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TIPO₃ and its comparison with isotypic RbPO₃ and CsPO₃

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The crystal structure of thallium(I) *catena*-polyphosphate, TIPO₃, contains a polyphosphate chain extending parallel to [010] with a repeating unit of two phosphate tetrahedra. The TI^I atom is located in-between the polyphosphate chains and is bonded by oxygen atoms in a distorted [6 + 1] coordination in the form of a monocapped prism, with the longest TI–O bond to the bridging O atom of the polyphosphate chain. A quantitative structural comparison with isotypic RbPO₃ and CsPO₃ reveals that the usually pronounced stereoactivity of the 6s² lone pair at the TI^I atom is not apparent in the case of TIPO₃.

1. Chemical context

The crystal chemistry of inorganic thallium(I) (or thallous) compounds is dominated by the presence of the $6s^2$ electron lone pair that, in the majority of cases, is stereochemically active (Galy *et al.*, 1975). Therefore, crystal structures comprising a Tl¹ atom mostly have unique structures, and isotypism with analogous phases where the Tl¹ site is replaced by a metal cation of comparable size or by ammonium is comparatively rare. One of these cases pertains to the *catena*-polyphosphate series *MPO*₃ (*M* = Tl, Rb, Cs) for which isotypism of TlPO₃ with the alkali polyphosphates was reported on basis of indexed powder X-ray diffraction data (El Horr, 1991). Although single crystals were available, a refinement of the crystal structure was not performed at that time.

With the intention of obtaining detailed structure data for $TIPO_3$ for a quantitative structural comparison with isotypic $RbPO_3$ and $CsPO_3$, single crystals of the thallium polyphosphate phase were grown and the crystal structure refined using single-crystal X-ray data.

2. Structural commentary

The asymmetric unit of TIPO₃ comprises one Tl, one P and three O sites, all on general positions. The crystal structure of TIPO₃ is made up from a polyphosphate chain with a repeating unit of two phosphate tetrahedra propagating along the [010] direction. Two polyphosphate chains with different orientations cross the unit cell (Fig. 1). The bond-length distribution (Table 1) within a PO₄ tetrahedron is characteristic of a polyphosphate chain (Durif, 1995), *i.e.* two long bonds to the bridging atoms O1 and O1^{vii} [mean 1.600 (8) Å; for symmetry code see Table 1] and two short bonds to the terminal O2 and O3 atoms [mean 1.483 (19) Å] are observed. The Tl^I atoms are situated between the chains and are coordinated to seven oxygen atoms. As has been done for thallium(I) oxoarsenates (Schroffenegger *et al.*, 2020), it is useful to classify the corresponding $Tl^I - O$ bonds into 'short' bonds less than 3.0 Å, and 'long' bonds greater than this threshold up to the maximum bond length of 3.50 Å for the first coordination sphere. The resulting [6 + 1] polyhedron can be derived from a monocapped trigonal prism where the capping O atom is that with the longest Tl - O bond (Fig. 2). This atom (O1) represents the bridging oxygen atom of the polyphosphate chain. Next to the Tl and two P atoms, atom O1 has no further coordination partners. The terminal O2 and O3 atoms of the polyphosphate chain each are bonded to one P and to three Tl atoms in the form of a distorted tetrahedron.

Bond-valence-sum (BVS) calculations (Brown, 2002) for $TIPO_3$ were carried out with the values provided by Locock & Burns (2009) for TI^I –O bonds, and by Brown & Altermatt



Figure 1

The crystal structure of TlPO₃ in a projection along $[00\overline{1}]$. Displacement ellipsoids are drawn at the 75% probability level. The symmetry code refers to Table 1.

Table 1

Comparison of bond lengths in the isotypic MPO_3 polyphosphates (M = TI, Rb, Cs).

(a) This work; (b) a = 12.123 (2), b = 4.228 (2), c = 6.479 (2) Å, $\beta = 96.33$ (33)° (Corbridge, 1956); (c) a = 12.6162 (11), b = 4.2932 (4), c = 6.7575 (6) Å, $\beta = 96.068$ (5)° (Weil & Stöger, 2020).

	$M = \mathrm{Tl}^a$	$M = \mathrm{Rb}^{b}$	$M = Cs^c$
$M-O3^{i}$	2.867 (5)	2.920	3.1097 (18)
M-O3	2.889 (4)	2.971	3.0980 (14)
$M - O3^{ii}$	2.935 (4)	2.948	3.0983 (14)
$M - O2^{iii}$	2.943 (5)	2.973	3.0981 (14)
$M - O2^{iv}$	2.963 (4)	2.905	3.0431 (15)
$M - O2^{v}$	2.997 (4)	3.024	3.1455 (15)
$M - O1^{vi}$	3.216 (4)	3.196	3.3649 (14)
P-O2	1.469 (5)	1.474	1.4793 (16)
P-O3	1.497(5	1.438	1.4919 (16)
P-O1	1.595 (4)	1.621	1.6134 (16)
$P-O1^{vii}$	1.606 (4)	1.624	1.6183 (16)

Symmetry codes (i) $-x + \frac{1}{2}, y - \frac{1}{2}, -z + \frac{3}{2}$; (ii) x, y - 1, z; (iii) x, y, z + 1; (iv) -x, -y, -z + 1; (v) -x, -y + 1, -z + 1; (vi) x, y - 1, z + 1; (vii) $-x + \frac{1}{2}, y - \frac{1}{2}, -z + \frac{1}{2}$.

(1985) for P–O bonds. The obtained BVS values (in valence units) of 0.88 for Tl1, 4.97 for P1, 2.17 for O1, 1.97 for O2 and 1.82 for O3 differ somewhat from the idealized values for atoms with a formal charge of +1, +5 and -2, respectively. In consequence, the global instability index *GII* (Salinas-Sanchez *et al.*, 1992) of 0.14 valence units is rather high and indicates a stable but strained structure (*GII* values < 0.1 valence units are typical for unstrained structures, *GII* values between 0.1 and 0.2 are characteristic of structures with lattice-induced strain, and *GII* values > 0.2 indicate unstable structures).

Apparently, the usually observed stereochemical activity of the $6s^2$ electron lone pair at the Tl^I atom is not very pronounced in the case of TlPO₃, and a crystal structure isotypic with those of the room-temperature forms of RbPO₃ and CsPO₃ is realized (Table 1). This may be due to the



Figure 2

The $[TIO_{6+1}]$ monocapped prism in the crystal structure of $TIPO_3$, with the long TI-O bond shown in yellow. Displacement ellipsoids are drawn at the 75% probability level. Symmetry codes refer to Table 1.

Table 2

Absolute atomic displacements (Å) of isotypic RbPO₃ and CsPO₃ relative to TlPO₃, as well as lattice distortion (S), arithmetic mean distance d_{av} (Å) and measure of similarity (Δ).

	Rb	Cs
<i>M</i> 1	0.0656	0.0703
P1	0.0505	0.0595
01	0.0421	0.0494
O2	0.0996	0.0735
O3	0.1332	0.1793
S	0.0099	0.0245
d_{av}	0.0782	0.0864
Δ	0.060	0.039

comparable ionic radii for monovalent Tl, Rb^+ and Cs^+ cations of 1.50, 1.52 and 1.67 Å, respectively, using a coordination number of six (Shannon, 1976; values for a coordination number of seven were not listed for Tl and Cs).

Whereas the isotypic polyphosphates RbPO₃ and CsPO₃ show structural phase transitions to two (Holst *et al.*, 1994) and to one high-temperature phases (Chudinova *et al.*, 1989), a structural phase transition at higher temperatures has not been reported for TlPO₃. On the contrary, the tetrametaphosphate Tl₄P₄O₁₂ converts at 690 K to the title polyphosphate (Dostál *et al.*, 1969) that therefore represents the high-temperature form of a phosphate with a Tl:P ratio of 1:1.

For a quantitative structural comparison of the three isotypic MPO_3 (M = Tl, Rb, Cs) structures, the program *compstru* (de la Flor *et al.*, 2016) available at the Bilbao Crystallographic Server (Aroyo *et al.*, 2006) was used. Numerical details of the comparison with the TlPO₃ structure as the reference are collated in Table 2. The low values for the degree of lattice distortion (S), the similarity index Δ and the arithmetic mean distance of paired atoms (d_{av}) indicate very similar structures, with the highest absolute displacement of atom O3 in each case.

3. Synthesis and crystallization

A mass of 0.50 g Tl₂CO₃ was immersed in 3 ml of concentrated phosphoric acid ($85\%_{wt}$) in a glass carbon crucible. The mixture was heated within six hours to 573 K, kept at that temperature for ten hours and slowly cooled to room temperature over the course of twelve hours. The obtained highly viscous phosphate flux was leached with a mixture of water and methanol ($\nu/\nu = 1:4$). After separation of the liquid phase through suction filtration, colourless crystals of TlPO₃, mostly with a platy form, were obtained.

4. Refinement

Crystal data, data collection and structure refinement details are summarized in Table 3.

The lattice parameters determined in the current study are in good agreement with those of the previous report [a = 12.270 (7), b = 4.263 (2), c = 6.328 (4) Å, $\beta = 96.72$ (3)°, V = 328.7 Å³; El Horr, 1991], however with higher precision.

Table	3	
Experin	mental	details

Crystal data	
Chemical formula	TIPO3
Mr	283.34
Crystal system, space group	Monoclinic, $P2_1/n$
Temperature (K)	296
a, b, c (Å)	12.2315 (12), 4.2432 (7), 6.3039 (1)
β (°)	96.727 (7)
$V(Å^3)$	324.92 (6)
Z	4
Radiation type	Μο Κα
$\mu (\text{mm}^{-1})$	49.99
Crystal size (mm)	$0.09\times0.08\times0.01$
Data collection	
Diffractometer	Bruker APEXII CCD
Absorption correction	Numerical (HABITUS;
-	Herrendorf, 1997)
T_{\min}, T_{\max}	0.110, 0.536
No. of measured, independent and	6570, 1189, 912
observed $[I > 2\sigma(I)]$ reflections	
R _{int}	0.059
$(\sin \theta / \lambda)_{\max} (\text{\AA}^{-1})$	0.758
Refinement	
$R[F^2 > 2\sigma(F^2)], wR(F^2), S$	0.027, 0.054, 0.99
No. of reflections	1189
No. of parameters	46
$\Delta \rho_{\rm max}, \Delta \rho_{\rm min} ({\rm e} \ {\rm \AA}^{-3})$	1.85, -1.64

Structure solution: isomorphous replacement. Computer programs: *APEX3* and *SAINT* (Bruker, 2018), *SHELXL2018/3* (Sheldrick, 2015), *ATOMS* (Dowty, 2006) and *publCIF* (Westrip, 2010).

For better comparison with the two isotypic structures of $RbPO_3$ and $CsPO_3$, the setting of the unit cell (cell choice 2 of space group No. 14), starting coordinates and atom labelling were adapted from $RbPO_3$ (Corbridge, 1956). The maximum and minimum electron densities in the final difference-Fourier synthesis are located 0.65 and 0.74 Å, respectively, from the Tl1 site.

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Computing details

Data collection: *APEX3* (Bruker, 2018); cell refinement: *SAINT* (Bruker, 2018); data reduction: *SAINT* (Bruker, 2018); program(s) used to solve structure: isomorphous replacement; program(s) used to refine structure: *SHELXL2018/3* (Sheldrick, 2015); molecular graphics: *ATOMS* (Dowty, 2006); software used to prepare material for publication: *publCIF* (Westrip, 2010).

Thallium(I) catena-polyphosphate

Crystal data

TIPO₃ $M_r = 283.34$ Monoclinic, $P2_1/n$ a = 12.2315 (12) Å b = 4.2432 (7) Å c = 6.3039 (1) Å $\beta = 96.727$ (7)° V = 324.92 (6) Å³ Z = 4

Data collection

Bruker APEXII CCD
diffractometer
Radiation source: fine-sealed tube
ω - and φ -scans
Absorption correction: numerical
(HABITUS; Herrendorf, 1997)
$T_{\min} = 0.110, \ T_{\max} = 0.536$
6570 measured reflections

Refinement

Refinement on F^2 Least-squares matrix: full $R[F^2 > 2\sigma(F^2)] = 0.027$ $wR(F^2) = 0.054$ S = 0.991189 reflections 46 parameters F(000) = 480 $D_x = 5.792 \text{ Mg m}^{-3}$ Mo $K\alpha$ radiation, $\lambda = 0.71073 \text{ Å}$ Cell parameters from 2009 reflections $\theta = 3.4-29.2^{\circ}$ $\mu = 49.99 \text{ mm}^{-1}$ T = 296 KPlate, colourless $0.09 \times 0.08 \times 0.01 \text{ mm}$

1189 independent reflections 912 reflections with $I > 2\sigma(I)$ $R_{int} = 0.059$ $\theta_{max} = 32.6^{\circ}, \ \theta_{min} = 3.4^{\circ}$ $h = -18 \rightarrow 18$ $k = -6 \rightarrow 6$ $l = -9 \rightarrow 9$

0 restraints $w = 1/[\sigma^2(F_o^2) + (0.0219P)^2]$ where $P = (F_o^2 + 2F_c^2)/3$ $(\Delta/\sigma)_{max} < 0.001$ $\Delta\rho_{max} = 1.85$ e Å⁻³ $\Delta\rho_{min} = -1.64$ e Å⁻³

Special details

Geometry. All esds (except the esd in the dihedral angle between two l.s. planes) are estimated using the full covariance matrix. The cell esds are taken into account individually in the estimation of esds in distances, angles and torsion angles; correlations between esds in cell parameters are only used when they are defined by crystal symmetry. An approximate (isotropic) treatment of cell esds is used for estimating esds involving l.s. planes.

	x	У	Ζ	$U_{ m iso}$ */ $U_{ m eq}$	
T11	0.08906 (2)	0.14776 (5)	0.77279 (4)	0.02917 (9)	
P1	0.18222 (13)	0.4944 (3)	0.3224 (2)	0.0183 (3)	
01	0.2184 (4)	0.7447 (9)	0.1551 (6)	0.0202 (9)	
O2	0.0814 (4)	0.3466 (9)	0.2180 (8)	0.0331 (11)	
O3	0.1858 (4)	0.6404 (9)	0.5393 (7)	0.0316 (11)	

Fractional atomic coordinates and isotropic or equivalent isotropic displacement parameters (\hat{A}^2)

Atomic displacement parameters $(Å^2)$

	U^{11}	U^{22}	U^{33}	U^{12}	U^{13}	U^{23}
T11	0.02974 (15)	0.02897 (13)	0.02893 (13)	-0.00135 (13)	0.00402 (10)	0.00170 (11)
P1	0.0196 (8)	0.0134 (6)	0.0227 (7)	-0.0015 (6)	0.0060 (6)	-0.0018 (5)
01	0.024 (2)	0.0119 (15)	0.025 (2)	-0.0029 (16)	0.0039 (18)	0.0000 (15)
O2	0.021 (2)	0.026 (2)	0.052 (3)	-0.004 (2)	0.002 (2)	-0.005 (2)
O3	0.046 (3)	0.025 (2)	0.026 (2)	0.001 (2)	0.011 (2)	-0.0035 (18)

Geometric parameters (Å, °)

Tl1—O3 ⁱ	2.867 (5)	Tl1—O1 ^{vi}	3.216 (4)
T11—O3	2.889 (4)	P1—O2	1.469 (5)
T11—O3 ⁱⁱ	2.935 (4)	P1—O3	1.497 (5)
Tl1—O2 ⁱⁱⁱ	2.943 (5)	P1	1.595 (4)
T11-O2 ^{iv}	2.963 (4)	P1—O1 ^{vii}	1.606 (4)
T11—O2 ^v	2.997 (4)		
O3 ⁱ —T11—O3	77.73 (13)	Tl1 ^{viii} —O1—Tl1 ^{ix}	75.05 (8)
O3 ⁱ —T11—O3 ⁱⁱ	77.00 (13)	P1	129.7 (2)
O3—Tl1—O3 ⁱⁱ	93.54 (13)	P1 ^x —O1—Tl1 ^x	66.97 (15)
O3 ⁱ —T11—O2 ⁱⁱⁱ	75.25 (13)	Tl1 ^{viii} —O1—Tl1 ^x	79.47 (8)
O3—Tl1—O2 ⁱⁱⁱ	109.83 (12)	Tl1 ^{ix} —O1—Tl1 ^x	73.65 (7)
O3 ⁱⁱ —Tl1—O2 ⁱⁱⁱ	138.47 (13)	P1—O1—Tl1 ^v	69.65 (16)
$O3^{i}$ —T11— $O2^{iv}$	128.90 (12)	P1 ^x —O1—Tl1 ^v	130.4 (2)
O3—Tl1—O2 ^{iv}	148.59 (14)	Tl1 ^{viii} —O1—Tl1 ^v	68.02 (8)
$O3^{ii}$ —Tl1— $O2^{iv}$	79.42 (13)	Tl1 ^{ix} —O1—Tl1 ^v	79.10 (8)
$O2^{iii}$ —T11— $O2^{iv}$	94.78 (12)	Tl1 ^x —O1—Tl1 ^v	141.92 (11)
$O3^{i}$ —Tl1— $O2^{v}$	129.52 (12)	P1-O1-Tl1 ^{xi}	61.69 (14)
O3—Tl1—O2 ^v	79.59 (13)	$P1^{x}$ — $O1$ — $T11^{xi}$	68.71 (14)
$O3^{ii}$ —Tl1— $O2^{v}$	149.02 (14)	Tl1 ^{viii} —O1—Tl1 ^{xi}	153.65 (12)
$O2^{iii}$ —Tl1— $O2^{v}$	71.11 (16)	Tl1 ^{ix} —O1—Tl1 ^{xi}	131.30 (10)
$O2^{iv}$ —Tl1— $O2^{v}$	90.79 (13)	Tl1 ^x —O1—Tl1 ^{xi}	105.89 (10)

	47 10 (11)		112 06 (10)
03 ¹ —111—01 ¹	47.18 (11)	$\Pi V \rightarrow O I \rightarrow \Pi I \Lambda V$	112.06 (10)
O3—T11—O1 ^{vi}	124.87 (13)	$P1-O2-T11^{ix}$	115.5 (3)
$O3^{ii}$ —Tl1—O1 ^{vi}	78.11 (12)	$P1-O2-T11^{iv}$	148.1 (3)
$O2^{iii}$ —Tl1—O1 ^{vi}	60.37 (11)	$T11^{ix}$ —O2— $T11^{iv}$	85.22 (12)
$O2^{iv}$ —Tl1—O1 ^{vi}	83.93 (12)	$P1-O2-T11^{\vee}$	103.6 (2)
O2 ^v —Tl1—O1 ^{vi}	130.42 (13)	$Tl1^{ix}$ $O2$ $Tl1^{v}$	108.89 (16)
O3 ⁱ —T11—P1	87.23 (9)	$Tl1^{iv}$ —O2— $Tl1^{v}$	90.79 (13)
O3—T11—P1	24.76 (9)	P1	74.9 (2)
O3 ⁱⁱ —Tl1—P1	73.32 (9)	Tl1 ^{ix} —O2—Tl1	149.54 (14)
O2 ⁱⁱⁱ —Tl1—P1	134.59 (9)	Tl1 ^{iv} —O2—Tl1	75.68 (11)
O2 ^{iv} —Tl1—P1	127.54 (11)	Tl1 ^v —O2—Tl1	95.07 (13)
O2 ^v —Tl1—P1	90.46 (10)	P1—O2—Tl1 ^{viii}	82.93 (19)
O1 ^{vi} —Tl1—P1	130.72 (8)	Tl1 ^{ix} —O2—Tl1 ^{viii}	66.99 (9)
O3 ⁱ —T11—O2	108.64 (12)	$Tl1^{iv}$ —O2— $Tl1^{viii}$	128.67 (15)
O3—Tl1—O2	45.47 (11)	Tl1v—O2—Tl1viii	61.83 (8)
O3 ⁱⁱ —Tl1—O2	69.49 (11)	Tl1—O2—Tl1 ^{viii}	143.17 (12)
O2 ⁱⁱⁱ —Tl1—O2	149.54 (14)	P1—O3—Tl1 ^{xi}	107.8 (3)
O2 ^{iv} —Tl1—O2	104.32 (11)	P1	101.3 (2)
O2 ^v —Tl1—O2	84.93 (13)	Tl1 ^{xi} —O3—Tl1	103.19 (15)
O1 ^{vi} —Tl1—O2	144.09 (10)	P1O3T11 ^{xii}	142.3 (3)
P1—T11—O2	23.87 (8)	$T11^{xi}$ —O3— $T11^{xii}$	102.06 (14)
O2—P1—O3	121.3 (3)	T11O3T11 ^{xii}	93.54 (13)
O2—P1—O1	105.7 (3)	P1	72.3 (2)
O3—P1—O1	110.3 (2)	$T11^{xi}$ —O3— $T11^{v}$	163.77 (15)
O2—P1—O1 ^{vii}	110.2 (2)	Tl1—O3—Tl1 ^v	92.54 (13)
O3—P1—O1 ^{vii}	104.6 (3)	$T11^{xii}$ —O3— $T11^{v}$	72.64 (11)
O1-P1-O1 ^{vii}	103.41 (12)		

Symmetry codes: (i) -*x*+1/2, *y*-1/2, -*z*+3/2; (ii) *x*, *y*-1, *z*; (iii) *x*, *y*, *z*+1; (iv) -*x*, -*y*, -*z*+1; (v) -*x*, -*y*+1, -*z*+1; (vi) *x*, *y*-1, *z*+1; (vii) -*x*+1/2, *y*-1/2, -*z*+1/2; (viii) *x*, *y*+1, *z*-1; (ix) *x*, *y*, *z*-1; (x) -*x*+1/2, *y*+1/2, -*z*+1/2; (xi) -*x*+1/2, *y*+1/2, -*z*+3/2; (xii) *x*, *y*+1, *z*.