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# Coherent crystal branches: the impact of tetragonal symmetry on the 2D confined polymer nanostructure 

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The symmetry of polymer crystals greatly affects the optical, thermal conductivity and mechanical properties of the materials. Past studies have shown that the two-dimensional (2D) confined crystallization of polymer nanorods could produce anisotropic structures. However, few researchers have focused on understanding confined nanostructures from the perspective of crystal symmetry. In this research, we demonstrate the molecular chain self-assembly of tetragonal crystals under cylindrical confinement. We specifically selected poly(4-methyl-1-pentene) (P4MP1) with a $4_{1}$ or $7_{2}$ helical conformation (usually crystallizing with a tetragonal lattice) as the model polymer. We found a coherent crystal branching of the tetragonal crystal in the P4MP1 nanorods. The unusual $45^{\circ}$ - and $135^{\circ}-\{200\}$ diffractions and the meridional 220 diffraction (from $45^{\circ}$-tilted crystals) have shown a uniform crystal branching between the $a_{1}$-axis crystals and the $45^{\circ}$-tilted crystals in the rod long axis, which originates from a structural defect associated with tetragonal symmetry. Surprisingly, this chain packing defect in the tetragonal cell can be controlled to develop along the rod long axis in 2D confinement.

## 1. Introduction

Confinement through a nanoporous template is an effective way to produce anisotropic polymer nanostructures (Steinhart et al., 2006; Higuchi et al., 2012; Jinnai et al., 2012; Zhu et al., 2001b; Dai et al., 2018; Lai et al., 2020; Yu et al., 2019; Zeng et al., 2019; Hsiao et al., 2008; Ho et al., 2005). Previous insightful works on confined polymer nanostructures are mainly related to nanophase morphologies, crystal nucleation and orientations and molecular dynamics (Cao et al., 2014; Chung et al., 2010; Wu et al., 2012, 2013; Nakagawa et al., 2012; Danch \& Osoba, 2003; Lutkenhaus et al., 2010; Zhu et al., 2001a; Huang et al., 2001, 2006). Recently, there has been great interest in discovering the impact of the symmetry of polymer crystals under cylindrical confinement via nanoporous alumina under 2D confinement (Zeng et al., 2019; Lai et al., 2020; Yu et al., 2019). A novel nanotwin has been investigated in nylon 6 nanorods with the twin axis aligned with the cylinder axis ( Yu et al., 2019). The 2D confined nanostructure of isotactic polypropylene exhibits five types of diversified $\alpha$-phase crystals due to various types of molecular assembly of $3_{1}$ helices (Zeng et al., 2019). The impact of triclinic symmetry on cylindrical confined hierarchical nanostructures has been illustrated by the rotation of the $a^{*} b^{*}$ plane of the $\alpha$-phase crystals in nylon 612 (Lai et al., 2020).


Figure 1
SEM images showing (a) a top-view of the anodic aluminium oxide (AAO) template with a pore diameter of 70 nm , and (b) the 70 and $(c)$ the 300 nm rods of P4MP1. Transmission electron microscopy (TEM) bright field (BF) images of $(d)$ the 70 and $(e)$ the 300 nm rods of P4MP1.

The above symmetry studies on monoclinic or triclinic crystals under cylindrical constraints mainly illustrate the hierarchical nanostructures based on $2_{1}$ and $3_{1}$ helical chains assembling in confined spaces. However, a study of the tetragonal nanostructure assembling normally by $4_{1}$ or $7_{2}$ helices under 2D constraints has not yet been carried out. Furthermore, an interesting structural feature of tetragonal or similar cell symmetry is that, as found by Lotz and Lovinger, chain packing defects occur during the growth process (Ruan et al., 2006a; Lovinger et al., 1993). For these reasons, in this study, we specifically selected poly(4-methyl-1-pentene) (P4MP1) (most occurring tetragonal crystals) as the model polymer to demonstrate the impact of tetragonal crystal symmetry on the 2D confined polymer nanostructure.

In addition, P4MP1 is an important engineering material with good performance and can be applied in medical appliances, labware materials and optical devices. Complex crystalline polymorphism can be found in the crystallization of P4MP1 (Griffith \& Rånby, 1960; Danch \& Gadomski, 1995; Lopez et al., 1992; DeRosa et al., 1995; Rånby et al., 1962; Chen et al., 2011). The crystal structure of P4MP1, phase I, had been solved by Tadokoro and co-workers using wide-angle X-ray diffraction (WAXD) (space group $P \overline{4} b 2, a=18.88$ and $c=$ $13.8 \AA$ ) (Kusanagi et al., 1978; Ruan et al., 2006a). Four $7_{2}$
helical chains are packing in one tetragonal unit cell. The monoclinic crystal structure of phase II had been discovered by Takayanagi and co-workers, and was later refined by Lotz $\left(a=18.50, b=10.43, c=7.22 \AA\right.$ and $\left.\gamma=113^{\circ}\right)$ (Ruan et al., 2006b). Phase III was determined by De Rosa et al. (1994), in which $4_{1}$ chains pack in a tetragonal cell $(a=19.46$ and $c=$ $7.02 \AA$ ). The hexagonal structure of phase IV was first proposed by Charlet and Delmas, and was refined by De Rosa ( $a=22.17$ and $c=6.69 \AA$ ) (De Rosa, 1999; Aharoni et al., 1981).

Here, P4MP1 nanorods crystallizing at a temperature of $T_{c}$ $\left(100-220^{\circ} \mathrm{C}\right.$ ) were made using the anodized alumina oxide (AAO) template. We first found an axially oriented crystal branching (phase I) of P4MP1 in the rod long axis under cylindrical confinement. The oriented crystal branching takes place along the rod long axis in 2D confinement and promotes $45^{\circ}$-tilted crystals to grow epitaxially from the parent crystals ( $a_{1}$-axis oriented crystals). The polymer nanostructure has been examined by 2D WAXD experiments. Detailed experiments on the morphologies, thermal analysis and crystal structure of the P4MP1 nanorods are presented below.

## 2. Results and discussion

### 2.1. Morphologies

The top-view SEM image of a nanoporous alumina template with self-organized cylindrical nanopores ( 70 nm ) is shown in Fig. 1(a). The pore depth of the AAO template is around $120 \mu \mathrm{~m}$. We used a $5-10 \% \mathrm{KOH}$ solution to etch the templates to release the nanorods after isothermal crystallization at around $100{ }^{\circ} \mathrm{C}$ for 8 h . The released rods were then washed with distilled water several times and placed on a cover glass for the SEM test or on carbon-coated copper grids for TEM measurements.

The SEM images of the 70 and 300 nm rods of P4MP1 are shown in Figs. $1(b)$ and $1(c)$, respectively, while the TEM BF morphologies of the P4MP1 rods with average diameters of 70 and 300 nm are shown in Figs. 1(d) and 1(e), respectively. The


Figure 2
A set of DSC (a) heating and (b) cooling curves of the P4MP1 bulk and the $30,50,70$ and 300 nm rods under 2D confinement (rate $10^{\circ} \mathrm{C} \mathrm{min}^{-1}$ ).

SEM and TEM images both show that the lengths of the P4MP1 nanorods are in the range of tens of microns.

### 2.2. Multiple nucleation of P4MP1 nanorods under confinement

In differential scanning calorimetry (DSC) experiments, all the rod samples of P4MP1 are measured within the nanopores of the AAO template. A set of DSC heating curves for the bulk and for rods with different sizes ( $30,50,70$ and 300 nm ) is shown in Fig. 2(a). It can be seen that the melting peak broadens with decreasing rod diameter. Meanwhile, the onset shoulder temperature for an endothermic peak around $200^{\circ} \mathrm{C}$ in the 30 nm rods decreases compared to that $\left(220^{\circ} \mathrm{C}\right)$ of the bulk, indicating that increased quantities of small crystallites are formed in strongly confined crystallization (small rods).

The DSC curves on cooling can reflect the nucleation type of crystals in 2D confinement (Lutkenhaus et al., 2010; Duran et al., 2011). The DSC cooling traces of PM4P1 in the bulk and confined rods with different sizes are shown in Fig. 2(b). One
sharp and strong exothermic peak at $214{ }^{\circ} \mathrm{C}$ is displayed in the bulk upon cooling. Regarding the different pore sizes, there are obvious changes in the cooling curves of rods confined to nanoporous alumina. For the 300 nm rods, one broad exothermic peak at $195^{\circ} \mathrm{C}$ is seen on the cooling runs. Compared with the cooling traces of the 300 nm rods, the cooling runs of the 70 nm rods display two exothermic peaks at 190 and $173^{\circ} \mathrm{C}$, and some additional exothermic processes arise at $138^{\circ} \mathrm{C}$. Similar observations are found in the 50 and 30 nm rods confined to nanoporous alumina. The two exothermic peaks at 190 and $173^{\circ} \mathrm{C}$ of the 70 nm rods (indicated by ' $\mathrm{e}_{1}$ ' and ' $\mathrm{e}_{2}$ ' in Fig. 2b) are assigned to heterogeneous nucleation. In addition, a homogeneous nucleation peak at $138^{\circ} \mathrm{C}$ indicated by ' o ') appears when the pore size is reduced to 70 nm . The homogeneous nucleation peak becomes stronger with decreasing rod size, reflecting the predominant heterogenous nucleation changing to dominant homogeneous nucleation as the degree of confinement increases (Duran et al., 2011). The reason for this can be described as follows: according to the literature, in bulk crystallization, the crys-


Figure 3
(a) An illustration of the perpendicular measurement geometry of the 2D WAXD experiments. The 2D WAXD patterns of (b) P4MP1 bulk and the (c) 30 , (d) 50 , (e) 70 and ( $f$ ) 300 nm rods. The nanorods within the template were crystallized isothermally at $T_{x}=100^{\circ} \mathrm{C}$ for about 8 h before the WAXD experiments.

Table 1
Observed diffraction Bragg angles, experimental and calculated $d$-spacings and Miller indices of the 2D WAXD patterns.
$2 \theta_{\text {obs }}$ is the observed diffraction Bragg angle. $d_{\text {obs }}$ is the observed $d$-spacing, corresponding to the WAXD patterns shown in Figs. 3(c)-(f). $d_{\text {cal }}$ is the calculated $d$-spacing using the unit-cell parameters $a=b=1.888$ and $c=$ 1.38 nm proposed by Tadokoro and Lotz (Kusanagi et al., 1978; Ruan et al., 2006a).

| $2 \theta_{\text {obs }}\left({ }^{\circ}\right)$ | $h$ | $k$ | $l$ | $d_{\text {obs }}(\mathrm{nm})$ | $d_{\text {cal }}(\mathrm{nm})$ |
| :--- | :--- | :--- | :--- | :--- | :--- |
| 9.43 | 2 | 0 | 0 | 0.937 | 0.944 |
|  | 0 | 2 | 0 | 0.937 | 0.944 |
| 13.35 | 2 | 2 | 0 | 0.662 | 0.668 |
| 16.41 | 3 | $\overline{1}$ | 1 | 0.540 | 0.548 |
| 16.77 | 2 | $\frac{1}{2}$ | 2 | 0.528 | 0.534 |
| 18.25 | 3 | $\frac{2}{2}$ | 1 | 0.486 | 0.490 |
| 18.25 | 2 | $\overline{2}$ | 2 | 0.486 | 0.479 |
| 20.59 | 4 | $\overline{1}$ | 1 | 0.431 | 0.435 |
| 21.18 | 4 | 2 | 0 | 0.419 | 0.422 |
|  | 4 | $\overline{2}$ | 0 | 0.419 | 0.422 |
|  | 2 | 4 | 0 | 0.419 | 0.422 |

tallization is mainly nucleated by heterogeneous nucleation due to the existence of impurity (Duran et al., 2011). With decreasing pore volume (rod size), the majority of the impurity is prohibited from entering into the nanopore.

Therefore, homogeneous nucleation is more dominant in the system under strong confinement. On the other hand, the double heterogeneous nucleation peak reflects secondary and tertiary nucleation corresponding to nucleation at the smooth or corner surfaces, respectively. Epitaxial crystallization occurs in the second or tertiary nucleation in the hightemperature region.

### 2.3. 2D WAXD measurements for confined nanorods

We utilized the Xeuss 2.0 instrument to measure the nanostructures of the $30,50,70$ and 300 nm rods confined to the nanopores. The test geometry of the 2D WAXD experiments is depicted in Fig. 3(a).

Fig. 3(a) shows that the direction of the incident X-ray beam is normal to the rod long axis. The 2D WAXD patterns of the bulk and the $30,50,70$ and 300 nm rods confined to the nanopores of the AAO template are shown in Figs. $3(b)-(f)$, respectively. Fig. $3(b)$ shows the ring pattern of the bulk, indicating that the crystals are randomly oriented. Compared to the ring pattern of the bulk, the 2D WAXD results for the nanorod samples (Figs. $3 c-f$ ) show an anisotropic structure with respect to the rod long axis. The 2D WAXD results for


Figure 4
The azimuthal plots for the particular $d$-spacing $d=6.68 \AA$ corresponding to the 220 diffractions of the 2D WAXD patterns (see Fig. 3) for the (a) 30 , (b) 50 , (c) 70 and (d) 300 nm rods. (e) In the 30,50 and 70 nm nanorods, three 220 diffraction peaks appear at 45,90 and $135^{\circ}$, respectively. ( $f$ ) The azimuthal profiles for the 420 reflections of the 2D WAXD patterns of the 3050,70 and 300 nm rods.
the P4MP1 30 nm rods display several typical reflections at $2 \theta$ (Bragg angle) of $9.43,13.35,16.41,16.77,18.25,20.59$ and $21.18^{\circ}$, with corresponding $d$-spacings of $0.937,0.662,0.540$, $0.528,0.486,0.431$ and 0.419 nm , respectively (Fig. 3c). Based on the phase I unit-cell parameters proposed by Tadokoro and co-workers (Kusanagi et al., 1978), the reflections with $d$ spacings of $0.937,0.662,0.540,0.528,0.486,0.431$ and 0.419 nm can be assigned as 200/020, 220, $3 \overline{1} 1,2 \overline{1} 2,3 \overline{2} 1 / 2 \overline{2} 2,4 \overline{1} 1$ and $240 /$ 420 , respectively. The observed diffraction Bragg angles, experimental and calculated $d$-spacings, and the Miller indices of the 2D WAXD patterns are listed in Table 1.

The $h k 0$ diffractions (200, 020, 220 and 420) in Table 1 show that it is a [001]-zone X-ray diffraction pattern. The stronger meridian reflection with a $d$-spacing of 0.937 nm could be assigned as the 200 reflection. Therefore, the $a^{*}$ axis could be obtained from the 200 reflection, which is superimposed with the long axis of the rod (Fig. 3d). According to the tetragonal crystal $\left(\alpha=\beta=\gamma=90^{\circ}\right)$, the angle between the $a^{*}$ and $b^{*}$ axes is $90^{\circ}$. The $b^{*}$ axis is thus perpendicular to the $a^{*}$ axis and is coincident with the equator. The equatorial reflections, such as the 020 reflections, were not observed due to the limit of the instrument. Similar results were observed in the 2D WAXD patterns of the 50,70 and 300 nm rods (Figs. $3 d, 3 e$ and $3 f$, respectively), which possesses the same $d$-spacings and reciprocal lattice.

Figs. $4(a), 4(b), 4(c)$ and $4(d)$ display the azimuthal plots of the 220 diffractions in the X-ray patterns (Figs. $3 c-f$ ) of the 30,

50, 70 and 300 nm rods, respectively. Compared to the 220 reflections situated at $90^{\circ}$ in weak confinement ( 300 nm rods; Fig. 4d), three $\{220\}$ planes can be clearly observed under strong confinement (rod size less than 100 nm ; Figs. $4 a-c$ ). The positions of the three $\{220\}$ reflections correspond to the azimuthal scanning angles of 45,90 and $135^{\circ}$ in the reciprocal lattice (Fig. $4 e$ ). One 220 diffraction $\left(90^{\circ}\right)$ situated at a meridian is coincident with the rod long axis, indicating that the $45^{\circ}$-tilted crystal has grown under confinement based on tetragonal geometry (Fig. 4e).

The other two 220 or $2 \overline{2} 0$ ( 45 or $135^{\circ}$ ) reflections are part of the [001]-zone diffraction pattern of the tetragonal crystals, reflecting that the $a_{1}$-axis-oriented crystal co-exists in the P4MP1 nanorods. Under this circumstance, the $c$ axes (chain axes) of the tetragonal crystals are perpendicular to the rod long axis and parallel to the direction of the X-ray beam.

On the other hand, it is also interesting to find that the azimuthal profiles of the 420 reflections in the different size rods (Fig. $4 f$ ) show that one of the 420 peaks at $90^{\circ}$ in the 300 nm rods (weak confinement) is split into two 420 peaks of the 30 nm rod (strong confinement). These two fractured 420 reflections of the 30 nm rods are part of the [001] zone diffraction pattern of the $a_{1}$-axis-oriented crystals. Therefore, we can deduce that strong confinement promotes a more ordered structure of the $a_{1}$-axis-oriented crystals.

To obtain more orderly nanostructures to clearly show that this $45^{\circ}$ tilting exists in all the rod sizes, the nanorod samples


Figure 5
The 2D WAXD patterns of the (a) 50, (b) 70, (c) 90 and (d) 300 nm rods isothermally crystallized at $120{ }^{\circ} \mathrm{C}$ under atmospheric pressure for 48 h . The measurement geometry for the X-ray experiments is the same as that described in Fig. 3(a).


The azimuthal profiles for $(a)$ the $\{200\}$ reflections with $d=0.937 \mathrm{~nm}$ for the 2D WAXD patterns of the $50,70,90$ and 300 nm rods. (b) The full width at half maxima (FWHM) of the 200 diffraction of the $a_{1}$-axisoriented and $45^{\circ}$-tilted crystals with different sizes.
were crystallized isothermally at a higher temperature $\left(120{ }^{\circ} \mathrm{C}\right)$ for a longer time (about 48 h$)$ and we carried out

X-ray experiments (Rigaku) on these rod samples with an identical test geometry to that shown in Fig. 3(a). Similar results are observed for the $50,70,90$ and 300 nm rods. Surprisingly, the 200 and 020 reflections are clearly located at the geometric position of the [001]-zone diffraction pattern for the tetragonal crystals in reciprocal space. Figs. 5(a), 5(b), 5(c) and 5(d) show the 2D WAXD patterns of the P4MP1 nanorods, crystallized isothermally at $120^{\circ} \mathrm{C}$ for about 48 h , with diameters of $50,70,90$ and 300 nm , respectively.

The azimuthal scanning profiles of the 200 or 020 reflections with $d=0.937 \mathrm{~nm}$ for the X-ray patterns (Figs. $5 a-d$ ) are shown in Fig. 6(a). Fig. 6(a) also displays that for all rod sizes, the $200\left(\varphi=90^{\circ}\right)$ and 020 reflections $\left(\varphi=180^{\circ}\right)$ belong to the $a_{1}$-axis crystal, and the $200\left(\varphi=45^{\circ}\right)$ and $020\left(\varphi=135^{\circ}\right)$ reflections are attributed to the $45^{\circ}$-tilted crystal. Therefore, the $45^{\circ}$-tilted crystals obviously exist in all the rod sizes identified by the X-ray results (see Figs. $5 a-d$ and Fig. $6 a$ ). Fig. $6(b)$ shows that the FWHM (full width at half maximum) value of the 200 reflections at $90^{\circ}$ for the $a_{1}$-axis crystal drops sharply when the rod size is less than 100 nm , and there is no obvious change in the FWHM values of the 200 reflections for the $45^{\circ}$-tilted crystal when reducing the size of the rods.


Figure 7
The (a) $a b,(b) b c$ and (c) ac plane projections of phase I of P4MP1, as determined by Tadokoro and Lotz and co-workers. (d) The 3D structure of phase I of P4MP1. Gray sticks represent C atoms in the side chain and blue sticks represent C atoms in the main chain. (e) The simulated $h k 0$ diffraction pattern of the P4MP1 crystal structure.

Therefore, compared with the $45^{\circ}$-tilted crystals, the order of the molecular packing of the $a_{1}$-axis crystal was more affected by the degree of confinement.

On the other hand, assuming that the defects of the $a_{1}$-axis and $45^{\circ}$-tilted crystals are identical, the relative amount of the $45^{\circ}$-tilted crystals with respect to the rod size, $f_{45^{\circ} / \text { tilt }}$, can be estimated based on the azimuthal scanning profiles of the $\{200\}$ reflections shown in Fig. 6(a). We calculate that the peak area ratio of the $\{200\}$ diffractions belong to the $45^{\circ}$-tilted crystals, with $\varphi=45$ and $135^{\circ}$, with respect to the total intensity of the $\{200\}$ reflections. The amorphous halo is subtracted. The equations can be described as $f_{45^{\circ} / \text { tilt }}=\left[I(200)_{45^{\circ}}+I(020)_{135^{\circ}}\right] /$ $\left[I(200)_{45^{\circ}}+I(020)_{135^{\circ}}+I(200)_{90^{\circ}}+I(020)_{180^{\circ}}\right]$, with $f_{45^{\circ} / \text { tilt }}$ for the $50,70,90$ and 300 nm rods being about $19,13,24$ and $16 \%$,
respectively, indicating that there is no significant change of $f_{45 \% \text { tilt }}$ with increasing degree of confinement.

Overall, on the basis of the above analysis, two kinds of tetragonal nanocrystal with respect to the rod long axis could be deduced: (i) an $a_{1}$-axis-oriented crystal and (ii) a $45^{\circ}$-tilted crystal. This raises several questions, such as why do the $a_{1}$-axis or $45^{\circ}$-tilted crystals co-exist under 2D confinement? How do the $45^{\circ}$-tilted crystals grow in confinement? How do molecular chains of P4MP1 arrange under 2D confinement?

To understand these questions, we have built the molecular packing model of the phase I crystal with the help of the Cerius ${ }^{2}$ modelling package using the structural data of Tadokoro and Lotz and co-workers (Kusanagi et al., 1978; Ruan et al., 2006a). Figs. $7(a), 7(b)$ and $7(c)$ show the $a b, b c$ and $a c$


Figure 8
(a) Diffraction pattern of the phase I crystals in 2D confinement extracted from the experimental results (Figs. 3 and 5). (b) A schematic illustration of the cell orientation in the parent crystal (marked in orange) and the $45^{\circ}$-tilted crystals (purple). (c) The probable branching mechanism between the $a_{1}$-axis-oriented and $45^{\circ}$-tilted crystals. The orange arrow represents the rod long axis. The helix $A$ and two neighbouring helices $B$ and $C$ are marked in green in part (c). (d) The calculated diffraction pattern with the [001]-zone for the $a_{1}$-axis-oriented crystals. (e) The calculated diffraction pattern for the $45^{\circ}$-tilted crystals; the [001]-zone diffraction pattern is rotated $45^{\circ}$ clockwise in the $a b$ plane around the $c$ axis. (f) The diffraction pattern of the superposition of parts (d) and (e).
plane projections of the phase I crystal, respectively. A threedimensional (3D) unit cell of the phase I crystal is shown in Fig. 7(d). Viewed from the $a b$ projection shown in Fig. 7(a), four $7_{2}$ chains of P4MP1 are located in one tetragonal cell. Figs. $7(b)-(d)$ show that the chain axis of P4MP1 is along the $c$ axis. According to the packing model of phase I, we can obtain the [001]-zone simulated pattern of phase I crystals (Fig. 7e). Therefore, our experimentally observed $h k 0$ diffractions (200, 020,220 and 420) are consistent with the [001]-zone calculated results.

## 2.4. $a_{1}$-axis-oriented crystals

Fig. 8(a) displays a typical 2D WAXD pattern of the P4MP1 nanorods. As mentioned above, the $a_{1}{ }^{*}$-axis orientation can be inferred from the meridional 200 diffraction. The $a_{1}$ axis is superimposed on the $a_{1} *$ axis and is consistent with the rod long axis. The $b^{*}$ axis can be deduced with reference to the equatorial 020 reflections. Combining the $45^{\circ}(\varphi)$ - and $135^{\circ}$ $\{220\}$ reflections, a preferential [200]-directed crystal in the rod long axis was defined as the $a_{1}$-axis-oriented crystal. The reason for the occurrence of $a_{1}$-axis-oriented crystals in the nanopore can be described as follows: in strong confinement, only a lamellar with a specific $\langle h k 0>$ orientation could develop (Steinhart et al., 2006). Meanwhile, it has been found that the fast growth direction of fibrils in the P4MP1 bulk spherulite is along the $a_{1}$-axis direction. In 2D confinement, the [200] direction of fibril crystals tends to be coincident with the rod long axis. Therefore, the occurrence of the $a_{1}$-axisoriented crystal results from the collaborative growth of hierarchical assembling in P4MP1 under cylindrical constraints.

## 2.5. $45^{\circ}$-tilted crystals

A schematic illustration of the $a_{1}$-axis-oriented and $45^{\circ}$ tilted crystals is shown in Fig. 8(b). As analyzed above, the molecular chain axis of the $45^{\circ}$-tilted and $a_{1}$-axis-oriented crystals is parallel to the direction of the X-ray beam, that is, perpendicular to the rod long axis. The $a_{2}$ axis of the $45^{\circ}$-tilted crystals is rotated $45^{\circ}$ clockwise away from the $a_{1}$ axis. A similar observation was made in solution-grown crystals of P4MP1, where unusual $37^{\circ}$ epitaxial crystal branching daughter crystals were discovered by Lotz and co-workers (Ruan et al., 2006a). Based on microscopy studies of the daughter and mother single crystals of P4MP1, we deduce that the origin of the $45^{\circ}$ angle between these two types of crystals in 2D confinement probably results from an epitaxial crystal branching occurring in the $a_{1}$-axis-oriented and $45^{\circ}$-tilted crystals.

An illustration of the epitaxial branching mechanism between the $a_{1}$-axis-oriented and $45^{\circ}$-tilted crystals is shown in Fig. $8(c)$. The nucleation takes place on the $a c$ layer of the $a_{1-}$ axis-oriented crystal and helix $A$ (marked in green) slips by $\frac{1}{4} a$. The $A B$ distance (two neighbouring helices $B$ and $A$ in the new crystal; Fig. $8 c$ ) is about $20.03 \AA$ and the $B C$ distance (two neighboring helices $B$ and $C$ of the parent crystal; Fig. $8 c$ ) is $18.88 \AA$. The size difference of the two lattices is (20.03 -
18.88)/18.88 $\simeq 6 \%$ and falls within the reasonable range of lattice epitaxy. This indicates that the $45^{\circ}$-tilted crystals probably grow epitaxially from the $a_{1}$-axis-oriented crystals. There are several cases of a similar shift occurring in syndiotactic polystyrene and polypropylene (Tosaka et al., 1998, 1999; Lotz et al., 1988; Lovinger et al., 1993). This molecular shift and nucleation are a typical structure defect in the tetragonal unit cell of polymers.

On the other hand, with the help of the Cerius ${ }^{2}$ modelling package, the [001]-zone diffraction pattern of the $a_{1}$-axisoriented and $45^{\circ}$-tilted crystals can be calculated, as shown in Figs. $8(d)$ and $8(e)$, respectively. The diffraction pattern in Fig. 8(e) can be obtained by clockwise rotation of the [001]zone diffraction pattern of the $a_{1}$-axis-oriented crystals (Fig. $8 d$ ) by $45^{\circ}$ in the $a b$ plane around the $c$ axis. The superimposed diffraction patterns (Fig. 8f) show a symmetric and mixed pattern, which resembles the 2D WAXD experimental results of the P4MP1 nanorods shown in Fig. 8(a). Therefore, the simulation results shown in Fig. 8(f) confirm the coherent crystal branching of the tetragonal nanostructure under cylindrical confinement.

In addition, the unique 2 D confined tetragonal nanostructure is significantly different from the X-ray fiber structure or the bulk crystallization. For the X-ray fiber diagram of the phase I crystals in P4MP1, the $c$ axis (chain axis) is parallel to the fiber axis, and the $h k 0$ reflections $200,220,420$, etc., are located at the equator, while the 113 reflections are on the meridian (Kaji et al., 1974). In our case, the 200, 220, 420, etc., reflections correspond to the reciprocal spatial distribution of the [001]-zone diffraction pattern of the phase I crystal. It is known that crystals are randomly oriented in the bulk crystallization of P4MP1. Compared with the arbitrary distribution of lamellar crystals grown from solution, tetragonal crystals in 2D confinement are controlled to form an ordered structure. However, the parent and daughter crystals in solution cannot assemble an ordered structure on a large length scale.

## 3. Conclusion

P4MP1 rods with different sizes under various degrees of confinement exhibit similar nanostructures. A detailed structure analysis based on WAXD, DSC and SEM experiments indicates that tetragonal crystals (phase I) are formed in rods with diameters of $30,50,70$ and 300 nm . Compared to the broad diffraction arcs of the 2D WAXD pattern of the 300 nm rod (weak confinement), the 2D X-ray diffractions of the 30 nm rod change sharply, implying that the molecular chains and lamellae assemble in a more orderly manner under strong confinement due to a collaborative hierarchical assembly of P4MP1 in 2D confinement.

The impact of tetragonal symmetry on the co-operative assembly of 2D confined nanostructures of P4MP1 has been investigated. We first found a coherent $45^{\circ}$ crystal branching of the anisotropic tetragonal nanostructure manipulated by cylindrical confinement. Two sets of [001]-zone diffraction patterns of phase I crystals with $45^{\circ}$ in the $a b$ plane are
superimposed on the 2D WAXD patterns of the P4MP1 nanorods. The 200 reflection located at 45 and $90^{\circ}$ (meridian) on the azimuthal scan profiles with a $d$-spacing of 0.937 nm reflected the formation of $45^{\circ}$-tilted and $a_{1}$-axis-oriented crystals, respectively. The formation mechanism of the $a_{1}$-axisoriented crystals is governed by the fastest crystal growth direction (the [200] direction), coincident with the rod long axis. More importantly, the $45^{\circ}$ angle between the $a_{1}$-axisoriented and branched crystals indicates that a tetragonal structural defect (ac layer shift) takes place along the rod long axis, which helps the new crystals to grow epitaxially from the $a_{1}$-axis-oriented crystals in 2D confinement and results in a coherent crystal branching under cylindrical confinement. In principle, our research on the chain assembly of tetragonal crystals under confinement could contribute to the understanding of the impact of tetragonal symmetry on molecular chain self-assembly in polymer nanostructures under confinement.

## 4. Experimental

### 4.1. Sample and materials

Two low and high molecular weight (MW) P4MP1 samples were obtained commercially from Sigma-Aldrich and used as received. For the low-MW sample, based on the ASTM D1238-01 standard, the melt flow index is $180 \mathrm{~g} / 10 \mathrm{~min}$ $\left(260{ }^{\circ} \mathrm{C} / 5 \mathrm{~kg}\right)$ and the density is around $0.833 \mathrm{~g} / \mathrm{ml}\left(25^{\circ} \mathrm{C}\right)$. The melt index of the high-MW sample is $26 \mathrm{~g} / 10 \mathrm{~min}\left(260^{\circ} \mathrm{C} /\right.$ $5 \mathrm{~kg})$ and the density is $0.835 \mathrm{~g} / \mathrm{ml}\left(25^{\circ} \mathrm{C}\right)$. The AAO templates were purchased from Shangmu Technology Co. Ltd. The average pore diameters of the AAO template are 30, 50, 70,90 and 300 nm , and the pore depth of the AAO template is about $150 \mu \mathrm{~m}$.

The cylindrically confined crystallization of P4MP1 was achieved by infiltrating the P4MP1 melt into the nanopores of the AAO template at a temperature of $260^{\circ} \mathrm{C}$. The residual bulk on the surface of the AAO template needs to be removed. In this article, both high- and low-MW samples provide the same phase behaviour and nanostructure at atmospheric pressure. Both samples provided tetragonal phase I during crystallization within a crystallization temperature range of $100-220^{\circ} \mathrm{C}$. Similar 2D WAXD results for the bulk and nanorod samples can be observed for highand low-MW commercial samples, indicating that this coherent crystal branching is an impact of common tetragonal symmetry on the nanostructure of P4MP1 in 2D confinement. Therefore, there is no need to identify specific samples in this report.

### 4.2. Differential scanning calorimetry (DSC)

All thermal analyses were operated under dry nitrogen with a PerkinElmer DSC 8500 instrument. The samples were first heated to the equilibrium melting temperature and subsequently cooled to $25^{\circ} \mathrm{C}$. The samples were then heated to the equilibrium melting temperature again. The second heating and first cooling curves were recorded. The heating and
cooling rates are both $10{ }^{\circ} \mathrm{C} \mathrm{min}^{-1}$. The weights of all the pans were within a deviation of 0.002 mg .

### 4.3. Scanning electron microscopy (SEM)

The morphologies of the P4MP1 nanorods with different diameters were captured by SEM (Hitachi SU-70). The P4MP1 nanorods were placed on a glass film and coated with gold before measurements.

### 4.4. Transmission electron microscopy (TEM)

A JEOL-1100 instrument was used to obtain the BF image of the P4MP1 nanorods, with an acceleration voltage of 110 kV . The P4MP1 nanorod samples were released from the AAO template etched by $5 \%$ aqueous KOH solution. P4MP1 nanorods in a distilled water droplet were then cast onto the carbon-coated copper grids and were dried in air.

### 4.5. Wide-angle X-ray diffraction (WAXD)

The 2D WAXD experiments (Fig. 3) of the nanorods within the AAO template were carried out using a Xeuss 2.0 wideangle X-ray diffraction system under a 40 kV working voltage and a 30 mA current. The Xeuss 2.0 instrument from French Xenocs was equipped with a Pilatus3 detector and a MetalJetD2 X-ray source $(\lambda=0.134 \mathrm{~nm})$. The 2D WAXD experiments (Fig. 5) were carried out using a Rigaku wide-angle X-ray diffraction system equipped with a Hypix-6000 detector and an FR-X rotating-anode X-ray source $(\lambda=0.154 \mathrm{~nm})$.

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## References

Aharoni, S. M., Charlet, G. \& Delmas, G. (1981). Macromolecules, 14, 1390-1394.
Cao, Y., Wu, H., Higaki, Y., Jinnai, H. \& Takahara, A. (2014). IUCrJ, 1, 439-445.
Chen, S. J., Jin, J. \& Zhang, J. (2011). J. Therm. Anal. Calorim. 103, 229-236.
Chung, T.-M., Wang, T.-C., Ho, R.-M., Sun, Y.-S. \& Ko, B.-T. (2010). Macromolecules, 43, 6237-6240.
Dai, X. Y. L. H. H., Li, H., Ren, Z., Russell, T. P., Yan, S. \& Sun, X. (2018). Macromolecules, 51, 5732-5741.

Danch, A. \& Gadomski, A. (1995). J. Therm. Anal. 45, 1175-1181.
Danch, A. \& Osoba, W. (2003). J. Therm. Anal. Calorim. 72, 641-650.

De Rosa, C. (1999). Macromolecules, 32, 935-938.
De Rosa, C., Borriello, A., Venditto, V. \& Corradini, P. (1994). Macromolecules, 27, 3864-3868.
De Rosa, C., Venditto, V., Guerra, G. \& Corradini, P. (1995). Polymer, 36, 3619-3624.
Duran, H., Steinhart, M., Butt, H. J. \& Floudas, G. (2011). Nano Lett. 11, 1671-1675.
Griffith, J. H. \& Rånby, B. G. (1960). J. Polym. Sci. 44, 369-381.
Higuchi, T., Motoyoshi, K., Sugimori, H., Jinnai, H., Yabu, H. \& Shimomura, M. (2012). Soft Matter, 8, 3791-3797.
Ho, R.-M., Chiang, Y.-W., Lin, C.-C. \& Huang, B.-H. (2005). Macromolecules, 38, 4769-4779.
Hsiao, M.-S., Chen, W. Y., Zheng, J. X., Van Horn, R. M., Quirk, R. P., Ivanov, D. A., Thomas, E. L., Lotz, B. \& Cheng, S. Z. D. (2008). Macromolecules, 41, 4794-4801.
Huang, P., Guo, Y. R. P. Q., Quirk, R. P., Ruan, J., Lotz, B., Thomas, E. L., Hsiao, B. S., Avila-Orta, C. A., Sics, I. \& Cheng, S. Z. D. (2006). Polymer, 47, 5457-5466.

Huang, P. Z. L., Zhu, L., Cheng, S. Z. D., Ge, Q., Quirk, R. P., Thomas, E. L., Lotz, B., Hsiao, B. S., Liu, L. \& Yeh, F. (2001). Macromolecules, 34, 6649-6657.
Jinnai, H., Tsuchiya, T., Motoki, S., Kaneko, T., Higuchi, T. \& Takahara, A. (2012). J. Electron Microsc. 62, 243-258.
Kaji, K., Sakurada, I., Nakamae, K., Shintaku, T. \& Shikata, E. (1974). Bull. Inst. Chem. Res. 52, 308-317.
Kusanagi, H., Takase, M., Chatani, Y. \& Tadokoro, H. (1978). J. Polym. Sci. Polym. Phys. Ed. 16, 131-142.
Lai, Z., Zhang, S., Zheng, N., Yu, S., Ageishi, M., Jinnai, H. \& Cao, Y. (2020). J. Appl. Cryst. 53, 27-33.

Lopez, L. C., Wilkes, G. L., Stricklen, P. M. \& White, S. A. (1992). J. Macromol. Sci. Part C Polym. Rev. 32, 301-406.
Lotz, B., Lovinger, A. J. \& Cais, R. E. (1988). Macromolecules, 21, 2375-2382.

Lovinger, A. J., Lotz, B., Davis, D. D. \& Padden, F. J. (1993). Macromolecules, 26, 3494-3503.
Lutkenhaus, J. L., McEnnis, K., Serghei, A. \& Russell, T. P. (2010). Macromolecules, 43, 3844-3850.
Nakagawa, S., Kadena, K., Ishizone, T., Nojima, S., Shimizu, T., Yamaguchi, K. \& Nakahama, S. (2012). Macromolecules, 45, 18921900.

Rånby, B. G., Chan, K. S. \& Brumberger, H. (1962). J. Polym. Sci. 58, 545-552.
Ruan, J., Alcazar, D., Thierry, A. \& Lotz, B. (2006a). Polymer, 47, 836-840.
Ruan, J., Thierry, A. \& Lotz, B. (2006b). Polymer, 47, 5478-5493.
Steinhart, M., Göring, P., Dernaika, H., Prabhukaran, M., Gösele, U., Hempel, E. \& Thurn-Albrecht, T. (2006). Phys. Rev. Lett. 97, 027801.

Tosaka, M., Tsuji, M., Kohjiya, S., Cartier, L. \& Lotz, B. (1999). Macromolecules, 32, 4905-4911.
Tosaka, M., Tsujl, M., Cartier, L., Lotz, B., Kohjiya, S., Ogawa, T., Isoda, S. \& Kobayashi, T. (1998). Polymer, 39, 5273-5275.
Wu, H., Cao, Y., Ishige, R., Higaki, Y., Hoshino, T., Ohta, N. \& Takahara, A. (2013). ACS Macro Lett. 2, 414-418.
Wu, H., Su, Z. \& Takahara, A. (2012). Soft Matter, 8, 3180-3184.
Yu, S., Lai, Z., Jinnai, H., Zeng, X., Ageishi, M., Lotz, B., Cheng, S. Z. D., Zheng, N., Zhang, S., Feng, X. \& Cao, Y. (2019). Macromolecules, 52, 3298-3305.
Zeng, X., Zhang, S., Zheng, N., Yu, S., Li, X., Ageishi, M., Lotz, B., Liu, G. \& Cao, Y. (2019). Polymer, 179, 121647.
Zhu, L., Calhoun, B. H., Ge, Q., Quirk, R. P., Cheng, S. Z. D., Thomas, E. L., Hsiao, B. S., Yeh, F. J., Liu, L. Z. \& Lotz, B. (2001a). Macromolecules, 34, 1244-1251.
Zhu, L., Mimnaugh, B., Ge, Q., Quirk, R., Cheng, S., Thomas, E., Lotz, B., Hsiao, B., Yeh, F. \& Liu, L. (2001b). Polymer, 42, 91219131.

