Direct measurement of Stokes–Einstein diffusion of Cowpea mosaic virus with 19 μs-resolved XPCS

Kacper Switalski,a Jingyu Fan,b Luxi Li,c Miaoqi Chu,c Erik Sarnello,d Pete Jemian,c Tao Li,d Qian Wangb and Qingteng Zhangc*

a Department of Chemical Engineering, University of Illinois at Chicago, Chicago, IL 60611, USA, b Department of Chemistry and Biochemistry, University of South Carolina, Columbia, SC 29208, USA, c X-ray Science Division, Argonne National Laboratory, 9700 South Cass Avenue, Argonne, IL 60439, USA, and d Department of Chemistry and Biochemistry, Northern Illinois University, DeKalb, IL 60115, USA. *Correspondence e-mail: qzhang234@anl.gov

Brownian motion of Cowpea mosaic virus (CPMV) in water was measured using small-angle X-ray photon correlation spectroscopy (SA-XPCS) at 19.2 μs time resolution. It was found that the decorrelation time \( \tau(Q) = 1/DQ^2 \) up to \( Q = 0.091 \text{ nm}^{-1} \). The hydrodynamic radius \( R_H \) determined from XPCS using Stokes–Einstein diffusion \( D = kT/(6\pi\eta R_H) \) is 43% larger than the geometric radius \( R_0 \) determined from SAXS in the 0.007 M K₃PO₄ buffer solution, whereas it is 80% larger for CPMV in 0.5 M NaCl and 104% larger in 0.5 M (NH₄)₂SO₄, a possible effect of aggregation as well as slight variation of the structures of the capsid resulting from the salt–protein interactions.

1. Introduction

X-ray photon correlation spectroscopy (XPCS) is a coherent X-ray scattering technique that directly probes the dynamic structure factor \( S(Q, \omega) \) in condensed matter. This is done by measuring the intensity autocorrelation function \( g_2(\tau, Q) \) from coherent X-ray scattering intensities (‘speckles’). Aside from the time-averaged static structure factor \( S(Q) \) provided by X-ray scattering (e.g. small-angle X-ray scattering, SAXS), XPCS also provides the fluctuation time scale of \( S(Q) \) similar to dynamic light scattering (DLS). The use of a hard X-ray beam with sub-Ångstrom wavelength not only allows XPCS to probe optically opaque samples (Yavitt et al., 2021) with sophisticated \textit{in situ} (Ju et al., 2019) and \textit{operando} (Lin et al., 2021) sample environments, but also provides spatial sensitivity to structural fluctuation over a wide range of length scales, \textit{i.e.} from sub-micrometre (Dallari et al., 2020) to tens of picometres (Ruta et al., 2020).

The rapid emergence of next-generation X-ray sources, including near diffraction-limited storage rings (DLSRs) such as PETRA IV (Schroer et al., 2018), MAX IV (Björklund Svensson et al., 2019), ESRF–EBS (Chenevier & Joly, 2018) and APS-U (Dooling et al., 2022), as well as free-electron lasers (FELs) such as European XFEL (Tschentscher et al., 2017), LCLS II (Halavanau et al., 2019), SwissFEL (Milne et al., 2017) and SACLA (Yabashi et al., 2017), promises an increase of coherent X-ray flux by several orders of magnitude. Combined with the development of high-speed, high-fidelity pixelated photon-counting X-ray detectors (Pennicard et al., 2018; Allahgholi et al., 2019; Ballabriga et al., 2018; Möller et al., 2019), XPCS will have the potential to fill the ‘no-man’s land’ in \( S(Q, \omega) \) from 0.1 nm to 100 nm and 10⁴ Hz to 10⁸ Hz (Shpyrko, 2014). The advance of the temporospatial...
scales of XPCS will not only extend from the well established works of Brownian motions in colloidal suspensions (Fluerasu et al., 2010; Urbani et al., 2016; Caronna et al., 2008; Möller & Narayanan, 2017; Pal et al., 2018; Ragulskaya et al., 2022), but also expand the scope to cover non-equilibrium dynamics during phase separations, including micelles (Sheyfer et al., 2020) and macromolecules such as domain-forming (Girelli et al., 2021) and free-diffusing (Vodnala et al., 2018) protein suspensions.

One of the simplest and biologically relevant hydrodynamic scenarios in condense matter is the diffusion of viruses and virus-like particles. Viruses are typically monodisperse with a <100 nm geometric radius $R_0$ and are incapable of self-propelled motion (Tejeda-Rodrı́guez et al., 2019). The dynamics of dilute virus suspension in aqueous environments is therefore speculated to behave largely similar to Brownian motion (Hammermann et al., 1997; Song et al., 1991). Cowpea mosaic virus (CPMV) is a non-enveloped, icosahedral-shaped virus with a radius of ~15 nm. The genome RNA of CPMV is surrounded by its capsid, a spherical shell comprising 60 identical units each consisting of two types of protein (Fig. 1). CPMV is an ideal model for virus-like particles in this study because (1) CPMV can be readily harvested and purified in gram quantities (Wang et al., 2002); (2) the molecular structure of CPMV is known to sub-nanometre precision (Lin et al., 1999); (3) CPMV can be engineered via genetic mutations (Johnson et al., 1997) and chemical modification with high selectivity (Strable et al., 2004; Souza et al., 2002; Wang et al., 2002), making it useful as a template for hybridized nano-materials (Uchida et al., 2007), vehicles for targeted drug delivery (Beatty & Lewis, 2019) and scaffolds for vaccine development (Lizotte et al., 2016; Micromont et al., 2008).

Here we demonstrate the small-angle XPCS (SA-XPCS) measurement on the hydrodynamics of dilute CPMV suspension in aqueous environments. Our SAXS results yield a geometric radius $R_0$ of 13.0 nm for CPMV, consistent with previous literature (Lin et al., 1999). However, the hydrodynamic radius $R_H$, determined by directly measuring the diffusion coefficient using XPCS, is 18.7 ± 0.7 nm in the buffer solution (0.007 $M$ K$_3$PO$_4$, 23.4 ± 1.6 nm with an additional 0.5 $M$ NaCl and 26.5 ± 1.3 nm with an additional 0.5 $M$ (NH$_4$)$_2$SO$_4$. The difference of $R_H$ in different salt solutions may arise from a combination of factors including ionic strength and effects from the Hofmeister series. The remainder of this paper is organized as follows: Section 2 describes the preparation of the CPMV samples; Section 3 outlines the instrumental conditions for SA-XPCS measurements; Sections 4 and 5 summarize the SAXS and XPCS results which lead to the evaluation of $R_0$ and $R_H$, respectively; Section 6 examines the differences between $R_0$ and $R_H$ under different ionic strengths and salt types; and Section 7 provides an outlook of the scientific opportunities that can be enabled by microsecond-resolved XPCS and ultra-high brilliance of the coherent X-ray beams of next-generation light sources.

2. CPMV sample preparation

Cowpea plants approximately 1 month old were inoculated with CPMV. The leaves from the host plant were crushed and added to 0.01 $M$ K$_3$PO$_4$ buffer at pH 7.8 with 0.2% mercaptoethanol. The mixture was centrifuged at 9000 rpm for 15 min and the supernatant was treated with a 1:1 ratio of CHCl$_3$:1-butanol. The aqueous portion was separated and CPMV was precipitated by adding polyethylene glycol 8 K and NaCl. The resultant pellets were resuspended in 0.01 $M$ K$_3$PO$_4$ buffer at pH 7.8. After a final ultracentrifugation at 42000 rpm for 2.5 h, pure CPMV was obtained and then resuspended overnight in 0.1 $M$ K$_3$PO$_4$ buffer at pH 7.8 or in deionized water to produce the stock solution with 10.96 mg ml$^{-1}$ CPMV concentration. The stock solution was aliquoted and mixed at a 7:1 ratio with deionized water, 4 $M$ NaCl solution and 4 $M$ (NH$_4$)$_2$SO$_4$, respectively, to produce three sample conditions with identical CPMV concentrations (9.59 mg ml$^{-1}$) but with 0.007 $M$ K$_3$PO$_4$, 0.007 $M$ K$_3$PO$_4$ + 0.5 $M$ NaCl and 0.007 $M$ K$_3$PO$_4$ + 0.5 $M$ (NH$_4$)$_2$SO$_4$, hereafter referred to as samples A, B and C. The samples were then pipetted into 40 mm-long, 2 mm-diameter thin-walled quartz capillary tubes (Charles–Supper) and fitted into customized aluminium blocks to maintain the sample temperature at 6°C throughout the SA-XPCS measurements.

3. SA-XPCS beamline instrumentation

The SA-XPCS measurements were performed at station 8-ID-I of the Advanced Photon Source at Argonne National...
Laboratory. The X-ray beam was generated from a tandem of 33 mm-period, 2.4 m-long undulators. The beam was then deflected by a plane silicon mirror at a 5 mrad angle to remove the higher harmonics, and passed through a Ge(111) monochromator with a 0.03% relative bandpass to select a longitudinally coherent X-ray beam with a photon energy of 10.94 keV. For transverse coherence, a 180 μm (vertical) × 15 μm (horizontal) portion of the beam was selected by tungsten-blade guard slits and then focused vertically using 15 pieces of beryllium compound refractive lenses (CRLs). The final beam footprint on the sample is 15 μm (horizontal) × 10 μm (vertical) with a flux of $1.2 \times 10^{10}$ photons s$^{-1}$.

The transmitted coherent X-ray scattering intensities were collected 8 m downstream of the sample using X-ray Seamless Pixel Array 500k (XSPA-500k), a single-photon-counting detector with a pixel size of 76 μm and tunable frame rate up to 52 kHz (Nakaye et al., 2021). For the current study, the frame rate was fixed at 52 kHz and each measurement consisted of 100000 detector frames collected continuously over a total duration of 1.92 s. Due to the extremely low scattering rate of CPMV, each individual measurement of 100000 frames was further repeated 14328 times for sample A, 7554 times for sample B and 13054 times for sample C, resulting in approximately one billion detector frames for each sample condition. The results from repeated measurements were averaged to produce $g_2(r, Q)$ with sufficient statistics for quantitative analysis. As a side note, to facilitate peer communication and community growth, the entire data lifecycle of this study has been made 100% open-source: (1) all communication and community growth, the entire data life-cycle of this study has been made 100% open-source: (1) all Python-based beamline control system (Arkilic et al., 2017); (2) the sparsified detector frames (SA-XPCS measurements were performed using Bluesky, a Python-based beamline control system (Arkilic et al., 2017); (2) the sparsified detector frames (~25 TB) were transferred and analyzed in near real-time using the APS Data Management workflow (Veseli et al., 2018); (3) the SA-XPCS results for each sample condition were averaged and visualized in pxyPcsViewer (Chu et al., 2022); (4) the reduced results were analyzed using pxyPcsViewer script mode and plotted using Matplotlib in a JupyterLab environment. Full .ipynb files including data analysis, figure rendering and the figures (embedded inline) can be found on GitHub (Zhang, 2022); (5) the manuscript was prepared in Overleaf. More details regarding the XAXS and XPSCS methods in this study can be found in Sections 4 and 5.

4. SAXS and $R_0$

Fig. 2(a) shows the 2D SAXS measured from sample A, where the 100000 frames acquired at a 52 kHz frame rate are averaged over time to produce the equivalent of an SAXS measurement from a single 1.92 s exposure. The 2D SAXS is then further averaged over 1000 repeating measurements to improve the statistics. The white circular region in Fig. 2(a) is the shadow from an ~3 mm-diameter tungsten cylinder placed ~10 cm in front of the detector to block the direct beam (i.e. beamstop), and the white triangular region at the bottom right corner is the cutoff from the downstream rim of the 8 m-long vacuum tube (i.e. flight path). Both regions were masked out and excluded from the SAXS and XPCS analyses. Fig. 2(b) shows the 1D SAXS azimuthally averaged from the 2D SAXS in Fig. 2(a), where the pixels in Fig. 2(a) were grouped into 270 logarithmically spaced partitions of $Q$ and the scattering intensities were averaged within each partition. The form factor of CPMV is consistent with the prediction from nanospheres with a Gaussian size distribution (Rieker et al., 1999), yielding a geometric radius $R_0$ of 13.0 ± 1.2 nm, consistent with the range of 12.7 nm (twofold axis) to 15.4 nm (fivefold axis) for the icosahedral CPMV structure measured using X-ray diffraction (Lin et al., 1999). For samples B and C, signs of aggregation can be observed from the tilting of the 1D SAXS at the lower $Q$ region; however, the change is slightly more pronounced in sample C than sample B. Besides the fact that the ionic strength in sample C is three times higher than that of sample B, we also notice that, in the Hofmeister series, both the cation and the anion of NaCl in sample B, yellow triangle), 9.59 mg ml$^{-1}$ CPMV in 0.007 M K$_2$PO$_4$ and 0.5 M NaCl (sample B, yellow triangle), 9.59 mg ml$^{-1}$ CPMV in 0.007 M K$_2$PO$_4$ and 0.5 M (NH$_4$)$_2$SO$_4$ (sample C, green square). The solid blue line is the form factor calculated from spherical particles with a Gaussian distribution of the radius (average = 13.0 nm, standard deviation = 1.2 nm).

Figure 2

(a) SAXS from 9.59 mg ml$^{-1}$ CPMV suspension in 0.007 M K$_2$PO$_4$ buffer (sample A) averaged over 100000 frames collected continuously within 1.92 s. The result was further averaged from 1000 repeated measurements to improve the statistics. (b) Azimuthal average of (a) for sample A (red circles), 9.59 mg ml$^{-1}$ CPMV in 0.007 M K$_2$PO$_4$ and 0.5 M NaCl (sample B, yellow triangle), 9.59 mg ml$^{-1}$ CPMV in 0.007 M K$_2$PO$_4$ and 0.5 M (NH$_4$)$_2$SO$_4$ (sample C, green square). The solid blue line is the form factor calculated from spherical particles with a Gaussian distribution of the radius (average = 13.0 nm, standard deviation = 1.2 nm).
5. XPCS and $R_{H}$

The difference in the ionic strength and salt type among samples A, B and C is more pronounced in the Stokes–Einstein diffusion of CPMV as directly probed by XPCS. Fig. 3 shows $\Delta g_2 = g_2 - 1$ (in the absence of correlation, $g_2 = 1$) at $Q = 0.031$ nm$^{-1}$ from sample A, where $g_2(Q, t)$ is calculated using the following method (Zhang et al., 2018).

$$G_2 = \langle I_i(i(t) I_j(i(t + \tau)) \rangle_{t},$$

$$IF = \langle I_i(i(t)) \rangle_{t},$$

$$IP = \langle I_i(i(t + \tau)) \rangle_{t + \tau},$$

$$g_2(Q, t) = \frac{\langle G_2 \rangle_{i,j}}{\langle IF \rangle_{i,j} \langle IP \rangle_{i,j}}.$$

(1)

Here, $t$ and $t + \tau$ are the measurement time of detector frames within the 100000 frame sequence and $\tau$ is the delay time between the two frames. The time average $\langle \ldots \rangle_t$ and $\langle \ldots \rangle_{t+\tau}$ go from 0 to $T - \tau$ and $\tau$ to $T$, respectively, where time 0 and $T$ are the start and end times of the frame sequence. In case the scattering intensity does not vary within the measurement (e.g. Fig. S1 of the supporting information), $IF$ and $IP$ are invariant of $\tau$ and are equal to the 2D SAXS pattern in Fig. 2(a). When evaluating $G_2$, $IF$ and $IP$ at larger delay time $\tau$, the frames are binned in an exponentially recursive manner based on the multi-tau algorithm used in DLS (Figs. S3 and S4).

In the spatial regime, $i$ and $j$ are pixel indices and $Q$ denotes the momentum transfer of the region where pixel binning $\langle \ldots \rangle_{i,j}$ is performed. In equation (1), the pixel binning $\langle \ldots \rangle_{i,j}$ is first performed using the same azimuthal averaging method that converts 2D SAXS [Fig. 2(a)] to 1D SAXS [Fig. 2(b)] with a width of approximately 2 pixels ($\Delta Q \simeq 1 \times 10^{-3}$ nm), and the resulting $g_2$ is further binned by a factor of 10 in $Q$ ($\Delta Q \simeq 1 \times 10^{-2}$ nm) to improve the overall signal to noise ratio. Use of initially narrower regions of pixel binning in the $g_2$ calculation reduces intensity variation from 1D SAXS within the binning region, which is known to increase the $g_2$ baseline as detailed in previous studies (Sheyfer et al., 2020). Note that the pixel binning is performed on $G_2$, $IF$ and $IP$ instead of $g_2$-per-pixel, i.e. pixel-wise division of $G_2/(IF \times IP)$. Performing the pixel binning before the division allows for evaluation of the coherence factor $\beta$ (explained later in Fig. 3) in the absence of temporal decorrelation, a quantity similar to fringe visibility in a multi-slit diffraction with a visible laser. The error in $g_2$ is determined as the standard deviation of $g_2$-per-pixel within the larger $\Delta Q \simeq 1 \times 10^{-2}$ nm region on the detector where $g_2(Q, t)$ is determined.

Typically, for samples with low scattering rates, $g_2$ is determined for each individual measurement and then averaged over repeating measurements to improve the statistics (Zhang et al., 2021). However, due to the extremely low scattering rate of the CPMV samples ($\sim 7 \times 10^{-5}$ photon per pixel per detector frame), $G_2$, $IF$ and $IP$ were averaged first before determining $g_2$ and the error using equation (1). The averaged $G_2$ has sufficient statistics to help identify noisy pixels that are too subtle to be flagged from the averaged scattering intensity, e.g. pixels with abnormally high correlation values due to the overlap in the gating signals of the double-counters on the pixel (Zhang et al., 2016), an artifact whose impact on $g_2$ is inversely proportional to the count rates.

The dynamic time scale $\tau_d(Q)$ of CPMV colloidal suspension at various length scales is evaluated by fitting $\Delta g_2(Q, t, \tau)$ at different $Q$ values with a simple exponential function $\Delta g_2(Q, t, \tau) = \beta \exp[ -2 \tau \tau_d(Q) ]$ (solid blue line in Fig. 3), where $\beta = 0.14$ is the coherence factor of the beamline and was determined from the $g_2(Q, \tau)$ of a static reference sample. We notice that $\tau_d(Q)$ follows the prediction from the Stokes–Einstein equation of $1/(DQ^2)$ up to $\sim 0.1$ nm$^{-1}$, as shown by the dashed red line in the inset of Fig. 3. The hydrodynamic radius $R_{H}$ of CPMV was determined from the diffusivity $D = kT/(6\pi \eta R_{H})$, where $k$ is the Boltzmann constant, $T = 279$ K and $\eta = 1.520 \times 10^{-3}$ Pa s is the viscosity of water at 6°C (Kestin et al., 1978). We found $R_{H} = 18.7 \pm 0.7$ nm for sample A, which is 43% larger than $R_0 = 13.0 \pm 1.2$ nm determined from SAXS. Fig. 4 shows the Stokes–Einstein diffusion measured from samples A, B and C. Taking into account the increase of water viscosity in the presence of electrolytes using the Jones–Dole model (Jenkins & Marcus, 1995), $\eta = 1.536 \times 10^{-3}$ Pa s for sample B and $\eta = 1.672 \times 10^{-3}$ Pa s for sample C, which lead to $R_{H} = 23.4 \pm 1.6$ nm for sample B and $R_{H} = 26.5 \pm 1.3$ nm for sample C, respectively. The effect of $R_{H} > R_0$ is therefore more pronounced in solution with higher ionic strength and in (NH$_4$)$_2$SO$_4$ than NaCl.

6. Discussion

Although the diffusion of CPMV follows Stokes–Einstein equations, we noticed that $R_{H}$ is larger than $R_0$ for all solvent conditions considered. Consistency among SAXS and XPCS results from subsets of 100000-frame acquisitions (Figs. S1 and S2, respectively) indicates there is no observable radiation damage. In addition, at a 0.7% CPMV volume fraction, the
solubility of proteins (3) attractions between the coat protein shell and the genomic RNA core. As a result, it is extremely difficult to untangle the complex effects of ions to all three interactions and to understand how those interactions influence the \( R_t \) of CPMV particles in aqueous environments, especially given the ion-specificity effects that play a critical role in the biological and physiological behaviors of biomacromolecules and viruses. XPCS therefore provides a direct analytical tool to monitor the hydrodynamic properties of nanoscale particles which can help us to uncover the complexity of ion-specific effects on virus and other nanoscale bioassemblies.

7. Outlook

Biomacromolecules present richer tunabilities in their structural and dynamic properties compared with inorganic nanoparticles because the very structure of the molecules can be altered either by design (genetic sequence) or by environment (temperature, ionic strength etc.). These changes can trigger phase transitions, where reconfiguration of molecular structures leads to increased interaction strength and causes biomacromolecules to self-assemble into mesoscale domains or fractals, eventually resulting in macroscopic structures with a wide range of porosity, viscosity, elasticity, opacity etc. Such non-equilibrium dynamics are characterized by their telescopic length scales, rapid fluctuation and constantly evolving dynamics, which can be technically challenging for raster imaging techniques (e.g. electron microscopy) and DLS but is the forte of XPCS. In our current study, the spatial and temporal range probed by XPCS is 69.0 to 226.3 nm and 19 \( \mu \)s to 1.24 s due to limitation from beamline geometry and detector frame rate. In addition, each sample condition requires 12–24 h to accumulate sufficient statistics due to the very low scattering rate of CPMV, which rules out studies of non-equilibrium dynamics with the current coherent X-ray flux. However, we expect to break through these technical ceilings in the next few years with both next-generation X-ray sources that promise 100 times higher coherent X-ray flux (DLSRs and FELs) and the development of state-of-the-art, dedicated XPCS beamlines with high-speed, high-fidelity X-ray detectors. Combined with beamline automation, open-source software packages and rapid growth in artificial intelligence, our study will hopefully pave the road to guided self-assembly of emergent biomaterials, where the exact dynamic pathway of the biomacromolecules can be fine-tuned based on feedback from \textit{in situ/operando} XPCS to produce bio- or bio-compatible materials with tailored properties.

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