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The monoclinic form of trilithium dichromium(III) tris(orthophosphate)

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Key indicators: single-crystal X-ray study; T = 290 K; mean σ (P–O) = 0.002 Å; disorder in solvent or counterion; R factor = 0.026; wR factor = 0.068; data-toparameter ratio = 10.7.

The monoclinic form of trilithium dichromium(III) tris(orthophosphate), $Li_3Cr_2(PO_4)_3$, was prepared by the reactive halide flux method. The structure of the title compound is composed of a three-dimensional anionic framework with composition $^{3}_{\infty}$ [Cr₂(PO₄)₃]³⁻ and Li⁺ ions situated in the empty channels. The rigid framework built up from CrO₆ octahedra and PO₄ tetrahedra is the same as that found in other monoclinic $Li_3M_2(PO_4)_3$ (M = Fe, Sc, V) phases. The three Li^+ cations of Li₃Cr₂(PO₄)₃ are unequally disordered over six crystallographically different sites. The classical charge balance of the title compound can be represented as $[Li^+]_3[Cr^{3+}]_2[P^{5+}]_3[O^{2-}]_{12}$. Solid-state UV/Vis spectra indicate that the crystal filed splitting (Δ_0) of the Cr³⁺ ion is around 2.22 eV.

Related literature

For the structures of $Li_3M_2(PO_4)_3$ (M = Fe, Sc, Cr, V), see: d'Yvoire et al. (1983); Verin et al. (1985); Maksimov et al. (1986). The structures of the orthorhombic form of $Li_3Cr_2(PO_4)_3$ have been investigated by Genkina *et al.* (1991). Structural studies of $Li_3V_2(PO_4)_3$ based on single-crystal data have been reported previously by Kee & Yun (2013). The general structural features of the monoclinic phases have been discussed by Patoux et al. (2003); Fu et al. (2010); Yang et al. (2010). For ionic radii, see: Shannon (1976).

Experimental

Crystal data Li₃Cr₂(PO₄)₃

 $M_r = 409.73$

Monoclinic, $P2_1/c$	
a = 8.4625 (4) Å	
b = 8.5560 (3) Å	
c = 14.5344 (5) Å	
$\beta = 125.186 \ (2)^{\circ}$	
V = 860.08 (6) Å ³	

Data collection

Rigaku R-AXIS RAPID S	8163 measured reflections
diffractometer	1962 independent reflections
Absorption correction: multi-scan	1887 reflections with $I > 2\sigma(I)$
(ABSCOR; Higashi, 1995)	$R_{\rm int} = 0.021$
$T_{\min} = 0.688, \ T_{\max} = 1.000$	

Refinement

 $R[F^2 > 2\sigma(F^2)] = 0.026$ 184 parameters $wR(F^2) = 0.068$ 1 restraint $\Delta \rho_{\rm max} = 0.71$ e Å⁻³ S = 1.141962 reflections $\Delta \rho_{\rm min} = -0.71 \text{ e } \text{\AA}^{-3}$

Data collection: RAPID-AUTO (Rigaku, 2006); cell refinement: RAPID-AUTO; data reduction: RAPID-AUTO; program(s) used to solve structure: SHELXS97 (Sheldrick, 2008); program(s) used to refine structure: SHELXL97 (Sheldrick, 2008); molecular graphics: DIAMOND (Brandenburg, 1999); software used to prepare material for publication: WinGX (Farrugia, 2012) and publCIF (Westrip, 2010).

Z = 4

Mo $K\alpha$ radiation

 $0.36 \times 0.12 \times 0.10 \text{ mm}$

 $\mu = 3.16 \text{ mm}^-$

T = 290 K

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Supplementary data and figures for this paper are available from the IUCr electronic archives (Reference: WM2772).

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The monoclinic form of trilithium dichromium(III) tris(orthophosphate)

Joobin Sun, Pilsoo Kim and Hoseop Yun

S1. Comment

The structures of trilithium dimetal tris(orthophosphates), $Li_3M_2(PO_4)_3$ (M = Fe, Sc, Cr, V) have been widely investigated due to their ion transport properties and temperature-dependent phase transitions (d'Yvoire *et al.*, 1983; Verin *et al.*, 1985; Maksimov *et al.*, 1986). For $Li_3Cr_2(PO_4)_3$, the structure of the orthorhombic phase has been studied based on singlecrystal diffraction data (Genkina *et al.*, 1991). The monoclinic and rhombohedral phases have been identified by powder diffraction techniques but no detailed structure determinations have been reported yet (d'Yvoire *et al.*, 1983). In attempts to prepare new mixed alkali metal phosphates by using various alkali metal halides, the monoclinic form of $Li_3Cr_2(PO_4)_3$ has been isolated as single crystals and the detailed structural characterization of this phase is reported here.

The anionic framework of $Li_3Cr_2(PO_4)_3$ is the same as that of the previously reported monoclinic $Li_3V_2(PO_4)_3$ structure (Kee & Yun, 2013). The general structural features of this phase have been discussed previously (Patoux *et al.*, 2003; Fu *et al.*, 2010). Figure 1 shows the coordination environment of the Cr and P atoms. CrO₆ octahedra are joined to PO₄ tetrahedra forming a $[Cr_2(PO_4)_3]$ unit. These units share a terminal oxygen atom to construct the anionic three-dimensional framework, ${}^3_{\infty}[Cr_2(PO_4)_3]^{3-}$ (Fig. 2). The Cr—O distances (1.9007 (18)–2.0392 (18) Å) are in good agreement with those calculated from their ionic radii (2.00 Å; Shannon, 1976), assuming a valence of +III for Cr.

The Li⁺ ions in the empty channels are surrounded by four O atoms in distorted tetrahedral coordinations. There are six crystallographically independent Li sites for this phase and three Li⁺ ions are unequally disordered over them. It has been reported that the positions of Li⁺ ions in Li₃V₂(PO₄)₃ can vary depending on the synthetic conditions while those of the V, P, and O atoms comprising the rigid framework remain intact (Yang *et al.*, 2010). The positions of the Li1, Li3, and Li4 sites in this work are very close to those of the ordered Li sites found in Li₃V₂(PO₄)₃ (Kee & Yun, 2013).

The classical charge balance of the title compound can be represented as $[Li^+]_3[Cr^{3+}]_2[P^{5+}]_3[O^{2-}]_{12}$. Solid-state UV/Vis spectra indicate that the crystal filed splitting(Δ_0) of the Cr³⁺ ion is around 2.22 eV, which is in agreement with the green color of the crystals.

S2. Experimental

The title compound, $Li_3Cr_2(PO_4)_3$, was prepared by the reaction of the elements with the use of the reactive halide-flux technique. A combination of the pure elements, Cr powder (Cerac, 99.95%) and P powder (Aldrich, 99%), were mixed in a fused silica tube in a molar ratio of Cr:P = 1:1 and then LiCl (Cerac, 99.8%) and CsCl (Alfa, 99.9%) mixed in molar ratio of LiCl:CsCl = 4:1 were added. The mass ratio of the reactants and the halides was 1:3. The tube was evacuated to 0.133 Pa, sealed, and heated gradually (30 K/h) to 1123 K, where it was kept for 48 h. The tube was cooled to room temperature at a rate of 4 K/h. The excess halide was removed with water and greenish block-shaped crystals were obtained. The crystals are stable in air and water. A qualitative X-ray fluorescence analysis of selected crystals indicated the presence of Cr and P. The final composition of the compound was determined by single-crystal X-ray diffraction.

S3. Refinement

After the positions of heavy elements (Cr, P, and O) had been established, six significant residual peaks suitable for Li^+ sites were revealed by difference Fourier maps. A model including disorder for these sites was applied. The sum of the Li^+ occupancies was fixed to 3 to meet the charge balance of the compound; the temperature factors of all Li sites were refined isotropically. The highest peak (0.71 e Å⁻³) and the deepest hole (-0.49 e Å⁻³) are 0.57 Å and 0.81 Å from atom Li4 and Cr1, respectively.



Figure 1

A view showing the local coordination environments of Cr and P atoms with the atom labeling scheme. Displacement ellipsoids for Cr, P, and O atoms are drawn at the 70% probability level. [Symmetry codes: (ii) -*x*, *y*+1/2, -*z*+1/2; (iii) - x+1, y+1/2, -z+1/2; (iv) -x+1, y-1/2, -z+1/2; (iv) -x+1, -y+1, -z; (vi) -x+1, -y+1, -z+1; (vii) -x, -y+1, -z; (viii) x, -y+1/2, z-1/2.].



Figure 2

The polyhedral representation of the anionic framework structure built up from $[Cr_2(PO_4)_3]$ units. The disordered Li⁺ cations are located in the channels of this framework.

Trilithium dichromium(III) tris(orthophosphate)

Crystal data	
$Li_3Cr_2(PO_4)_3$	F(000) = 792
$M_r = 409.73$	$D_{\rm x} = 3.164 {\rm Mg} {\rm m}^{-3}$
Monoclinic, $P2_1/c$	Mo $K\alpha$ radiation, $\lambda = 0.71073$ Å
Hall symbol: -P 2ybc	Cell parameters from 8071 reflections
a = 8.4625 (4) Å	$\theta = 3.4 - 27.7^{\circ}$
b = 8.5560 (3) Å	$\mu = 3.16 \text{ mm}^{-1}$
c = 14.5344 (5) Å	T = 290 K
$\beta = 125.186 \ (2)^{\circ}$	Block, green
V = 860.08 (6) Å ³	$0.36 \times 0.12 \times 0.10 \text{ mm}$
Z = 4	
Data collection	
Rigaku R-AXIS RAPID S	8163 measured reflections
diffractometer	1962 independent reflections
Radiation source: Sealed X-ray tube	1887 reflections with $I > 2\sigma(I)$
Graphite monochromator	$R_{\rm int} = 0.021$
ω scans	$\theta_{\text{max}} = 27.5^{\circ}, \ \theta_{\text{min}} = 3.4^{\circ}$
Absorption correction: multi-scan	$h = -10 \rightarrow 10$
(ABSCOR; Higashi, 1995)	$k = -11 \rightarrow 10$
$T_{\min} = 0.688, \ T_{\max} = 1.000$	$l = -18 \rightarrow 18$

Refinement

Refinement on F^2 Least-squares matrix: full $R[F^2 > 2\sigma(F^2)] = 0.026$	Primary atom site location: structure-invariant direct methods Secondary atom site location: difference Fourier
$wR(F^2) = 0.068$	map
S = 1.14	$w = 1/[\sigma^2(F_o^2) + (0.0319P)^2 + 1.8772P]$
1962 reflections	where $P = (F_o^2 + 2F_c^2)/3$
184 parameters	$(\Delta/\sigma)_{\rm max} < 0.001$
1 restraint	$\Delta \rho_{\rm max} = 0.71 \text{ e } \text{\AA}^{-3}$
	$\Delta \rho_{\rm min} = -0.71 \text{ e } \text{\AA}^{-3}$

Special details

Geometry. All e.s.d.'s (except the e.s.d. in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell e.s.d.'s are taken into account individually in the estimation of e.s.d.'s in distances, angles and torsion angles; correlations between e.s.d.'s in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell e.s.d.'s is used for estimating e.s.d.'s involving l.s. planes.

Fractional atomic coordinates and	l isotropic of	[.] eauivalent	isotropic	displacement	parameters	$(Å^2)$)
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	x	у	Ζ	$U_{ m iso}$ */ $U_{ m eq}$	Occ. (<1)
Lil	0.4750 (10)	0.2119 (8)	0.1752 (6)	0.022 (2)*	0.71 (2)
Li2	0.104 (2)	0.208 (2)	0.3364 (14)	0.022 (6)*	0.30 (2)
Li3	0.1164 (11)	0.5885 (9)	0.1920 (7)	0.017 (3)*	0.59 (2)
Li4	0.1935 (14)	0.1892 (12)	0.2627 (8)	0.036 (3)*	0.64 (3)
Li5	0.672 (3)	0.227 (2)	0.2586 (15)	0.019 (6)*	0.27 (2)
Li6	0.273 (3)	0.059 (3)	0.1835 (19)	0.072 (8)*	0.48 (3)
Cr1	0.36305 (5)	0.53352 (4)	0.11142 (3)	0.00608 (11)	
Cr2	0.13604 (5)	0.53218 (5)	0.38801 (3)	0.00787 (11)	
P1	0.46068 (8)	0.39077 (7)	0.35382 (5)	0.00707 (13)	
P2	0.75261 (8)	0.38724 (7)	0.14717 (5)	0.00693 (13)	
P3	0.04107 (8)	0.25059 (7)	0.00513 (5)	0.00717 (13)	
01	0.6057 (2)	0.4162 (2)	0.17588 (15)	0.0129 (4)	
O2	0.2909 (3)	0.3809 (2)	0.36484 (16)	0.0138 (4)	
O3	0.5955 (3)	0.0119 (2)	0.23933 (16)	0.0181 (4)	
O4	0.0766 (3)	0.0017 (2)	0.27885 (15)	0.0124 (3)	
05	0.6674 (3)	0.4170 (2)	0.02547 (15)	0.0135 (4)	
06	0.3515 (3)	0.5558 (2)	0.54233 (16)	0.0197 (4)	
07	0.1224 (3)	0.6330(2)	0.06579 (16)	0.0135 (4)	
08	0.0340 (2)	0.1757 (2)	0.09856 (15)	0.0135 (4)	
09	0.2391 (2)	0.3295 (2)	0.06304 (17)	0.0166 (4)	
O10	0.0217 (3)	0.3652 (2)	0.41922 (16)	0.0156 (4)	
011	0.4784 (2)	0.2282 (2)	0.31441 (14)	0.0106 (3)	
O12	0.1852 (3)	0.7155 (2)	0.32091 (15)	0.0140 (4)	

Atomic displacement parameters $(Å^2)$

	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
Cr1	0.00427 (18)	0.00702 (19)	0.00645 (19)	0.00016 (12)	0.00280 (15)	0.00019 (13)
Cr2	0.00503 (18)	0.0106 (2)	0.00828 (19)	-0.00115 (13)	0.00402 (15)	-0.00151 (14)
P1	0.0064 (3)	0.0078 (3)	0.0061 (3)	0.0019 (2)	0.0030 (2)	0.0007 (2)

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P2	0.0054 (3)	0.0085 (3)	0.0063 (3)	0.0014 (2)	0.0031 (2)	0.0000 (2)
P3	0.0053 (3)	0.0063 (3)	0.0100 (3)	-0.0001 (2)	0.0045 (2)	-0.0001 (2)
01	0.0089 (8)	0.0216 (9)	0.0095 (8)	0.0060 (7)	0.0060 (7)	0.0022 (7)
O2	0.0112 (8)	0.0133 (8)	0.0197 (9)	-0.0001 (7)	0.0106 (7)	-0.0023 (7)
O3	0.0348 (11)	0.0105 (8)	0.0154 (9)	-0.0066 (8)	0.0182 (9)	-0.0043 (7)
O4	0.0105 (8)	0.0128 (8)	0.0095 (8)	0.0013 (7)	0.0033 (7)	0.0010 (7)
05	0.0140 (8)	0.0171 (9)	0.0089 (8)	0.0027 (7)	0.0062 (7)	0.0018 (7)
O6	0.0117 (9)	0.0235 (10)	0.0146 (9)	-0.0025 (8)	0.0023 (8)	-0.0065 (8)
O7	0.0117 (8)	0.0122 (8)	0.0186 (9)	0.0053 (7)	0.0099 (7)	0.0053 (7)
08	0.0100 (8)	0.0180 (9)	0.0108 (8)	-0.0009 (7)	0.0050(7)	0.0038 (7)
09	0.0076 (8)	0.0083 (8)	0.0302 (11)	-0.0018 (7)	0.0087 (8)	-0.0017 (8)
O10	0.0115 (8)	0.0191 (9)	0.0157 (9)	-0.0037 (7)	0.0075 (7)	0.0043 (7)
O11	0.0125 (8)	0.0081 (8)	0.0086 (8)	0.0038 (6)	0.0045 (7)	0.0002 (6)
O12	0.0216 (9)	0.0100 (8)	0.0151 (8)	-0.0057 (7)	0.0133 (8)	-0.0041 (7)

Geometric parameters (Å, °)

Li1—O3	1.934 (7)	Cr1—O5 ^v	1.9007 (18)
Li1-09	1.977 (7)	Cr1—O7	1.9380 (17)
Li1-011	2.011 (7)	Cr1—O9	1.9471 (18)
Li1—O1	2.066 (7)	Cr1—O1	1.9709 (17)
Li2—O4	1.908 (17)	Cr1—O3 ⁱⁱⁱ	1.9965 (18)
Li2—O2	2.028 (17)	Cr1—O11 ⁱⁱⁱ	2.0172 (17)
Li2—O10	2.170 (17)	Cr2—O6	1.9192 (19)
Li2—O12 ⁱ	2.184 (17)	Cr2—O10	1.9208 (18)
Li3—07	1.902 (8)	Cr2—O8 ⁱⁱ	1.9847 (18)
Li3—012	1.943 (8)	Cr2—O2	2.0041 (18)
Li3—O4 ⁱⁱ	2.049 (8)	Cr2—O12	2.0129 (18)
Li3—O3 ⁱⁱⁱ	2.137 (8)	Cr2—O4 ⁱⁱ	2.0392 (18)
Li4—08	1.953 (10)	P1—O6 ^{vi}	1.4994 (19)
Li4—O4	1.969 (10)	P1—O2	1.5368 (18)
Li4—O2	2.040 (10)	P1011	1.5443 (17)
Li4—011	2.098 (10)	P1—O3 ⁱⁱⁱ	1.5463 (19)
Li5—01	1.900 (18)	P2—O5	1.4979 (18)
Li5—O3	1.916 (18)	P2—O12 ^{iv}	1.5394 (18)
Li5—O12 ^{iv}	2.103 (18)	P2—O1	1.5424 (17)
Li5—011	2.206 (18)	P2—O4 ⁱⁱⁱ	1.5532 (18)
Li5—O7 ^{iv}	2.252 (18)	P3—07 ^{vii}	1.5248 (18)
Li6—O8	1.93 (2)	P3—O10 ^{viii}	1.5268 (19)
Li6—O1 ^{iv}	2.08 (2)	Р3—О9	1.5319 (18)
Li6—011	2.22 (2)	P3—O8	1.5337 (18)
Li6—O3	2.39 (2)		
O5 ^v —Cr1—O7	93.57 (8)	O2—Cr2—O12	94.84 (8)
O5 ^v —Cr1—O9	95.83 (9)	O6—Cr2—O4 ⁱⁱ	175.15 (8)
07-Cr1-09	91.63 (8)	O10-Cr2-O4 ⁱⁱ	88.07 (8)
05 ^v —Cr1—O1	94.97 (8)	O8 ⁱⁱ —Cr2—O4 ⁱⁱ	90.18 (7)
07—Cr1—O1	171.08 (8)	O2—Cr2—O4 ⁱⁱ	86.09 (8)

O9—Cr1—O1	84.97 (8)	O12—Cr2—O4 ⁱⁱ	79.09 (8)
$O5^{v}$ — $Cr1$ — $O3^{iii}$	172.27 (8)	O6 ^{vi} —P1—O2	115.09 (11)
O7—Cr1—O3 ⁱⁱⁱ	84.53 (8)	O6 ^{vi} —P1—O11	112.02 (11)
O9—Cr1—O3 ⁱⁱⁱ	91.72 (9)	O2—P1—O11	106.60 (10)
O1—Cr1—O3 ⁱⁱⁱ	87.34 (8)	O6 ^{vi} —P1—O3 ⁱⁱⁱ	106.84 (12)
O5 ^v —Cr1—O11 ⁱⁱⁱ	91.32 (8)	O2—P1—O3 ⁱⁱⁱ	107.11 (11)
O7—Cr1—O11 ⁱⁱⁱ	93.70 (8)	O11—P1—O3 ⁱⁱⁱ	108.98 (10)
O9—Cr1—O11 ⁱⁱⁱ	170.80 (8)	O5—P2—O12 ^{iv}	111.51 (10)
O1—Cr1—O11 ⁱⁱⁱ	88.66 (8)	O5—P2—O1	112.18 (10)
O3 ⁱⁱⁱ —Cr1—O11 ⁱⁱⁱ	81.34 (8)	O12 ^{iv} —P2—O1	105.13 (10)
O6—Cr2—O10	94.07 (9)	O5—P2—O4 ⁱⁱⁱ	109.45 (11)
O6—Cr2—O8 ⁱⁱ	94.27 (8)	O12 ^{iv} —P2—O4 ⁱⁱⁱ	111.89 (10)
O10-Cr2-O8 ⁱⁱ	86.83 (8)	O1—P2—O4 ⁱⁱⁱ	106.55 (10)
O6—Cr2—O2	89.50 (8)	O7 ^{vii} —P3—O10 ^{viii}	104.06 (10)
O10—Cr2—O2	91.50 (8)	O7 ^{vii} —P3—O9	111.22 (10)
O8 ⁱⁱ —Cr2—O2	175.97 (8)	O10 ^{viii} —P3—O9	107.65 (11)
O6—Cr2—O12	99.31 (8)	O7 ^{vii} —P3—O8	112.88 (10)
O10—Cr2—O12	165.23 (8)	O10 ^{viii} —P3—O8	114.36 (11)
O8 ⁱⁱ —Cr2—O12	85.96 (8)	O9—P3—O8	106.63 (11)

Symmetry codes: (i) -x, y-1/2, -z+1/2; (ii) -x, y+1/2, -z+1/2; (iii) -x+1, y+1/2, -z+1/2; (iv) -x+1, y-1/2, -z+1/2; (v) -x+1, -y+1, -z; (vi) -x+1, -y+1, -z; (vii) x, -y+1/2, z-1/2.