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Supporting information for article:

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Andy S. Anker, Emil T. S. Kjaer, Mikkel Juelsholt and Kirsten M. Ø. Jensen

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POMFinder: Identifying polyoxometalate cluster structures from pair distribution function data using explainable machine learning

Andy S. Anker¹, Emil T. S. Kjaer¹, Mikkel Juulsholt,^{1,2} and Kirsten M. Ø. Jensen^{1}*

**1: Department of Chemistry & Nano-Science Center, University of Copenhagen, 2100
Copenhagen Ø, Denmark**

2: Department of Materials, University of Oxford, Parks Road, Oxford, OX1 3PH, UK

*Correspondence to kirsten@chem.ku.dk (KMØJ)

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A: Determining if two polyoxometalate (POM) fragments are identical

Table S1: Simulation parameters for pair distribution functions (PDFs) used to determine if two clusters are similar. The isotropic atomic displacement parameters (ADP) have been set high to emphasise the general trends in the PDF and not the disorder.

$R_{\text{Range}} = 0 - 30 \text{ \AA}$
$R_{\text{step}} = 0.1 \text{ \AA}$
$Q_{\text{min}} = 0.2 \text{ \AA}^{-1}$
$Q_{\text{max}} = 30 \text{ \AA}^{-1}$
$Q_{\text{damp}} = 0.01 \text{ \AA}^{-1}$
$\text{ADP}^{\text{Biso}} = 1 \text{ \AA}^2$

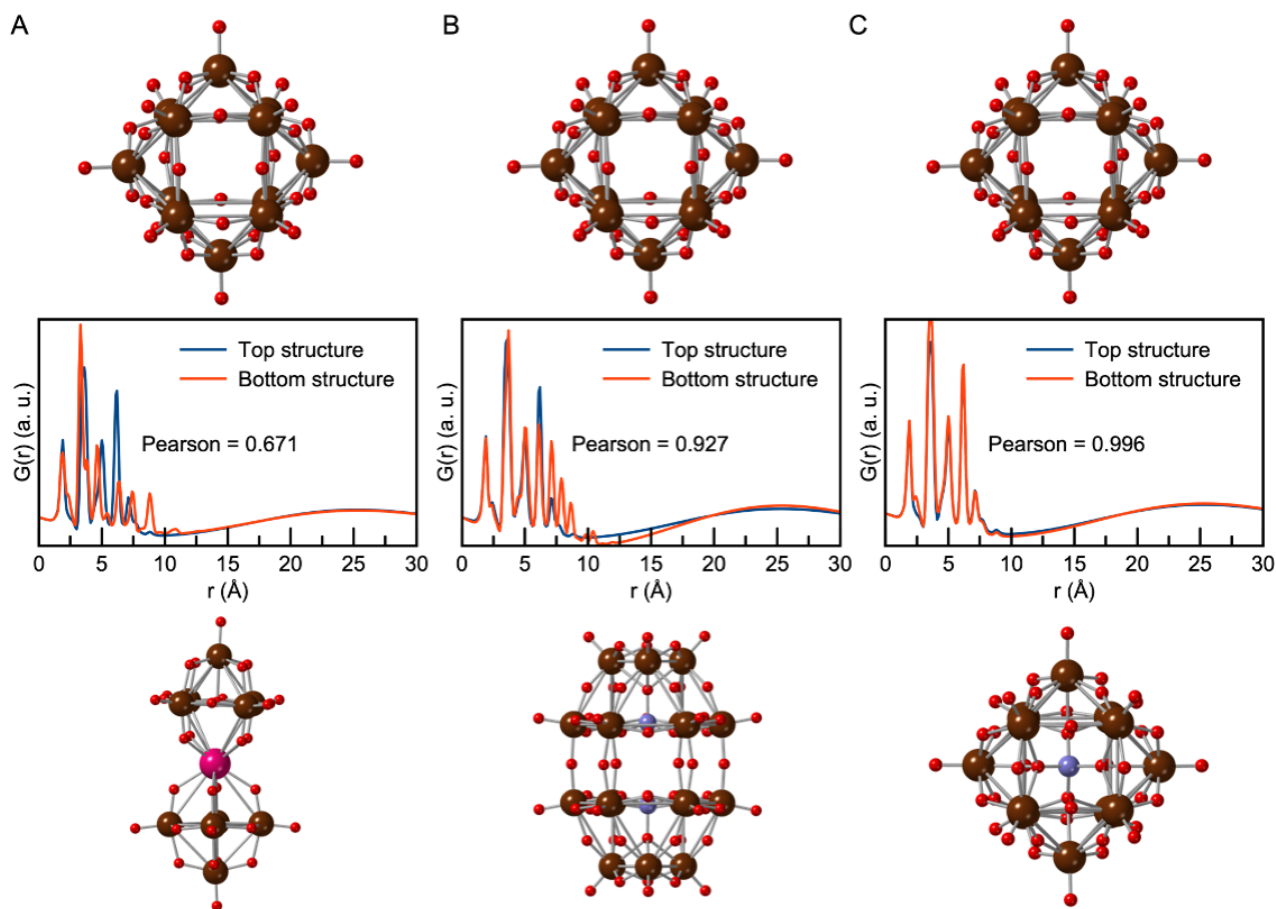


Figure S1: Three examples where the Pearson correlation coefficient is calculated between the simulated PDF of a $W_{12}O_{36}$ cluster and a simulated PDF of a A) $SmW_{10}O_{36}$ cluster, B) $As_2W_{18}O_{62}$ cluster and C) $PW_{12}O_{40}$ cluster.

B: Simulation parameters for the simulated data sets used to train POMFinder and normalisation

Table S2: Parameter range for the simulated data sets.¹ The simulated parameters were determined using hypercube sampling.²

PDF	SAXS
$R_{\text{Range}} = 0 - 10 \text{ \AA}$	$Q_{\text{Range}} = 0 - 2 \text{ \AA}^{-1}$
$R_{\text{step}} = 0.1 \text{ \AA}$	Background = 0 – 0.01

$Q_{\min} = 0 - 2 \text{ \AA}^{-1}$	DebyeSumRmax = 10^7 \AA
$Q_{\max} = 14 - 28 \text{ \AA}^{-1}$	Gaussian Noise RMS = 0 - 0.01
$Q_{\text{damp}} = 0.01 - 0.04 \text{ \AA}^{-1}$	
$\text{ADP}^{\text{Biso}} = 0 - 2 \text{ \AA}^2$	

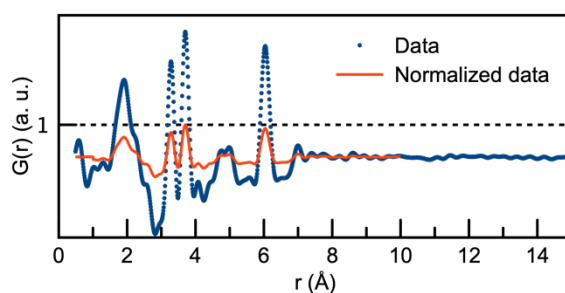


Figure S2: Normalisation of the PDF. Comparison of the experimental data set of a 0.05 M ammonium metatungstate hydrate, $(\text{NH}_4)_6[\text{H}_2\text{W}_{12}\text{O}_{40}] \cdot x\text{H}_2\text{O}$, solution before and after normalisation.

C: Loss curve for the training of POMFinder

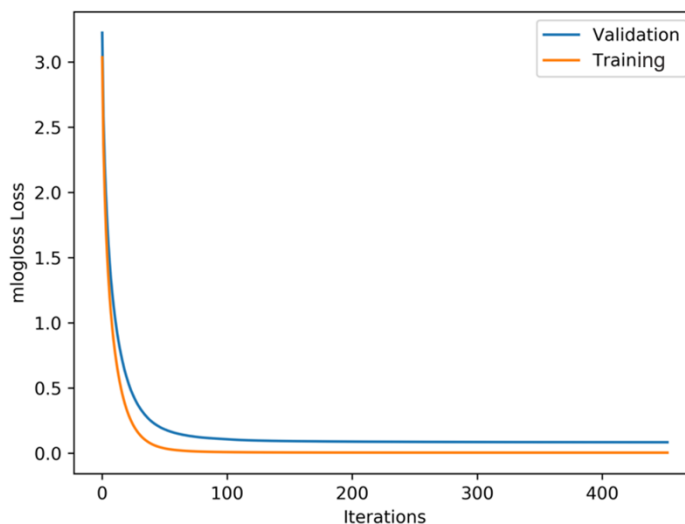


Figure S3: Loss curve for the training of the GBDT algorithm to predict which POM cluster a PDF matches. The training loss converges to zero, while the validation loss is slightly higher (overfitting). This means the model learns to predict perfectly on previously seen data sets, while it has minor discrepancies on unknown data. The mlogloss is defined elsewhere.³

D: Refinement parameters for the fits shown in Figure 4-6 in the main paper

Table S3: Refined parameters for the five best candidate POMs obtained from POMFinder for PDF data analysis. The structures are shown in Figure 4 in the main paper. The B_{iso} value for oxygen is set to 2 \AA^2 .

Rank	Probability [%]	Structure	Scale	Expansion/contraction factor	B_{iso} (metal) [\AA^2]
1 st	82.8	A $W_{11}O_{35}$ Keggin-based fragment from the dimeric $K_{5.5}Na_7Nd(SiW_{11}O_{39}(H_2O))_2(CH_3COO)_2(H_2O)_{10}$ complex ⁴	1.53	0.989	0.660
2 nd	14.4	A $W_{12}O_{36}$ fragment from the $K_5H(CoW_{12}O_{40})(H_2O)_{15}$ crystal ⁵	1.601	1.000	0.738
3 rd	1.5	A $W_{12}O_{40}$ fragment from an ionic crystal structure ⁶ of $(Al_{13}O_4(OH)_{24}(H_2O)_{12})(H_2W_{12}O_{40})(OH)(H_2O)_{23.12}$	1.505	1.003	0.788
4 th	1.0	A $W_{12}O_{36}$ fragment from the porous inorganic of the form $K_2NaH_2(BW_{12}O_{40})(H_2O)_{12}$ ⁷	1.414	1.004	0.822
5 th	0.2	A $W_{12}Rb_4BO_{43}$ fragment from another ionic crystal ⁸ $Rb_4(Cr_3O(OOCH)_6(H_2O)_3(BW_{12}O_4)_3)(H_2O)_{16}$	0.514	1.000	0.000

Table S4: Refined parameters for the five best candidate POMs obtained from POMFinder for analysis of rapid acquisition PDF data. The structures are shown in Figure 5 in the main paper. The B_{iso} value for oxygen is set to 2 \AA^2 .

Rank	Probability [%]	Structure	Scale	Expansion/contraction factor	B_{iso} (metal) [\AA^2]
1 st	65.0	A W_9SiO_{34} fragment from a Keggin-based	1.086	0.994	0.395

		$\text{Na}_2[\text{C}(\text{NH}_2)_3]_2[\{(\text{CH}_3)_2\text{Sn}(\text{H}_2\text{O})\}_3(A-\alpha\text{-SiW}_9\text{O}_{34})] \cdot 10\text{H}_2\text{O}$ crystal ⁹			
2 nd	27.4	A $\text{W}_{12}\text{O}_{36}$ fragment from the crystal structure of a porous framework based on Keggin polyoxoanions, $\text{K}_2\text{NaH}_2[\text{BW}_{12}\text{O}_{40}] \cdot 12\text{H}_2\text{O}$ ¹⁰	0.848	1.001	0.498
3 rd	1.6	A $\text{W}_{20}\text{O}_{64}$ fragment from a pseudo-Keggin based crystal ¹¹ with chemical composition $\text{H}(2-x)\text{Bi}_2\text{W}_{20}\text{O}_{70}(\text{HWO}_3)$	1.053	0.956	0.373
4 th	1.6	A $\text{SbW}_9\text{O}_{30}$ fragment from a $\text{K}_{11}[\text{Sb}_3(\text{SiW}_9\text{O}_{34})_2] \cdot 31\text{H}_2\text{O}$ crystal structure ¹²	1.228	0.983	0.325
5 th	0.9	A $\text{V}_{15}\text{O}_{42}$ fragment from the bicapped Keggin structure ¹³ $(\text{TMA})_3\text{H}_6\text{V}^{\text{V}}_{15}\text{O}_{42} \cdot 2.5\text{H}_2\text{O}$ (TMA = tetramethylammonium)	1.830	0.952	2.174

Table S5: Refined parameters for the five best candidate POMs obtained from POMFinder for analysis of rapid acquisition PDF data. The structures are shown in Figure 6 in the main paper. The B_{iso} value for oxygen is set to 2 \AA^2 .

Rank	Probability [%]	Structure	Scale	Expansion/contraction factor	B_{iso} (metal) [\AA^2]
1 st	80.7	A $\text{W}_{48}\text{O}_{152}$ fragment from the polyanion $\text{K}_{26.5}\text{Li}_{9.5}[\text{H}_4\text{As}_8\text{W}_{48}\text{O}_{184}] \cdot 90\text{H}_2\text{O}$ ¹⁴	1.883	0.957	3.284
2 nd	8.6	A $\text{W}_{12}\text{O}_{42}$ fragment from the acidic sodium polytungstates ¹⁵ $\text{Na}_5[\text{H}_7\text{W}_{12}\text{O}_{42}] \cdot 20\text{H}_2\text{O}$	1.176	0.989	0.503
3 rd	1.4	A $\text{W}_{11}\text{K}_3\text{O}_{38}$ fragment from the crystal structure ¹⁶ $\text{K}_6\text{H}_4\text{W}_{11}\text{O}_{38} \cdot \text{H}_2\text{O}$	0.602	1.001	0.000
4 th	1.0	A W_2O_7 fragment from the crystal structure ¹⁷ of $\text{Bi}_2\text{W}_2\text{O}_9$	1.885	0.998	0.338
5 th	0.9	A Re_2O_8 fragment from the crystal structure $\text{Bi}_{28}\text{Re}_2\text{O}_{49}$ ¹⁸	0	-	-

E: SHAP analysis

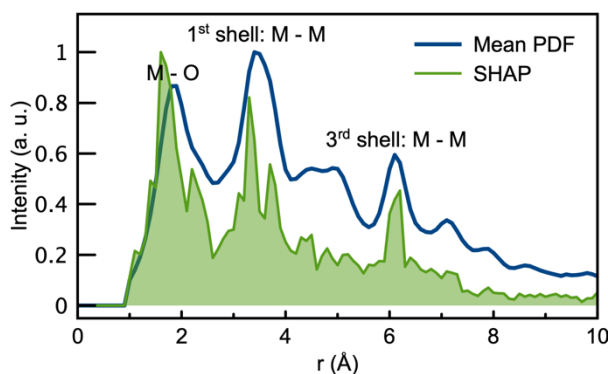


Figure S4: The average absolute SHAP value and PDF are calculated for all POM fragments in the database. Simulation parameters from section A in are used for the PDF simulation. When calculating the average PDF intensity, the intensity beyond the largest distance of the POM fragment is left out. The SHAP values for Q_{\min} , Q_{\max} and Q_{damp} are insignificant (Q_{\min} : 0.003, Q_{\max} : 0.003, Q_{damp} : 0.0006).

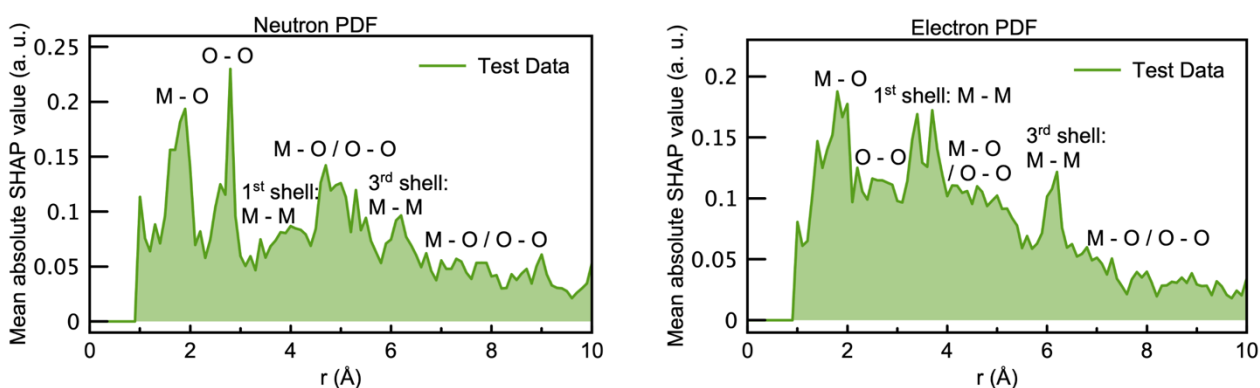


Figure S5: The average SHAP value over classes for the test set plotted for the r_{range} for A) nPDF data, B) ePDF data. Where The SHAP values for Q_{\min} , Q_{\max} and Q_{damp} are insignificant b) Q_{\min} : 0.009, Q_{\max} : 0.009, Q_{damp} : 0.006 and c) Q_{\min} : 0.015, Q_{\max} : 0.010, Q_{damp} : 0.007.

F: Performance versus the number of datasets

Table S6: The mean and standard deviation based on 5 iterations where the model has been trained on different simulated PDFs and predictions have been done on the same test set.

	2	3	5	8	98
xPDF	43.84 ± 0.09	40.32 ± 0.66	53.95 ± 0.00	71.38 ± 0.09	93.95 ± 0.16
nPDF	46.95 ± 0.55	39.37 ± 0.27	54.00 ± 0.36	73.27 ± 0.31	94.27 ± 0.23

ePDF	45.10 ± 0.33	41.67 ± 0.51	50.93 ± 0.27	74.27 ± 0.00	95.98 ± 0.17
xSAXS	29.12 ± 3.32	48.67 ± 0.44	60.95 ± 0.00	70.56 ± 0.11	93.59 ± 0.11
xPDF + xSAXS	55.12 ± 0.22	55.76 ± 0.00	75.17 ± 0.00	83.88 ± 0.18	97.02 ± 0.17
xPDF + nPDF + xSAXS	65.55 ± 0.11	65.1 ± 0.11	77.47 ± 0.09	86.68 ± 0.00	97.52 ± 0.32

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