental zirconium (foil, 0.25 mm thick 99.8 at.%, Aldrich), copper (powder, pure, POCH) and bismuth (granules, 99.5 at.%, POCH). The pieces of the pure metals with a stoichiometry $\text{Zr}_{50}\text{Cu}_{20}\text{Bi}_{30}$ were pressed into pellet. The sample was melted in arc furnace under continuous argon flow. The losses in alloy composition during melting were checked by weight comparison of the initial mixtures and the alloys. Metallic grey prismatic crystals were found in a crushed alloy using a conventional light microscope.

S3. Refinement

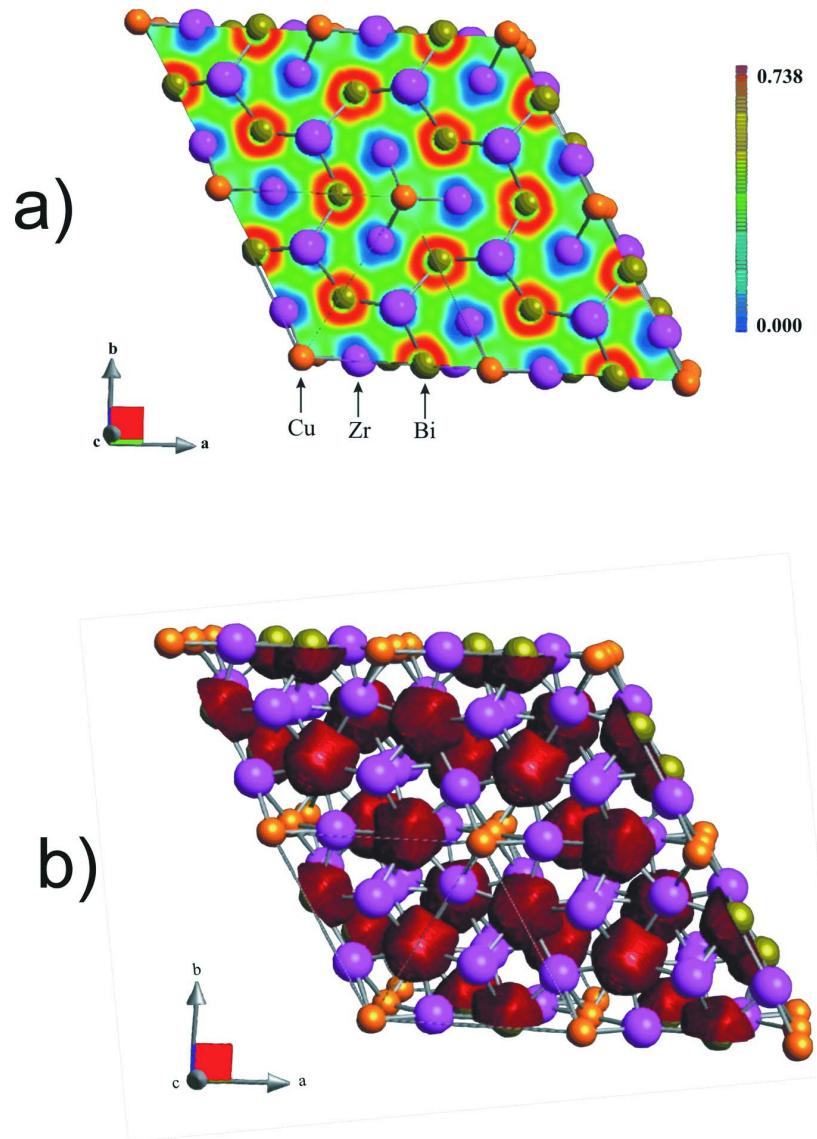
The structure was solved after the analytical absorption correction. In the first stage of the refinement, the positions of the Zr, Cu and Bi atoms were obtained correctly by direct methods. After the last cycle of refinement the highest peak of $1.915 \text{ e}/\text{\AA}^3$ is at $(0; 0.4552; 1/4)$ and 0.76 \AA away from the Bi atom. The deepest hole $-1.539 \text{ e}/\text{\AA}^3$ is at $(0.2424; 0; 1/4)$ and 1.12 \AA away from the same atom.

**Figure 1**

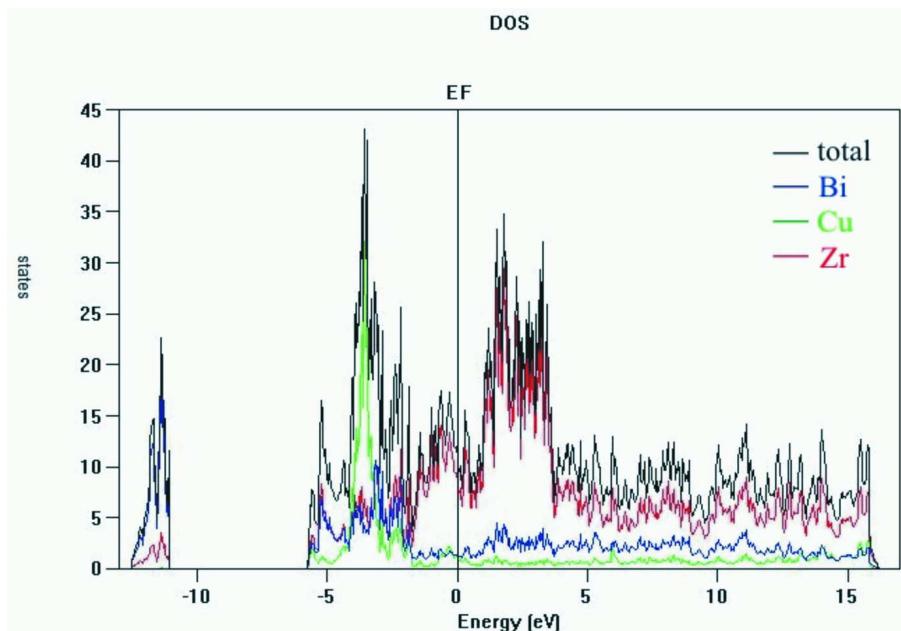
The projection of the unit cell and coordination polyhedra of the atoms.

**Figure 2**

The distribution of Zr and Cu atoms in three-dimensional-nets from Bi atoms (*a*) and distribution of Bi and Cu atoms in three-dimensional-nets from Zr atoms (*b*).

**Figure 3**

(a) The electron localization function (ELF) mapping and (b) isosurfaces of the electron localization function around the atoms for $\text{Zr}_5\text{Cu}\text{Bi}_3$.

**Figure 4**

Total and partial DOS (densities of states) for Zr_5CuBi_3 .

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Crystal data

Zr_5CuBi_3
 $M_r = 1146.58$
Hexagonal, $P6_3/mcm$
Hall symbol: -P 6c 2
 $a = 8.8712 (4)$ Å
 $c = 6.0246 (3)$ Å
 $V = 410.60 (3)$ Å³
 $Z = 2$
 $F(000) = 956$

$D_x = 9.274 \text{ Mg m}^{-3}$
Mo $K\alpha$ radiation, $\lambda = 0.71073$ Å
Cell parameters from 185 reflections
 $\theta = 2.7\text{--}27.4^\circ$
 $\mu = 72.54 \text{ mm}^{-1}$
 $T = 293$ K
Prism, metallic grey
 $0.08 \times 0.04 \times 0.02$ mm

Data collection

Oxford Diffraction Xcalibur3 CCD
diffractometer
Radiation source: fine-focus sealed tube
Graphite monochromator
Detector resolution: 0 pixels mm⁻¹
 ω scans
Absorption correction: analytical
(*CrysAlis RED*; Oxford Diffraction, 2008)
 $T_{\min} = 0.231$, $T_{\max} = 0.654$

1713 measured reflections
193 independent reflections
185 reflections with $I > 2\sigma(I)$
 $R_{\text{int}} = 0.136$
 $\theta_{\max} = 27.4^\circ$, $\theta_{\min} = 2.7^\circ$
 $h = -11 \rightarrow 11$
 $k = -11 \rightarrow 11$
 $l = 0 \rightarrow 7$

Refinement

Refinement on F^2
Least-squares matrix: full
 $R[F^2 > 2\sigma(F^2)] = 0.023$
 $wR(F^2) = 0.041$
 $S = 0.87$
193 reflections

13 parameters
0 restraints
Primary atom site location: structure-invariant
direct methods
Secondary atom site location: difference Fourier
map

$$w = 1/[\sigma^2(F_o^2) + (0.010P)^2]$$

where $P = (F_o^2 + 2F_c^2)/3$

$(\Delta/\sigma)_{\max} < 0.001$

$$\Delta\rho_{\max} = 1.92 \text{ e } \text{\AA}^{-3}$$

$$\Delta\rho_{\min} = -1.54 \text{ e } \text{\AA}^{-3}$$

Special details

Geometry. All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

Refinement. Refinement of F^2 against ALL reflections. The weighted R -factor wR and goodness of fit S are based on F^2 , conventional R -factors R are based on F , with F set to zero for negative F^2 . The threshold expression of $F^2 > \sigma(F^2)$ is used only for calculating R -factors(gt) etc. and is not relevant to the choice of reflections for refinement. R -factors based on F^2 are statistically about twice as large as those based on F , and R -factors based on ALL data will be even larger.

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\AA^2)

	x	y	z	$U_{\text{iso}}^*/U_{\text{eq}}$
Bi1	0.63082 (6)	0.63082 (6)	0.2500	0.00715 (19)
Zr1	0.26831 (17)	0.26831 (17)	0.2500	0.0083 (3)
Zr2	0.6667	0.3333	0.0000	0.0103 (4)
Cu1	0.0000	0.0000	0.0000	0.0102 (10)

Atomic displacement parameters (\AA^2)

	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
Bi1	0.0060 (2)	0.0060 (2)	0.0098 (3)	0.0033 (2)	0.000	0.000
Zr1	0.0075 (4)	0.0075 (4)	0.0102 (8)	0.0039 (5)	0.000	0.000
Zr2	0.0132 (7)	0.0132 (7)	0.0045 (11)	0.0066 (3)	0.000	0.000
Cu1	0.0106 (14)	0.0106 (14)	0.009 (3)	0.0053 (7)	0.000	0.000

Geometric parameters (\AA , $^\circ$)

Bi1—Zr1 ⁱ	2.9319 (6)	Zr2—Zr2 ⁱⁱ	3.0123 (2)
Bi1—Zr1 ⁱⁱ	2.9319 (6)	Zr2—Zr2 ^{viii}	3.0123 (2)
Bi1—Zr1 ⁱⁱⁱ	3.1424 (5)	Zr2—Bi1 ^{ix}	3.1896 (2)
Bi1—Zr1 ^{iv}	3.1424 (5)	Zr2—Bi1 ⁱⁱ	3.1896 (2)
Bi1—Zr2 ^v	3.1896 (2)	Zr2—Bi1 ^{vi}	3.1896 (2)
Bi1—Zr2 ⁱⁱ	3.1896 (2)	Zr2—Bi1 ^x	3.1896 (2)
Bi1—Zr2	3.1896 (2)	Zr2—Bi1 ^{iv}	3.1896 (2)
Bi1—Zr2 ^{iv}	3.1896 (2)	Zr2—Zr1 ⁱⁱ	3.6126 (9)
Bi1—Zr1	3.2159 (17)	Zr2—Zr1 ^{vi}	3.6126 (9)
Zr1—Cu1	2.8167 (13)	Zr2—Zr1 ^{ix}	3.6126 (9)
Zr1—Cu1 ^v	2.8167 (13)	Zr2—Zr1 ^x	3.6126 (9)
Zr1—Bi1 ^{vi}	2.9319 (6)	Cu1—Zr1 ^{xi}	2.8167 (13)
Zr1—Bi1 ^{vii}	2.9319 (6)	Cu1—Zr1 ^{ix}	2.8167 (13)
Zr1—Bi1 ⁱⁱⁱ	3.1424 (5)	Cu1—Zr1 ^{xii}	2.8167 (13)
Zr1—Bi1 ^{iv}	3.1424 (5)	Cu1—Zr1 ^{xiii}	2.8167 (13)
Zr1—Zr2 ⁱⁱ	3.6126 (9)	Cu1—Zr1 ^{xiv}	2.8167 (13)
Zr1—Zr2 ^v	3.6126 (9)	Cu1—Cu1 ^v	3.0123 (2)

Zr1—Zr2	3.6126 (9)	Cu1—Cu1 ^{xii}	3.0123 (2)
Zr1—Zr2 ^{iv}	3.6126 (9)		
Zr1 ⁱ —Bi1—Zr1 ⁱⁱ	89.35 (6)	Zr2 ^{viii} —Zr2—Bi1 ^{ix}	61.822 (2)
Zr1 ⁱ —Bi1—Zr1 ⁱⁱⁱ	78.32 (3)	Zr2 ⁱⁱ —Zr2—Bi1 ⁱⁱ	61.822 (2)
Zr1 ⁱⁱ —Bi1—Zr1 ⁱⁱⁱ	78.32 (3)	Zr2 ^{viii} —Zr2—Bi1 ⁱⁱ	118.178 (2)
Zr1 ⁱ —Bi1—Zr1 ^{iv}	78.32 (3)	Bi1 ^{ix} —Zr2—Bi1 ⁱⁱ	88.460 (16)
Zr1 ⁱⁱ —Bi1—Zr1 ^{iv}	78.32 (3)	Zr2 ⁱⁱ —Zr2—Bi1 ^{vi}	61.822 (2)
Zr1 ⁱⁱⁱ —Bi1—Zr1 ^{iv}	146.91 (6)	Zr2 ^{viii} —Zr2—Bi1 ^{vi}	118.178 (2)
Zr1 ⁱ —Bi1—Zr2 ^v	72.20 (3)	Bi1 ^{ix} —Zr2—Bi1 ^{vi}	73.185 (10)
Zr1 ⁱⁱ —Bi1—Zr2 ^v	145.409 (19)	Bi1 ⁱⁱ —Zr2—Bi1 ^{vi}	99.528 (3)
Zr1 ⁱⁱⁱ —Bi1—Zr2 ^v	69.571 (14)	Zr2 ⁱⁱ —Zr2—Bi1 ^x	118.178 (2)
Zr1 ^{iv} —Bi1—Zr2 ^v	123.798 (7)	Zr2 ^{viii} —Zr2—Bi1 ^x	61.822 (2)
Zr1 ⁱ —Bi1—Zr2 ⁱⁱ	145.409 (19)	Bi1 ^{ix} —Zr2—Bi1 ^x	99.528 (3)
Zr1 ⁱⁱ —Bi1—Zr2 ⁱⁱ	72.20 (3)	Bi1 ⁱⁱ —Zr2—Bi1 ^x	73.185 (10)
Zr1 ⁱⁱⁱ —Bi1—Zr2 ⁱⁱ	69.571 (14)	Bi1 ^{vi} —Zr2—Bi1 ^x	170.093 (17)
Zr1 ^{iv} —Bi1—Zr2 ⁱⁱ	123.798 (7)	Zr2 ⁱⁱ —Zr2—Bi1 ^{iv}	118.178 (2)
Zr2 ^v —Bi1—Zr2 ⁱⁱ	106.815 (9)	Zr2 ^{viii} —Zr2—Bi1 ^{iv}	61.822 (2)
Zr1 ⁱ —Bi1—Zr2	145.409 (19)	Bi1 ^{ix} —Zr2—Bi1 ^{iv}	99.528 (3)
Zr1 ⁱⁱ —Bi1—Zr2	72.20 (3)	Bi1 ⁱⁱ —Zr2—Bi1 ^{iv}	170.093 (17)
Zr1 ⁱⁱⁱ —Bi1—Zr2	123.798 (7)	Bi1 ^{vi} —Zr2—Bi1 ^{iv}	88.460 (16)
Zr1 ^{iv} —Bi1—Zr2	69.571 (14)	Bi1 ^x —Zr2—Bi1 ^{iv}	99.528 (3)
Zr2 ^v —Bi1—Zr2	137.327 (18)	Zr2 ⁱⁱ —Zr2—Bi1	61.822 (2)
Zr2 ⁱⁱ —Bi1—Zr2	56.356 (5)	Zr2 ^{viii} —Zr2—Bi1	118.178 (2)
Zr1 ⁱ —Bi1—Zr2 ^{iv}	72.20 (3)	Bi1 ^{ix} —Zr2—Bi1	170.093 (17)
Zr1 ⁱⁱ —Bi1—Zr2 ^{iv}	145.409 (19)	Bi1 ⁱⁱ —Zr2—Bi1	99.528 (3)
Zr1 ⁱⁱⁱ —Bi1—Zr2 ^{iv}	123.798 (7)	Bi1 ^{vi} —Zr2—Bi1	99.528 (3)
Zr1 ^{iv} —Bi1—Zr2 ^{iv}	69.571 (14)	Bi1 ^x —Zr2—Bi1	88.460 (16)
Zr2 ^v —Bi1—Zr2 ^{iv}	56.356 (5)	Bi1 ^{iv} —Zr2—Bi1	73.185 (9)
Zr2 ⁱⁱ —Bi1—Zr2 ^{iv}	137.327 (18)	Zr2 ⁱⁱ —Zr2—Zr1 ⁱⁱ	65.360 (7)
Zr2—Bi1—Zr2 ^{iv}	106.815 (10)	Zr2 ^{viii} —Zr2—Zr1 ⁱⁱ	114.640 (7)
Zr1 ⁱ —Bi1—Zr1	135.33 (3)	Bi1 ^{ix} —Zr2—Zr1 ⁱⁱ	139.216 (18)
Zr1 ⁱⁱ —Bi1—Zr1	135.33 (3)	Bi1 ⁱⁱ —Zr2—Zr1 ⁱⁱ	56.01 (2)
Zr1 ⁱⁱⁱ —Bi1—Zr1	106.55 (3)	Bi1 ^{vi} —Zr2—Zr1 ⁱⁱ	127.097 (6)
Zr1 ^{iv} —Bi1—Zr1	106.55 (3)	Bi1 ^x —Zr2—Zr1 ⁱⁱ	54.600 (5)
Zr2 ^v —Bi1—Zr1	68.664 (9)	Bi1 ^{iv} —Zr2—Zr1 ⁱⁱ	114.38 (2)
Zr2 ⁱⁱ —Bi1—Zr1	68.664 (9)	Bi1—Zr2—Zr1 ⁱⁱ	50.598 (19)
Zr2—Bi1—Zr1	68.664 (9)	Zr2 ⁱⁱ —Zr2—Zr1 ^{vi}	65.360 (7)
Zr2 ^{iv} —Bi1—Zr1	68.664 (9)	Zr2 ^{viii} —Zr2—Zr1 ^{vi}	114.640 (7)
Cu1—Zr1—Cu1 ^v	64.65 (3)	Bi1 ^{ix} —Zr2—Zr1 ^{vi}	54.600 (5)
Cu1—Zr1—Bi1 ^{vi}	77.64 (3)	Bi1 ⁱⁱ —Zr2—Zr1 ^{vi}	50.598 (19)
Cu1 ^v —Zr1—Bi1 ^{vi}	77.64 (3)	Bi1 ^{vi} —Zr2—Zr1 ^{vi}	56.01 (2)
Cu1—Zr1—Bi1 ^{vii}	77.64 (3)	Bi1 ^x —Zr2—Zr1 ^{vi}	114.38 (2)
Cu1 ^v —Zr1—Bi1 ^{vii}	77.64 (3)	Bi1 ^{iv} —Zr2—Zr1 ^{vi}	139.216 (18)
Bi1 ^{vi} —Zr1—Bi1 ^{vii}	150.65 (6)	Bi1—Zr2—Zr1 ^{vi}	127.097 (6)
Cu1—Zr1—Bi1 ⁱⁱⁱ	138.87 (4)	Zr1 ⁱⁱ —Zr2—Zr1 ^{vi}	103.844 (8)
Cu1 ^v —Zr1—Bi1 ⁱⁱⁱ	74.221 (13)	Zr2 ⁱⁱ —Zr2—Zr1 ^{ix}	114.640 (7)
Bi1 ^{vi} —Zr1—Bi1 ⁱⁱⁱ	94.137 (2)	Zr2 ^{viii} —Zr2—Zr1 ^{ix}	65.360 (7)

Bi1 ^{vii} —Zr1—Bi1 ⁱⁱⁱ	94.137 (2)	Bi1 ^{ix} —Zr2—Zr1 ^{ix}	56.01 (2)
Cu1—Zr1—Bi1 ^{iv}	74.221 (13)	Bi1 ⁱⁱ —Zr2—Zr1 ^{ix}	139.216 (18)
Cu1 ^v —Zr1—Bi1 ^{iv}	138.87 (4)	Bi1 ^{vi} —Zr2—Zr1 ^{ix}	54.600 (5)
Bi1 ^{vi} —Zr1—Bi1 ^{iv}	94.137 (2)	Bi1 ^x —Zr2—Zr1 ^{ix}	127.097 (6)
Bi1 ^{vii} —Zr1—Bi1 ^{iv}	94.137 (2)	Bi1 ^{iv} —Zr2—Zr1 ^{ix}	50.598 (19)
Bi1 ⁱⁱⁱ —Zr1—Bi1 ^{iv}	146.91 (6)	Bi1—Zr2—Zr1 ^{ix}	114.38 (2)
Cu1—Zr1—Bi1	147.675 (17)	Zr1 ⁱⁱ —Zr2—Zr1 ^{ix}	164.10 (4)
Cu1 ^v —Zr1—Bi1	147.675 (17)	Zr1 ^{vi} —Zr2—Zr1 ^{ix}	89.71 (3)
Bi1 ^{vi} —Zr1—Bi1	104.67 (3)	Zr2 ⁱⁱ —Zr2—Zr1 ^x	114.640 (7)
Bi1 ^{vii} —Zr1—Bi1	104.67 (3)	Zr2 ^{viii} —Zr2—Zr1 ^x	65.360 (7)
Bi1 ⁱⁱⁱ —Zr1—Bi1	73.45 (3)	Bi1 ^{ix} —Zr2—Zr1 ^x	50.598 (19)
Bi1 ^{iv} —Zr1—Bi1	73.45 (3)	Bi1 ⁱⁱ —Zr2—Zr1 ^x	54.600 (5)
Cu1—Zr1—Zr2 ⁱⁱ	134.725 (16)	Bi1 ^{vi} —Zr2—Zr1 ^x	114.38 (2)
Cu1 ^v —Zr1—Zr2 ⁱⁱ	104.942 (7)	Bi1 ^x —Zr2—Zr1 ^x	56.01 (2)
Bi1 ^{vi} —Zr1—Zr2 ⁱⁱ	57.205 (10)	Bi1 ^{iv} —Zr2—Zr1 ^x	127.097 (6)
Bi1 ^{vii} —Zr1—Zr2 ⁱⁱ	146.09 (3)	Bi1—Zr2—Zr1 ^x	139.216 (18)
Bi1 ⁱⁱⁱ —Zr1—Zr2 ⁱⁱ	55.829 (13)	Zr1 ⁱⁱ —Zr2—Zr1 ^x	89.71 (3)
Bi1 ^{iv} —Zr1—Zr2 ⁱⁱ	103.75 (3)	Zr1 ^{vi} —Zr2—Zr1 ^x	64.19 (4)
Bi1—Zr1—Zr2 ⁱⁱ	55.32 (2)	Zr1 ^{ix} —Zr2—Zr1 ^x	103.844 (8)
Cu1—Zr1—Zr2 ^v	134.725 (16)	Zr1—Cu1—Zr1 ^{xi}	180.00 (6)
Cu1 ^v —Zr1—Zr2 ^v	104.942 (7)	Zr1—Cu1—Zr1 ^{ix}	85.92 (2)
Bi1 ^{vi} —Zr1—Zr2 ^v	146.09 (3)	Zr1 ^{xi} —Cu1—Zr1 ^{ix}	94.08 (2)
Bi1 ^{vii} —Zr1—Zr2 ^v	57.205 (11)	Zr1—Cu1—Zr1 ^{xii}	85.92 (2)
Bi1 ⁱⁱⁱ —Zr1—Zr2 ^v	55.829 (13)	Zr1 ^{xi} —Cu1—Zr1 ^{xii}	94.08 (2)
Bi1 ^{iv} —Zr1—Zr2 ^v	103.75 (3)	Zr1 ^{ix} —Cu1—Zr1 ^{xii}	94.08 (2)
Bi1—Zr1—Zr2 ^v	55.32 (2)	Zr1—Cu1—Zr1 ^{xiii}	94.08 (2)
Zr2 ⁱⁱ —Zr1—Zr2 ^v	90.29 (3)	Zr1 ^{xi} —Cu1—Zr1 ^{xiii}	85.92 (2)
Cu1—Zr1—Zr2	104.942 (7)	Zr1 ^{ix} —Cu1—Zr1 ^{xiii}	85.92 (2)
Cu1 ^v —Zr1—Zr2	134.725 (16)	Zr1 ^{xii} —Cu1—Zr1 ^{xiii}	180.00 (3)
Bi1 ^{vi} —Zr1—Zr2	57.205 (10)	Zr1—Cu1—Zr1 ^{xiv}	94.08 (2)
Bi1 ^{vii} —Zr1—Zr2	146.09 (3)	Zr1 ^{xi} —Cu1—Zr1 ^{xiv}	85.92 (2)
Bi1 ⁱⁱⁱ —Zr1—Zr2	103.75 (3)	Zr1 ^{ix} —Cu1—Zr1 ^{xiv}	180.00 (3)
Bi1 ^{iv} —Zr1—Zr2	55.829 (13)	Zr1 ^{xii} —Cu1—Zr1 ^{xiv}	85.92 (2)
Bi1—Zr1—Zr2	55.32 (2)	Zr1 ^{xiii} —Cu1—Zr1 ^{xiv}	94.08 (2)
Zr2 ⁱⁱ —Zr1—Zr2	49.279 (13)	Zr1—Cu1—Cu1 ^v	57.675 (17)
Zr2 ^v —Zr1—Zr2	110.65 (4)	Zr1 ^{xi} —Cu1—Cu1 ^v	122.325 (17)
Cu1—Zr1—Zr2 ^{iv}	104.942 (7)	Zr1 ^{ix} —Cu1—Cu1 ^v	122.325 (17)
Cu1 ^v —Zr1—Zr2 ^{iv}	134.725 (16)	Zr1 ^{xii} —Cu1—Cu1 ^v	122.325 (17)
Bi1 ^{vi} —Zr1—Zr2 ^{iv}	146.09 (3)	Zr1 ^{xiii} —Cu1—Cu1 ^v	57.675 (17)
Bi1 ^{vii} —Zr1—Zr2 ^{iv}	57.205 (10)	Zr1 ^{xiv} —Cu1—Cu1 ^v	57.675 (17)
Bi1 ⁱⁱⁱ —Zr1—Zr2 ^{iv}	103.75 (3)	Zr1—Cu1—Cu1 ^{xii}	122.325 (17)
Bi1 ^{iv} —Zr1—Zr2 ^{iv}	55.829 (13)	Zr1 ^{xi} —Cu1—Cu1 ^{xii}	57.675 (17)
Bi1—Zr1—Zr2 ^{iv}	55.32 (2)	Zr1 ^{ix} —Cu1—Cu1 ^{xii}	57.675 (17)
Zr2 ⁱⁱ —Zr1—Zr2 ^{iv}	110.65 (4)	Zr1 ^{xii} —Cu1—Cu1 ^{xii}	57.675 (17)
Zr2 ^v —Zr1—Zr2 ^{iv}	49.279 (13)	Zr1 ^{xiii} —Cu1—Cu1 ^{xii}	122.325 (17)
Zr2—Zr1—Zr2 ^{iv}	90.29 (3)	Zr1 ^{xiv} —Cu1—Cu1 ^{xii}	122.325 (17)

Zr2 ⁱⁱ —Zr2—Zr2 ^{viii}	180.0	Cu1 ^v —Cu1—Cu1 ^{xii}	180.0
Zr2 ⁱⁱ —Zr2—Bi1 ^{ix}	118.178 (2)		

Symmetry codes: (i) $-y+1, x-y+1, z$; (ii) $-x+y+1, -x+1, -z+1/2$; (iii) $-x+1, -y+1, -z+1$; (iv) $-x+1, -y+1, -z$; (v) $x-y, x, z+1/2$; (vi) $-y+1, x-y, z$; (vii) $-x+y, -x+1, -z+1/2$; (viii) $-x+y+1, -x+1, -z-1/2$; (ix) $y, -x+y, -z$; (x) $x-y+1, x, z-1/2$; (xi) $-x, -y, -z$; (xii) $x-y, x, z-1/2$; (xiii) $-x+y, -x, -z+1/2$; (xiv) $-y, x-y, z$.